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RESEARCH ARTICLE

An Adaptive and Robust Method for Oriented Oversampling With Spatial Information for Imbalanced Noisy Datasets

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ABSTRACT Imbalanced datasets have a large negative impact on the classifiers, biasing the classification results towards the majority class. Since imbalanced data distribution is an inevitable and significant challenge in the real world, many variants of SMOTE have been proposed. However, current oversampling methods still need improvement because they rely on hyperparameter optimization, overgeneralize due to emphasizing specific synthetic regions, randomly synthesize samples or suffer from noise performance degradation. To overcome the above problems, we propose an adaptive and robust method (OOSI) for oriented oversampling with spatial information to deal with imbalanced noisy datasets. OOSI is a rare adaptive and effective oversampling method that can fill the gaps of existing methods through dataset-specific spatial partitioning and information quantization, three-stage noise suppression, and spatially-informed generation path improvement. Firstly, a specific and adaptive clustering space is adaptively derived through the data space division of the characteristics of datasets. Then, all minority clusters are assigned a reasonable number of synthetic samples to simultaneously address intra- and inter-class imbalances by integrating the cluster samples' intra-cluster sparsity and the multi-class density information. After differentiating and identifying the noise, oriented weights are assigned based on the multi-class information level to guide the enhancement of the generation path of the synthetic samples and prevent the generation of extra noisy and overlapping samples. Extensive experiments demonstrate that the proposed algorithm outperforms 11 prominent oversampling algorithms on 11 real-world datasets with varying noise levels.

INDEX TERMS Imbalanced learning, label noise, oriented oversampling.

19 I. INTRODUCTION

Imbalanced noisy learning refers to the problem of training 20 models on datasets that exhibit imbalanced class distributions 21 and contain noisy or mislabeled samples [1]. In this case, 22 there is a significant difference in the number of samples of 23 different classes, which will cause the classifier to be biased 24 towards the majority class in learning while ignoring the 25 characteristics of the minority class, thereby impacting the 26 classification performance [2]. Additionally, the presence of 27 noisy or mislabeled samples further complicates the learning 28 process as they introduce errors and mislead the model 29

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during training. The objective of this paper is to propose 30 an adaptive and robust oversampling that adaptively divides 31 and quantizes spatial information to inhibit the intrusion of 32 noise and to guide reasonable sampling path improvement. 33 Data imbalance is common and inevitable in many real-34 world applications, such as fraud identification [3], medical 35 diagnosis [4], sentiment analysis [5], anomaly detection [6], 36 and other fields. Among them, due to the characteristics 37 of the data itself, certain classes of samples are inevitably 38 challenging to obtain or cost highly. Meanwhile, the minority 39 samples involve important or sensitive information. For 40 example, in rare species recognition or cancer diagnosis, 41 the minority class has a low occurrence rate in real life, 42 but ignoring or misclassifying rare species and cancer will 43

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reduce the generalization ability and robustness of the model, 44 resulting in severe practical consequences [7]. Therefore, 45 how to effectively deal with data imbalance and improve the 46 generalization ability of classifiers is a research topic with 47 crucial theoretical significance and practical value in machine 48 learning. 49

In-depth research on imbalanced learning has developed 50 numerous algorithms, which can be broadly categorised 51 as cost-sensitive approaches, algorithm-level approaches, 52 and data-level approaches [8]. Cost-sensitive approaches 53 assign higher misclassification costs to minority classes to 54 emphasize the learning of minority classes [9]. Nevertheless, 55 not only do the costs of misclassifying various classes 56 depend on specific data, but it is also frequently difficult 57 to measure precisely. Algorithm-level approaches improve 58 learning in the minority class by enhancing or designing 59 new algorithms to deal with imbalanced issues [10]. Data-60 level approaches directly manipulate datasets by resampling 61 to equalise class number disparities [11]. As a result of their 62 independence from particular scenarios and classifiers, data-63 level approaches have become the most prevalent strategies 64 in imbalanced learning. 65

Data-level approaches replicate or synthesise minority 66 samples (i.e., oversampling), remove majority samples (i.e., 67 undersampling), or combine minority synthesis and majority 68 removal (i.e., hybrid sampling) to balance the quantity of 69 different classes [12]. Although eliminating samples might 70 somewhat reduce the amount of data, undersampling can 71 easily result in the loss of crucial information. Furthermore, 72 by evaluating the area under the ROC curve (AUC), 73 74 Batista et al. have further shown that undersampling typically performs worse than oversampling [13]. Currently, synthetic 75 minority oversampling technology (SMOTE) is one of the 76 most influential oversampling algorithms, which randomly 77 synthesizes minority samples based on their k-nearest 78 79 neighbors [14]. Due to its simplicity and efficiency, it has become the established sampling mechanism for subsequent 80 oversampling algorithms. 81

Meanwhile, some researches have demonstrated that data 82 imbalance is not the only factor that hinders learning. 83 84 Class overlap, small separation within classes, and label noise can exacerbate the complexity of imbalanced learning, 85 resulting in suboptimal performance [15]. In particular, the 86 unavoidable noise itself often has a substantial influence 87 on the learning process [16]. During model training with 88 label noise, models may learn incorrect or misleading 89 patterns between features and labels, which can lead to 90 decreased accuracy. Additionally, the model could over-adapt 91 to the noise in the training data, failing to discern between 92 true underlying patterns and noisy labels, as a result of 93 which the model does not generalize well beyond the 94 training set [17]. Label noise affects the decision boundary 95 of the classifiers. Moreover, based on the current ran-96 dom sampling mechanism, it is simple to introduce extra 07 noise and overlapping samples, further increasing learning 98

difficulty [18]. In recent years, various sampling algorithms have been proposed from different perspectives, such as noise-filtering approaches, region-emphasizing approaches, 101 clustering-based approaches, etc [19]. Nevertheless, they still have the following drawbacks: (1) Most methods easily introduce extra hyperparameters. (2) Most methods are ineffective 104 at detecting suspect noise and prone to overgeneralization. (3) Most of the current sampling algorithms are based on 106 the random linear sampling mechanism of SMOTE, which is not only limited by its blindness, but also the noise will 108 exacerbates the performance degradation resulting from its blindness.

Given that oversampling plays an important role in Mixup, it improves the learning ability and robustness of traditional models to minority classes. For the absence of minority classes, oversampling compensates the traditional biased models by synthesizing minority samples. Oversampling not only enhances the diversity of the data, it mitigates the bias of the model that tends to predict common classes and avoids overfitting. Given the current challenges of learning difficulty exacerbated by imbalance and label noise, as well as the limitations of current sampling methods that require additional hyperparameter optimization and fail to effectively detect noise, resulting in performance degradation due to blind random sampling. we are committed to exploring an adaptive and robust oversampling method that guides sample synthesis to alleviate blind random sampling and effectively deal with imbalanced noisy learning.

To fill gaps, an adaptive and robust method (OOSI) for 127 oriented oversampling with spatial information is proposed 128 to deal with imbalanced noisy datasets. First, a dataset-129 specific adaptive spatial partitioning strategy is proposed to 130 effectively fit the data distribution characteristics to obtain 131 a dataset-specific adaptive clustering space. Then, by inte-132 grating the intra-cluster sparsity and multi-class density 133 information, the spatial distribution information is adequately 134 quantified and guides the reasonable sample generalization 135 of the cluster space to alleviate both intra- and inter-class 136 imbalance problems. Finally, to avoid noisy samples from 137 introducing additional and chaotic generalization, sample 138 synthesis paths are guided based on the level of multi-class 139 information among non-noisy seed samples, keeping new 140 samples away from chaotic regions. In conclusion, the 141 proposed OOSI approach is expected to deal with imbalanced 142 noisy datasets benefiting from oriented oversampling with 143 spatial information and the innovative three-stage noise 144 suppression strategy. Oriented oversampling with spatial 145 information guides the rational allocation of the number of 146 samples within the cluster and the improvement of the gen-147 eration path of the synthesized samples to ensure the quality 148 of the synthesized samples. The innovative three-stage noise 149 suppression strategy consists of optimizing the clustering 150 space and avoiding the chaotic expansion of noisy samples 151 and guiding the improved synthesis. The main advantages 152 of OOSI compared to existing methods are that a) It is 153

a rare adaptive and robust oversampling method; b) it 154 can prevent noise hazards with the innovative three-stage 155 noise suppression strategy rather than removing them; c) it 156 can create safe synthetic minority samples with spatial 157 information to avoid overgeneralization and blindness of 158 SMOTE. The following are the main contributions of this 159 paper: 160

• A spatial partitioning strategy for dataset specificity is 161 proposed to adaptively mine dataset-specific distribution 162 information. 163

The proposed OOSI is an adaptive and rare oversam-164 pling method. It not only guides reasonable sample 165 generalization and sample synthesis path enhancement 166 through spatial information, but also addresses the 167 common and unavoidable imbalance and noise hazards 168 at the same time. 169

• Extensive comparative experiments with 11 mainstream 170 sampling algorithms demonstrate the effectiveness and 171 superiority of the proposed OOSI on 11 datasets and 172 5 classifiers with varying noise levels. 173

The rest of the paper is organized as follows: Section II 174 briefly reviews relevant literature. Section III presents 175 the details and rationale for the proposed oversampling 176 method. Section IV reports empirical results of extensively 177 contrasting. Section V summarizes our work. 178

II. RELATED WORK 179

The oversampling technique, the most widely used strategy 180 in imbalanced learning, enhances the data class distri-181 bution by generating new minority samples. In addi-182 tion, the linear sampling mechanism built on SMOTE is 183 currently the most effective resampling paradigm [20]. 184 Numerous SMOTE-based variations have been devel-185 oped due to the ubiquity and inevitability of imbalanced 186 noisy applications. Representative approaches include noise-187 filtering approaches, region-emphasizing approaches, and 188 clustering-based approaches [21]. 189

Filtering-based approaches rely on various noise-filtering 190 strategies to clean data. Based on the invasion of hetero-191 geneous spaces by distinct classes, Batista et al. first pro-192 posed employing data-cleaning approaches for oversampling 193 methods to generate balanced datasets with better-defined 194 clusters [13]. The SMOTE-Tomek links and SMOTE-ENN 195 delete samples of multiple categories based on the Tomek links and any sample misclassified by its three nearest 197 neighbours, respectively. Moreover, Yang et al. rectified the 198 sampling results of ant colony clustering by eliminating 199 noisy and overlapping samples with Tomek links cleaning 200 technology [22]. Ramentol et al. proposed SMOTE-RSB 201 based on rough set theory and approximate editing under 202 subsets, which iteratively filters noisy samples from original 203 and synthetic data with similarity thresholds [23]. In addition, 204 S'aez et al. and Ramentol et al. eliminate noisy samples 205 iteratively by iterative partition filters [24] and distinct 206 thresholding strategies based on instance selection in rough 207 set theory [25], respectively. Proper data cleansing is feasible 208

in the presence of noisy or improperly synthesised samples. 209 However, the strategy of iterating or optimizing the threshold 210 is vulnerable to high cost and hyperparameter optimization 211 and limited by practical scenario applications.

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To maintain the security of fresh samples and prevent the 213 production of noisy samples, region-emphasizing approaches 214 typically synthesise samples in particular regions. By care-215 fully calculating the ratio of minority samples in the nearest 216 neighbour, safe-level smote emphasises synthesising new 217 samples near bigger safe-level samples, that is, the minority 218 aggregation region [26]. The focus of MWMOTE is on 219 synthesising new samples from informative minority samples 220 near the decision boundary with assigned weights by their 221 majority class distance [27]. Additionally, random space 222 division sampling [28] and constrained oversampling [29] 223 concentrate sampling on the boundary region through the 224 random space division of the complete random forest and the 225 minority class boundary defined by ant colony optimization, 226 respectively. Nevertheless, region-emphasizing approaches 227 are susceptible to over-generalization and might ignore the 228 inherent characteristics of the data. In order to concentrate 229 more on difficult-to-learn samples, He et al. dynamically 230 modify the weights and distribute the number of new samples 231 generated from each minority sample based on the data 232 neighbourhood distribution [30]. Inspired by ADASYN, 233 numerous methods employ similar mechanisms to regulate 234 the number of new artificial instances associated with each 235 minority sample or subset of minority samples [31], [32]. 236 Pan et al. proposed an adaptive sampling method called 237 adaptiveSMOTE. It improves the SMOTE by adaptively 238 selecting the inner and danger areas from the minority 239 class, thereby compiling new minority samples from the 240 selected data, thus preventing the class boundary expansion 241 and enhance the distribution characteristics of the original 242 data [33]. Chen et al. proposed a robust method known 243 as RSMOTE. It identifies non-noisy samples based on 244 the locally salient characteristics of minority samples and 245 reweights the synthetic number of new samples based on their 246 degree of chaos [34]. 247

Clustering-based approaches divide sub-clusters to guar-248 antee the quality of synthetic samples by following the 249 original distribution information. Bunkhumpornpat et al. 250 proposed a sampling algorithm based on a density clus-251 tering strategy, DBSMOTE. It synthesizes new samples 252 along the shortest paths between the minority and the 253 pseudo-centroids of arbitrarily shaped clusters found by 254 DBSCAN [35]. Although DBSMOTE has a certain noise 255 resistance due to DBSCAN, dense synthetic samples near 256 the centroid are prone to overfitting. Moreover, Iman et al. 257 proposed A-SUWO, an adaptive semi-unsupervised weighted 258 oversampling method. It clusters minority instances via 259 semi-unsupervised hierarchical clustering and oversamples, 260 considering the distance from the majority class to avoid 261 generating overlapping samples [36]. Douzas et al. combined 262 k-means clustering and SMOTE, namely kmeans-SMOTE. 263 It detects secure clusters with non-overlapping classes 264

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across the entire data space by a high proportion of 265 minority samples to prevent noise generation [37]. As well, NI-MWMOTE not only utilizes aggregated hierarchical 267 clustering to prevent ignoring small minority sub-clusters but 268 also eliminates real noise through iteratively suspected noise 269 probabilities and misclassification errors [38]. Nevertheless, 270 DBSMOTE, A-SUWO, NI-MWMOTE, k-means SMOTE 271 require 3, 4, 6 and 9 parameters, respectively. More-272 over, region-emphasizing approaches and clustering-based 273 approaches cannot effectively detect and deal with suspicious 274 noises. 275

Several efforts focus on improving the current mainstream 276 sampling mechanisms. Geometric SMOTE (G-SMOTE) 277 synthesized new samples around geometric regions of the 278 input space as an enhancement to the current data generation 279 mechanism [39]. The SW framework performed weighted 280 sampling by calculating the chaos of the sample space 281 to handle imbalanced noisy datasets [40]. In conclusion, 282 current sampling algorithms continue to have deficiencies 283 when coping with imbalanced, noisy data sets. (1) Addi-284 tional hyperparameter optimisation restricts most methods. 285 (2) Most methods fail to detect suspicious noise effectively 286 and are prone to over-generalization. (3) Most of the current 287 sampling algorithms are based on the random linear sampling 288 mechanism of SMOTE, which is not only limited by its 289 blindness, but also the noise will exacerbates the performance 290 degradation resulting from its blindness. Therefore, this 291 paper proposes an adaptive and robust method for oriented 292 oversampling with spatial information to simultaneously 293 address the aforementioned issues. 294

III. PROPOSED METHOD 205

A. MOTIVATION 296

The oversampling algorithms that exist now are basically 297 improvements on the SMOTE algorithm. These improve-298 ments overcome some of the shortcomings of the SMOTE 299 algorithm though. There are still several drawbacks as 300 follows. (1). inability to fit the distribution characteristics 301 of the data set. (2). large fluctuations in the sampling 302 results since the selection of hyperparameters in the sampling 303 performance. (3). blindness of random linear oversampling 304 lead. (4). SMOTE and most of its variants are often 305 restricted to specific application scenarios or datasets, such 306 as high-dimensional datasets, large datasets or datasets with 307 a large number of noisy samples. Therefore, an adaptive 308 and robust method for oriented oversampling with spatial 309 information is proposed. The purpose is to initially fit the data 310 distribution characteristics by adaptive spatial partitioning 311 of dataset characteristics, and to quantify spatial informa-312 tion to guide reasonable neighborhood generalization and 313 sample synthesis path enhancement. The uncontrollability 314 associated with random linear interpolation is avoided. Few 315 of the sampling algorithms that have been proposed give 316 mathematical models. For the sake of algorithmic soundness, 317 we give the mathematical model and mathematical proof of 318 the algorithm. 319

B. THE OOSI METHOD

An adaptive and robust method (OOSI) for oriented oversam-321 pling with spatial information is proposed to fill those gaps. 322 As is depicted in Figure 1, the OOSI is divided into three 323 stages.

- Adaptive data space partitioning.
- Quantification of spatial information.
- Sampling with oriented information. •

TABLE 1. Notaions and definitions.

Notaions	Definitions
k(means)	the number of nearest neighbors
D	a data set
D_+	majority samples $\in D$
D_{-}	minority samples $\in D$
x_i	an sample
C_i	a cluster
D_{c+}	majority samples of a cluster
D_{c-}	minority samples of a cluster
Γ	a set of seed clusters $\in D$, referring to Eq.(6)
P	a condition referring to Def. (1)
Q	a condition referring to Def. (2)
ζ	the sparsity of a cluster, referring to Def. (3)
σ	the multi-class density information, referring to Def. (4)
Θ_C	synthesized numbers of a cluster, referring to Def. (5)
η	a seed sample, referring to Def. (6)

1) ADAPTIVE DATA SPACE PARTITIONING

The data space is divided adaptively according to the own 329 characteristics of the dataset to fit the data space distribution 330 characteristics initially. The initial spatial partitioning can 331 be achieved by clustering, rather than simply dividing the 332 data space into majority and minority classes. Any clustering 333 method can be used for this step, e.g. k-means, dbscan, 334 spectral clustering. Different distance metrics can also be 335 chosen. Furthermore, the number of clusters of specificity 336 is determined by the own characteristics of the dataset. The 337 number of adaptive clusters k for dataset specificity is defined 338 as following. 339

$$k = \log_2 \left\{ (|D_-| + |D_+|) * \frac{D_-}{D_+} \right\}$$
(1) 340

Therefore, the larger the dataset and the more unevenly 341 distributed the data are, the more spatial partitioning is 342 required to capture more detailed spatial information of 343 the data. Taking kmeans and Euclidean distance as an 344 example, the distance between two samples is $d(x_i, x_i)$. Then 345 define the sum of the distances between the sample and the 346 center of the cluster as the loss function. The loss function 347 W(C) is defined as following. 348

$$W(C) = \sum_{l=1}^{k} \sum_{C_i=l} ||x_i - \bar{x}_j||^2$$
(2) 349

where $\bar{x}_l = (\bar{x}_{1l}, \bar{x}_{2l}, \dots, \bar{x}_{ml})^{\mathrm{T}}$ is the mean or center of the *i*-th class, $n_l = \sum_{i=1}^n I(C(i) = l)$. I(C(i) = l) is an indicator 350 351



FIGURE 1. Three stages of oriented oversampling with spatial information.

function. The value of I is 1 or 0. *K* means is to solve the following optimization model.

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$$C^* = \arg\min_{C} W(C)$$

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$$= \arg\min_{C} \sum_{l=1}^{k} \sum_{C(i)=l} \|x_i - \bar{x}_l\|^2$$
(3)

When similar samples are clustered into the same cluster, the loss function gets the optimal solution. This is a combinatorial optimization problem. *n* samples are clustered into *k* clusters, and there are S(n, k) clustering results.

$$S(n,k) = \frac{1}{k!} \sum_{l=1}^{k} (-1)^{k-l} \binom{k}{l} k^{n}$$
(4)

In imbalanced data sets, the optimization model for clustering has some additional constraints. There are no overlapping regions for each cluster. In order to reduce the interference of outlier samples to clustering, the number of samples in each cluster is bigger than k. The final mathematical model is shown in Eq. (5).

$$\begin{array}{ll} & \underset{C_{1},C_{2}\cdots,C_{k}}{\min}\sum_{i=1}^{k}\sum_{x\in C_{i}}\|x-c_{i}\|^{2},\\ & \underset{C_{1}}{\text{s.t.}}\quad C_{1}\cup C_{2}\cup\cdots\cup C_{k}=\{x_{1},x_{2},\cdots,x_{n}\},\\ & \underset{C_{0}}{\text{s.t.}}\quad C_{1}\cup C_{2}\cup\cdots\cup C_{k}=\{x_{1},x_{2},\cdots,x_{n}\},\\ & \underset{C_{i}}{\text{s.t.}}\quad C_{i}\cap C_{j}=\varnothing, \quad \forall i\neq j,\\ & \underset{C_{i}}{\text{rows}}\quad |C|>k. \end{array}$$

371 2) QUANTIFICATION OF SPATIAL INFORMATION

To better quantify spatial information, after obtaining an adaptive and dataset-specific clustering space, a simple and effective optimization of the clustering space is necessary. If the imbalanced distribution of clusters (IR_C) has been mitigated or the number of minority class samples within

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clusters (D_{c-}) is insufficient to synthesize new samples, it will not be necessary or appropriate to synthesize new samples within these clusters. Therefore, the clustering space will be filtered to obtain seed clusters.

$$\Gamma = \{ C | IR_C > 0.5 * IR \text{ and } | D_{c-} | \ge k_{nn} | \}$$
(6) 38

The seed clusters will serve as the optimized clustering space and will synthesize new samples in the seed clusters. Therefore, the filtering conditions for seed clusters are two as follows.

Definition 1 (Condition P): The proportion of minority samples in a cluster should be greater than half of the imbalanced proportion(IR) of the original dataset. The imbalance ratio of a cluster is denoted by IR_C .

$$IR_C > 0.5 * IR$$
 (7) 390

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Definition 2 (Condition Q): The number of minority391samples (D_{c-}) in a cluster must be bigger than the number of392k nearest neighbor (k_{nn}) samples. In the stage of synthesizing393samples, it needs to be used to interpolate between the seed394sample and the neighbor samples. If there are too few samples395in the cluster, overlapping samples will be synthesized,396resulting in overfitting.397

$$|D_{c-}| \ge k_{nn} \tag{8} \quad 3$$

Eligible clusters are called seed clusters. In order to 399 effectively quantify and utilize spatial information, two 400 quantitative techniques are proposed within the optimized 401 clustering space. Specifically, to avoid overgeneralization 402 of region-emphasizing sample synthesis and intra-class 403 imbalance, the two quantitative techniques measure the 404 distributional characteristics of clusters in terms of spatial 405 sparsity and multi-class distributional information, respec-406 tively. Then the number of sample synthesis within clusters 407 are reasonably allocated. These two techniques are sparsity 408

and multi-class density information of the cluster. The 409 corresponding definitions and calculation method has been 410 given in the Def. (3) and Def. (4). 411

Definition 3 (Sparsity, ζ): Given a cluster C with center 412 x_c and the minority set D_{c-} with n_- samples and the majority 413 set D_{c+} with n_+ samples. $d(x_i, x_j)$ is the distance of any two 414 samples x_i and x_i . The radius r of cluster C is the average 415 of the deviations of all minority samples' distances to the 416 cluster center. The sparsity of a cluster (ζ) is the reciprocal of 417 the number of minority samples per unit area in the cluster, 418 as defined below. 419

 $r = \frac{\sum d(x_c, x_i)}{n_-}, x_i \in D_{c-}$

$$\zeta = \frac{\pi * r^2}{n_-} \tag{10}$$

(9)

Specifically, the space within a cluster is quantified as 422 the simulated area based on the mean of the intra-cluster 423 distance deviation, i.e., the radius. After that, the number of 424 minority classes in a given space, i.e., the minority density, 425 is quantized. Thus, intra-cluster sparsity based on spatial 426 sparsity quantifies the sparsity of minority classes per unit 427 of cluster space. The more minority classes per unit cluster 428 space, the smaller the value of intra-cluster sparsity (ζ). 429 The fewer the minority samples in the unit cluster space, 430 the larger the value of intra-cluster sparsity (ζ). Therefore, 431 intra-cluster sparsity (ζ) considers the difference in the 432 spatial sparsity sparsity of clusters and requires allocating 433 a reasonable number of samples for generalization. The 434 sparser the samples within a cluster, the more samples can be 435 allocated to generalize the space, and the denser the samples 436 within a cluster, the fewer samples can be allocated to avoid 437 overgeneralization or generation of overlapping samples with 438 low values. 439

Definition 4 (Multi-Class Density Information, ρ): Given 440 a cluster C with center x_c and the minority class c and the 441 majority class c+. The absolute density information within 442 a cluster, i.e., $\sigma(c)$, indicates how densely the samples of 443 a certain class are distributed within the cluster. The larger 444 the absolute density information within a cluster, the more 445 446 dense the distribution of such samples are. The multi-class density information, i.e., ρ , fully integrates the intra-class 447 and inter-class distribution information within a cluster, as 448 follows. 449

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$$\sigma(c.) = \frac{n_{-}}{\sum d(x_c, x_i)}, x_i \in D_{c.}$$
(11)

$$\rho = \frac{\sigma(c-)}{\sigma(c+)} = \frac{n_{-}/\sum d(x_c, x_i)(x_i \in D_{c-})}{n_{+}/\sum d(x_c, x_i)(x_i \in D_{c+})}$$
(12)

Specifically, according to Eq. 11, the absolute density 452 information is the number of class per unit distance from 453 the cluster center x_c to the given class. Thus for any given 454 cluster, the farther the cluster center x_c is from the unit 455 distance to the given class, the sparser the distribution of 456 the given class within the cluster; conversely, the denser 457 it is. Then, information about the spatial distribution of 458

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a given class within the cluster is quantized. In addition, 459 based on the ratio of the cluster center x_c to the multiple 460 classes of homogeneous and heterogeneous samples, the 461 difference distribution information within the cluster space 462 for multiple classes is quantified. The multi-class density 463 information of the cluster ρ is a composite measure of 464 the multi-class distribution information within the cluster 465 to synthesize more samples in clusters far from the dense 466 distribution of heterogeneous classes. By definition 4, 467 the larger the value of $\sigma(c-)/\sigma(c+)$, the relatively denser the 468 distribution of minority classes and the relatively sparser the 469 distribution of majority classes within the cluster. Therefore, 470 the larger the multi-class density information within a cluster 471 (ρ) indicates, the closer it is to the densely distributed 472 minority class and away from the densely distributed majority 473 class. 474

3) SAMPLING WITH ORIENTED INFORMATION

During the sampling process, on the one hand, most current 476 sampling algorithms emphasize synthesizing more samples 477 in specific regions or synthesizing the same samples in 478 distinct regions. It not only tends to lead to overgeneralization 479 in specific regions, but also suffers from sample general-480 ization blindness. Few sampling algorithms consider spatial 481 information to guide the oriented allocation of the number 482 of synthesized samples for different clusters. Therefore, after 483 obtaining the simple optimized clustering space and the 484 quantitative measures of cluster distribution characteristics, 485 the sampling number within minority clusters is assigned 486 reasonably to avoid overgeneralization of specific regions 487 and to alleviate both intra- and inter-class imbalances. The 488 number of synthesis per cluster with oriented information Θ_C 489 is defined as follows. 490

Definition 5 (Synthesized Number, Θ_C): Given a dataset 491 $D = D_+ \cup D_-$, in which the majority and minority samples 492 are D+ and D-, respectively. C_i represents one of the seed 493 clusters $(i = 1, ... |\Gamma|)$. The normalization of the sparsity 494 and multi-class density information of C_i are $norm(\zeta(C_i))$, 495 *norm*($\rho(C_i)$). The specific calculation formula for the number 496 of new samples of $Ci(\Theta_{C_i})$ is as following: 497

$$G(D) = |D_+| - |D_-| \tag{13}$$

$$\Theta_{C_i} = G(D) * \frac{\operatorname{norm}(\zeta(C_i)) * \operatorname{norm}(\rho(C_i))}{\sum_{1}^{|\Gamma|} \operatorname{norm}(\zeta(C_i)) * \operatorname{norm}(\rho(C_i))}$$
(14) ⁴⁹⁹

During the sampling process, on the other hand, most 500 current sampling algorithms either fail to detect and handle 501 noise efficiently or rely on noise filtering mechanisms that 502 require iteration and optimization. Not only do they suffer 503 from noise-induced performance deterioration, but most of 504 the current sampling algorithms are blind based on the smote 505 random sampling mechanism. Blind generalization of seed 506 samples and selection of nearest neighbors can extend the 507 performance deterioration caused by noise generalization. 508 Furthermore, the blind synthesis position between samples 509 tends to introduce more chaotic samples. Thus, OOSI not 510

only detects suspicious noise and prevents noise expansion 511 by avoiding the selection of noisy samples as seed samples 512 through neighborhood space information. The neighbor space 513 of a suspicious noise sample tends to be distributed with 514 more heterogeneous samples. It indicates that its neighbor 515 space has been invaded by majority classes, then it is prone 516 to synthesize new confusion samples or noise samples. Thus 517 according to Eq. 15, the set of non-noise seed samples is 518 obtained. Also, the oriented weights are assigned based on 519 the multi-class information level of the seed samples to guide 520 the generation path improvement of synthetic samples and 521 avoid generating additional chaotic samples. Thus, the seed 522 samples (η) and the synthetic new samples (s_{new}) are defined 523 as follows. 524

Definition 6 (Seed Samples, η): Given a cluster C_i , each sample $s \in C_i$ has minority neighbors D_{k-} and majority neighbors D_{k+} . The seed samples η of cluster C_i and their oriented weights $\omega(s)$ are defined exactly as following.

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$$\eta = \{s | |D_{k-}| > |D_{k+}| \}$$
 (15)

$$\omega(s) = \frac{\sigma(k-)}{\sigma(k+)} = \frac{|D_{k-}| / \sum d(s, s_j)(s_j \in D_{k-})}{|D_{k+}| / \sum d(s, s_j)(s_j \in D_{k+})}$$

⁵³¹ Definition 7 (New Samples, s_{new}): Given any two seed ⁵³² samples *ss* and *cs*, where $\omega(ss) > \omega(cs)$, the reasonable ⁵³³ synthesis of a new sample s_{new} with oriented weights is as ⁵³⁴ follows. ξ is the random number between [0, 1] to maintain ⁵³⁵ the randomness.

$$s_{new} = ss + (cs - ss) * \frac{\min(\omega(ss), \omega(cs))}{\omega(ss) + \omega(cs)} * \xi$$
(17)

Specifically, according to Eq. 16, Specifically, the 537 multi-class information level of the non-noise seed samples 538 are based on their k-neighborhoods, which portray their 539 local characteristics. According to Eq. 16, the multi-class 540 information level of a non-noise seed sample is determined 541 by calculating the ratio of the distances of the number of 542 classes per unit distance between the k homogeneous and 543 heterogeneous neighbors. The multi-class information level 544 of the non-noise seed samples integrates the multi-class 545 distribution information of the samples and fully reflects 546 the information of homogeneous and heterogeneous samples 547 within the neighborhoods in order to efficiently differentiate 548 and guide diverse sampling. Therefore, the larger the value of 549 $\omega(s)$, the closer the seed sample is to homogeneous samples, 550 the further it is from heterogeneous samples, and the safer it 551 is. 552

According to the multi-class information level of the seed 553 samples, it is reasonable toguide the synthetic synthesis 554 path improvement, which makes the new samples close to 555 the safe region and away from the chaotic region. As in 556 Figure 2 (a), ss is for any seed sample, and neighbors nn =557 $[n_1, n_2, n_3](k = 3)$ is its near neighbor sample. According 558 to the information of the distribution of homogeneous and 559 heterogeneous samples in the neighborhood, it is easy to 560 see the discrepancy that exists in different seed samples. 561 According to Eq. 16, the multi-class information level 562

between samples can be calculated i.e. $\omega(n_1) < \omega(n_2) < \omega(n_2)$ 563 $\omega(ss) < \omega(n_3)$. When synthesizing new samples, if based on 564 ss and n_1 , since $\omega(n_1) < \omega(ss)$, the safer sample at this time is 565 ss, the position of the synthesized sample is closer to the ss, 566 as shown in Figure 2 (b). if based on ss and n_3 , since $\omega(ss) < \infty$ 567 $\omega(n_3)$, the safer sample at this time is n_3 , the position of 568 the synthesized sample is closer to the n_3 . Therefore, the 569 multi-class information level of the non-noise seed samples 570 effectively guides the improvement of the synthetic sample 571 generation path, ensures the synthetic quality of the new 572 samples, and avoids the confusion introduced by blind 573 generalization. 574

Algorithm 1 The OOSI Algorithm.

Input: Imbalanced dataset $D=D_+\cup D_-$, $|D_-|$: the minority samples, $|D_+|$: the majority samples, $n=|D_-|+|D_+|$

Output: Balanced dataset D'.

- **//FIRST** : Adaptive data space partitioning.
- 1: Computing dataset specificity's adaptive clusters k according to Eq. 1.
- 2: Division space with the clustering strategy, $D \rightarrow S(n, k)$.
- 3: clustering(k)
- //SECOND: Quantification of spatial information.
 4: Initialize Γ = Ø
- 4. Initialize $I = \emptyset$
- 5: for C_i in S(n, k) do 6: if $IR_C > 0.5 * IR$ and $|D_{c-1}| \ge k_{nn}$ then
- 7: $\Gamma = \Gamma \cup C$
- 7: $\Gamma = \Gamma \cup C_i$ 8: Calculate sparsity ζ according to Def. (3).
- 9: Calculate multi-class density information ρ according to Def. (4).
- 10: end if

11: end for

(16)

- //Third Sampling with oriented information.
- 12: Initialize $D_{new} = \emptyset$
- 13: for C_i in Γ do

14: Calculate Θ_{C_i} by Eq. (14)

- 15: **for** s in C_i **do**
- 16: **if** s is η judge by Eq. (15) **then**
- 17: Select nearest neighbor sample of s_i ;
- 18: Synthesize a new sample s_{new} between *s* and neighbours;
- 19: $D_{new} = D_{new} \cup s_{new};$
- 20: end if

21:

22: end for 23: end for

24: $D' = D_+ \cup D_- \cup D_{new}$

25: **Return** Balanced dataset D'.

C. TIME COMPLEXITY ANALYSIS

The time complexity of the proposed method is deter-576 mined by three main parts: adaptive data space partition-577 ing, quantification of spatial information and sampling with 578 oriented information. Given a dataset D containing N samples 579 and *n* minority samples. For adaptively partitioning data 580 space with specificity k, The time complexity of the kmeans 581 clustering is O(k * t * N), where t is the constant number 582 of iterations. For quantifying spatial information, the time 583 complexity of computing the cluster sparsity and multi-class 584 density information are less than O(k * n). For sampling with 585 oriented information, The time complexity of distributing the 586 number of synthetic samples within a cluster and synthesizing 587 new samples is no greater than O(k) and O(n*n), respectively. 588 Therefore, the overall time complexity of the proposed 589 method is $O(k * t * N + n^2)$. 590

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FIGURE 2. Schematic diagram of the synthesized new samples. (a) Original data distribution, (b) Location of sample synthesis.

591 IV. EXPERIMENTS

592 A. EXPERIMENTAL DATASETS

In order to evaluate the effectiveness of the proposed method, 593 11 real-world application datasets are obtained from the 594 UCI and KEEL dataset repositories [41]. Moreover, the 595 one versus others data processing strategy is employed to 596 restructure the imbalanced multi-class datasets into binary 597 classes. The specific information of all datasets is shown in 598 Table 2. Among them, Minority, Majority, Features, and IR 599 denote the number of minority class samples, the number 600 of majority class samples, the number of attributes, and 601 the imbalance ratio. The imbalance ratio equals Majority 602 divided by Minority. In order to effectively evaluate the 603 performance and stability of the method, hierarchical ten-fold 604 cross-validation is used for data division to maintain the 605 consistency of the distribution characteristics and imbalance 606 ratio of each class. Furthermore, to validate the robustness 607 of the proposed method, the dataset is manually added with 608 varying levels of flip noise. Specifically, the same number 609 of samples (n * nl) from minority and majority classes 610 are randomly flipped into heterogeneous classes, where n 611 is the number of minority class and *nl* is the noise level 612 $(0\% \le nl \le 20\%).$ 613

614 **B. EVALUATION METRICS**

Frequently, the proportion of positive (minority) and negative 615 (majority) samples is disproportionate in practical applica-616 tions. Currently, traditional classification evaluation metrics 617 such as accuracy rate and error rate may be misleading and 618 cannot effectively reflect the model's true performance. Since 619 these metrics are more biased toward the predictions of the 620 majority classes, they are insensitive to the prediction errors 621 of the minority classes [42]. Therefore, specific evaluation 622 metrics for imbalanced datasets, such as F-measure, G-mean, 623 and AUC, are required [43]. 624

The F-measure is the harmonic mean of precision and recall, which can reflect the model's predictive ability for

TABLE 2. The specific information of all datasets.

Datasets	Samples	Features	Majority	Minority	IR
ecoli	336	7	284	52	5.46
haberman	306	3	225	81	2.78
creditApproval	459	15	383	76	5.04
wisconsin	488	9	444	44	10.09
breastcancer	532	10	444	88	5.05
pima	768	8	500	268	1.87
segment	2310	16	1980	330	6.00
mushrooms	4628	112	4208	420	10.02
page-blocks0	5472	10	4913	559	8.79
svmguide1	4400	4	4000	400	10.00
magic	13565	10	12332	1233	10.00

the minority class. The precision refers to the proportion of
truly positive samples in the predicted positive examples, and
the recall refers to the proportion of truly positive samples
predicted to be positive. The higher the F-measure value, the
better the model can correctly classify the positive samples.629
630The calculation of F-measure is as formula (18).631

$$F-\text{measure} = \frac{2 * \text{Recall} * \text{Precision}}{\text{Recall} + \text{Precision}}, \quad (18) \quad {}_{633}$$

The G-mean is the geometric mean of sensitivity (recall) 634 and specificity, reflecting the model's predictive performance 635 for positive and negative samples. Specificity refers to the 636 proportion of truly negative samples predicted to be negative. 637 The calculation method of the G-mean considers the true 638 class rate and the true negative class rate. Therefore, the 639 higher the G-mean, the more balanced the model's ability 640 to identify positive and negative samples. The calculation of 641 G-mean is as formula (19). 642

$$G-mean = \sqrt{Sensitivity * Specificity}.$$
 (19) 643

The AUC is the area under the ROC curve, which can reflect the ability of the model to distinguish positive and negative examples under different thresholds. Among them, 646



FIGURE 3. The average results of five classifiers on 11 real-world datasets for method comparison with varying noise levels (0% ≤ nl ≤ 20%).

the ROC curve is a curve with the false positive rate 647 as the horizontal axis and the true positive rate as the 648 vertical axis. The larger the AUC value, the better the 649 classification performance of the model for different classes. 650 The calculation of AUC is as formula (20). 651

$$AUC = \frac{\text{Sensitivity} + \text{Specificity}}{2}.$$
 (20)

C. COMPARATIVE OVERSAMPLING METHODS 653

To demonstrate the superiority of the proposed method, 654 11 related oversampling methods with distinct strategies 655 are compared, and sample synthesis is conducted on 656 twelve real-world application datasets. SMOTE-TomekLinks 657 (S.-TkL) [13], SMOTE-IPF (S.-IPF) [24], and SMOTE-658 FRST-2T (S.-FRST) [25] are noise-filtering techniques. 659 ADASYN [30], MWMOTE [27], and Adaptive-SMOTE 660 (AdaptS.) [33] are region-emphasizing approaches. 661 DBSMOTE [35], kmeans-SMOTE (means-S.) [37], and 662 RSMOTE [34] are competitive clustering-based methods. 663 Geometric SMOTE (G-SMOTE) [39] and SMOTE-SW 664 (S.-SW) [40] are enhanced sampling mechanisms. The core 665 idea of their algorithm has been presented in Section II. 666 All sampling methods are provided with concrete imple-667 mentations by the SMOTE-variant library [44] or respective 668 authors. To verify the general validity and stability of the proposed method, five mainstream classifiers were used to 670 evaluate the classification performance, including logistic 671 regression (LR), support vector machine (SVM), adaptive 672 boosting (AdaBoost), Gradient Boosted Decision Trees 673 (GBDT), and Backpropagation Neural Networks (BPNN). 674

D. COMPARATIVE EXPERIMENTS ON REAL DATASETS

To verify the superiority of the proposed method when coping 676 with imbalanced and noisy datasets, 11 sampling methods 677 with distinct strategies are compared on five classifiers 678 and 11 real-world datasets. These datasets involve different 679 samples, features, and imbalance ratios to comprehensively 680 evaluate the performance of different methods under various 681 data distributions. Furthermore, to demonstrate the robust-682 ness of the proposed method, different levels of flip noise are 683 randomly introduced into each experimental datasets ($nl \in$ 684 $\{0\%, 5\%, 10\%, 15\%, 20\%\}$).

The average results of method comparisons averaged over 5 classifiers and 11 datasets are shown in Figure 3. Each subplot in Figure 3 depicts the variation trend of the ten methods with increasing noise level for a particular metric. The solid red line with a five-pointed star represent the proposed method OOSI. Each color represents a comparative algorithm for a group of strategies.

In general, the solid red line with a five-pointed star 693 is always above other lines for all metrics, noise levels, 694 and methods. It demonstrates that OOSI consistently out-695 performs its competitors, regardless of the metrics and 696 noise levels. It is common knowledge that the presence 697 of noise impairs decision-making, leading to performance 698 degradation. When noise is present, i.e., at 5% noise 699 level, the performance of other lines (comparison method) 700 decreases significantly, particularly for ADASYN. However, 701 there is a slight decrease in OOSI performance and a 702 larger performance improvement in OOSI compared to 703 Noiseless. Notably, as the level of noise increases, OOSI 704 achieves greater enhancement than most contrasting methods, 705 particularly filtering-based methods, and region-emphasizing 706

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TABLE 3. Mean and variance of 12 oversampling methods under 5 classifiers on each real-world dataset (nl = 0%).

Metrics	Datasets	STkL	SIPF	SFRST	ADASYN	MWMOTE	AdaptS.	DBSMOTE	means-S.	RSMOTE	SG	SSW	OOSI
	ecoli	0.937±0.03	0.945±0.02	0.942±0.02	0.898±0.04	0.937±0.03	0.942±0.02	0.961±0.02	0.965±0.02	0.947±0.02	0.933±0.03	0.944±0.03	0.963±0.02
	haberman	0.687±0.07	0.693±0.08	0.721±0.07	0.638±0.08	0.693±0.08	0.823 ± 0.04	0.685±0.06	0.725±0.06	0.682±0.06	0.653±0.07	0.637±0.09	0.785±0.07
	creditApproval	0.909±0.03	0.908±0.03	0.937±0.01	0.889±0.03	0.915±0.03	0.924±0.03	0.922±0.02	0.914±0.03	0.931±0.02	0.898±0.03	0.917±0.03	0.938±0.03
	wisconsin	0.988 ± 0.01	0.988 ± 0.01	0.994±0.01	0.990 ± 0.01	0.990±0.01	0.987±0.01	0.988 ± 0.01	0.985 ± 0.01	0.971±0.01	0.985 ± 0.01	0.992 ± 0.01	0.989 ± 0.01
	breastcancer	0.979±0.01	0.980 ± 0.01	0.990±0.01	0.979±0.01	0.978±0.01	0.985±0.01	0.981±0.01	0.983±0.01	0.969 ± 0.02	0.977±0.01	0.992±0.01	0.981±0.01
	pima	0.795±0.04	0.782±0.04	0.838 ± 0.02	0.755±0.03	0.785±0.03	0.787±0.04	0.802±0.02	0.748±0.04	0.775±0.04	0.753±0.04	0.818 ± 0.04	0.806±0.04
F1-measure	segment	0.947±0.01	0.949±0.01	0.947±0.01	0.938±0.01	0.948±0.01	0.957±0.01	0.948±0.01	0.959 ± 0.01	0.952±0.01	0.939±0.01	0.952±0.01	0.960±0.01
	svmguide1	0.975±0.01	0.974±0.01	0.973±0.01	0.960±0.01	0.968±0.00	0.975±0.00	0.977±0.00	0.980 ± 0.00	0.984±0.00	0.960±0.01	0.974±0.00	0.986±0.00
	mushrooms	1.000 ± 0.00	1.000 ± 0.00	1.000 ± 0.00	1.000 ± 0.00	1.000 ± 0.00	1.000 ± 0.00	0.996±0.00	1.000 ± 0.00	1.000 ± 0.00	0.999 ± 0.00	1.000 ± 0.00	1.000±0.00
	page-blocks0	0.935±0.01	0.933±0.01	0.930±0.01	0.914±0.01	0.934±0.01	0.930±0.01	0.947±0.01	0.956±0.01	0.960±0.01	0.930±0.01	0.941±0.01	0.972±0.00
	magic	0.834±0.01	0.834±0.01	0.881±0.00	0.792±0.01	0.856±0.01	0.900±0.01	0.887±0.00	0.928±0.00	0.943±0.00	0.832±0.01	0.813±0.01	0.965±0.00
	Average	0.908±0.02	0.908±0.02	0.923±0.02	0.887±0.02	0.909±0.02	0.928±0.02	0.918±0.02	0.922±0.02	0.919±0.02	0.896 ± 0.02	0.907±0.02	0.940±0.02
	Win-Lose	0-11	0-11	3-8	1 - 10	1 - 10	2-9	0-11	2-9	0-11	0-11	3-8	N/A
	ecoli	0.971±0.02	0.974±0.02	0.973±0.01	0.945±0.03	0.971±0.02	0.975±0.02	0.981±0.02	0.979 ± 0.02	0.976±0.02	0.966 ± 0.02	0.969 ± 0.02	0.988±0.01
	haberman	0.796±0.05	0.786±0.07	0.768±0.08	0.735±0.07	0.781±0.06	0.828±0.05	0.776±0.05	0.812±0.05	0.778±0.06	0.734±0.07	0.758±0.07	0.860±0.05
	creditApproval	0.953±0.02	0.953±0.02	0.963±0.02	0.945±0.02	0.962±0.02	0.968±0.02	0.973±0.02	0.958±0.02	0.974±0.02	0.946±0.02	0.965±0.02	0.973±0.02
	wisconsin	0.997±0.00	0.997±0.00	0.997±0.00	0.997±0.01	0.997±0.00	0.997±0.00	0.998±0.00	0.997±0.00	0.981±0.01	0.996±0.00	0.999±0.00	0.999±0.00
	breastcancer	0.995±0.01	0.996±0.01	0.998±0.00	0.993±0.01	0.996±0.01	0.996±0.00	0.997±0.00	0.994±0.01	0.985±0.01	0.994±0.01	0.999±0.00	0.998±0.00
	pima	0.872±0.03	0.867±0.03	0.873±0.03	0.835±0.03	0.858±0.03	0.864±0.03	0.873±0.02	0.831±0.04	0.863±0.03	0.845±0.03	0.911±0.03	0.886±0.03
AUC	segment	0.978±0.01	0.980±0.00	0.978±0.00	0.969±0.01	0.977±0.01	0.985±0.00	0.982±0.01	0.988±0.00	0.988±0.00	0.976±0.01	0.981±0.00	0.989±0.00
	svmguide1	0.996±0.00	0.996±0.00	0.996±0.00	0.991±0.00	0.995±0.00	0.996±0.00	0.997±0.00	0.997±0.00	0.999±0.00	0.992±0.00	0.996±0.00	0.998±0.00
	mushrooms	1.000 ± 0.00	1.000 ± 0.00	1.000 ± 0.00	1.000 ± 0.00	1.000±0.00	1.000 ± 0.00	1.000±0.00	1.000 ± 0.00	1.000 ± 0.00	1.000 ± 0.00	1.000 ± 0.00	1.000±0.00
	page-blocks0	0.976±0.00	0.975±0.00	0.972±0.00	0.957±0.01	0.975±0.00	0.974 ± 0.00	0.979±0.00	0.989 ± 0.00	0.990±0.00	0.972 ± 0.00	0.979±0.00	0.992±0.00
	magic	0.914±0.00	0.914±0.00	0.914±0.00	0.876±0.00	0.932±0.00	0.956±0.00	0.942±0.00	0.974±0.00	0.981±0.00	0.910±0.00	0.898 ± 0.00	0.988±0.00
	Average	0.950±0.01	0.949±0.01	0.948 ± 0.01	0.931±0.01	0.949±0.01	0.958±0.01	0.954±0.01	0.956 ± 0.01	0.956±0.02	0.939 ± 0.01	0.956±0.01	0.970±0.01
	Win-Lose	0-11	0-11	0-11	0-11	0-11	0-11	0-11	0-11	2-9	0-11	2–9	N/A
	ecoli	0.935±0.03	0.943±0.03	0.940 ± 0.02	0.897±0.04	0.935±0.03	0.932±0.03	0.959±0.02	0.964±0.02	0.947±0.02	0.930±0.03	0.944±0.02	0.962±0.02
	haberman	0.706±0.06	0.716±0.07	0.687±0.08	0.646 ± 0.08	0.713±0.07	0.699 ± 0.06	0.678±0.08	0.739±0.05	0.698±0.06	0.675±0.06	0.666 ± 0.08	0.796±0.06
	creditApproval	0.902±0.03	0.899±0.03	0.900 ± 0.02	0.882±0.03	0.908±0.03	0.910±0.03	0.919±0.02	0.905±0.03	0.929±0.03	0.890 ± 0.04	0.910±0.03	0.938±0.03
	wisconsin	0.988±0.01	0.988 ± 0.01	0.991±0.01	0.990±0.01	0.989±0.01	0.985±0.01	0.988±0.01	0.984 ± 0.01	0.970 ± 0.01	0.985±0.01	0.992±0.01	0.988±0.01
	breastcancer	0.979±0.01	0.979 ± 0.01	0.985 ± 0.01	0.979 ± 0.01	0.978 ± 0.01	0.982 ± 0.01	0.981±0.01	0.983 ± 0.01	0.968±0.02	0.977 ± 0.01	0.992 ± 0.01	0.981±0.01
	pima	0.794±0.04	0.782±0.04	0.777±0.04	0.752±0.03	0.780±0.03	0.783±0.03	0.799±0.02	0.742±0.04	0.773±0.04	0.752±0.04	0.820 ± 0.04	0.810±0.04
G-mean	segment	0.942±0.01	0.946 ± 0.01	0.943±0.01	0.933±0.01	0.943±0.01	0.949 ± 0.01	0.944±0.01	0.957±0.01	0.951±0.01	0.934±0.01	0.949 ± 0.01	0.959±0.01
	svmguide1	0.974±0.01	0.973±0.01	0.973±0.01	0.959 ± 0.01	0.967±0.00	0.972±0.00	0.976±0.01	0.980 ± 0.01	0.984±0.00	0.959 ± 0.01	0.974±0.00	0.986±0.00
	mushrooms	1.000±0.00	1.000 ± 0.00	0.996±0.00	1.000 ± 0.00	1.000 ± 0.00	0.999±0.00	1.000 ± 0.00	1.000 ± 0.00				
	page-blocks0	0.936±0.01	0.934±0.01	0.931±0.01	0.914 ± 0.01	0.934±0.01	0.930±0.01	0.947±0.01	0.957±0.01	0.960 ± 0.01	0.932 ± 0.01	0.942 ± 0.01	0.972±0.00
	magic	0.839 ± 0.01	0.839 ± 0.01	0.818 ± 0.01	0.796 ± 0.01	0.859 ± 0.01	0.896 ± 0.01	0.886 ± 0.00	0.929 ± 0.00	0.944±0.00	0.837±0.01	0.819 ± 0.01	0.965 ± 0.00
	Average	0.909 ± 0.02	0.909 ± 0.02	0.904 ± 0.02	0.886 ± 0.02	0.910±0.02	0.913±0.02	0.916±0.02	0.922±0.02	0.920 ± 0.02	0.897±0.02	0.910 ± 0.02	0.942±0.02
	Win-Lose	0-11	0-11	2–9	1 - 10	1 - 10	1 - 10	0-11	2–9	0-11	0-11	3-8	N/A

TABLE 4. Mean and variance of 12 oversampling methods under 5 classifiers on each real-world dataset (nl = 10%).

Metrics	Datasets	STkL	SIPF	SFRST	ADASYN	MWMOTE	AdaptS.	DBSMOTE	means-S.	RSMOTE	SG	SSW	OOSI
	ecoli	0.770±0.05	0.751±0.06	0.771±0.06	0.727±0.07	0.782±0.06	0.874±0.03	0.822±0.05	0.828±0.04	0.856±0.04	0.776±0.05	0.802±0.05	0.912±0.03
	haberman	0.626±0.08	0.604±0.07	0.708±0.05	0.616±0.07	0.626±0.06	0.784±0.05	0.672±0.06	0.707±0.07	0.636±0.10	0.624±0.06	0.642±0.07	0.755±0.05
	creditApproval	0.827±0.04	0.807 ± 0.04	0.848±0.03	0.767±0.05	0.828±0.03	0.884±0.03	0.836±0.04	0.805±0.03	0.862 ± 0.04	0.799 ± 0.04	0.781±0.04	0.877±0.03
	wisconsin	0.767±0.04	0.765±0.05	0.803±0.03	0.704±0.05	0.814±0.04	0.888±0.03	0.670±0.06	0.884±0.03	0.894±0.03	0.767±0.05	0.722±0.05	0.939±0.03
	breastcancer	0.822±0.04	0.814 ± 0.04	0.787±0.03	0.736±0.06	0.836±0.05	0.918±0.02	0.720 ± 0.05	0.927±0.02	0.899±0.03	0.852±0.04	0.825 ± 0.04	0.935±0.03
	pima	0.750±0.04	0.735±0.05	0.720±0.03	0.711±0.03	0.745±0.04	0.776±0.03	0.747±0.04	0.736±0.04	0.748±0.04	0.707±0.04	0.767±0.05	0.780±0.03
F1-measure	segment	0.795±0.02	0.789±0.02	0.790±0.02	0.649±0.02	0.809±0.02	0.870±0.01	0.826±0.02	0.752±0.02	0.874±0.02	0.800 ± 0.02	0.747±0.03	0.896 ± 0.01
	svmguide1	0.716±0.02	0.700 ± 0.02	0.696 ± 0.02	0.558±0.02	0.667±0.02	0.731±0.01	0.703±0.02	0.771±0.02	0.905±0.01	0.675±0.02	0.680 ± 0.02	0.927±0.01
	mushrooms	0.844 ± 0.01	0.851±0.01	0.855 ± 0.01	0.835±0.01	0.892±0.01	0.940 ± 0.01	0.656±0.05	0.919 ± 0.01	0.950 ± 0.01	0.901±0.01	0.821±0.01	0.945±0.01
	page-blocks0	0.753±0.02	0.741±0.02	0.773±0.01	0.653±0.02	0.760±0.02	0.831±0.01	0.711±0.01	0.852±0.01	0.893±0.01	0.772±0.01	0.721±0.02	0.923±0.01
	magic	0.630 ± 0.01	0.629 ± 0.01	0.778±0.00	0.583±0.01	0.717±0.01	0.802±0.01	0.681±0.01	0.872±0.01	0.871±0.01	0.659±0.01	0.592±0.01	0.914±0.01
	Average	0.755±0.03	0.744±0.03	0.775±0.03	0.685±0.04	0.771±0.03	0.845±0.02	0.731±0.04	0.823±0.03	0.853±0.03	0.757±0.03	0.736±0.04	0.891±0.02
	Win-Lose	0-11	0-11	0-11	0-11	0-11	2-9	0-11	0-11	1-10	0-11	0-11	N/A
	ecoli	0.867±0.04	0.857±0.04	0.876 ± 0.04	0.808±0.05	0.879±0.03	0.919±0.03	0.906±0.04	0.871±0.04	0.922±0.04	0.860 ± 0.05	0.896 ± 0.04	0.952±0.02
	haberman	0.726±0.07	0.712±0.05	0.695±0.09	0.700±0.06	0.703±0.06	0.770±0.06	0.739±0.06	0.794±0.06	0.720±0.09	0.687±0.06	0.720±0.08	0.824±0.05
	creditApproval	0.899±0.03	0.881±0.03	0.885±0.03	0.860 ± 0.04	0.892±0.02	0.922±0.03	0.889±0.04	0.876±0.03	0.919±0.03	0.853±0.04	0.861±0.04	0.925±0.03
	wisconsin	0.857±0.04	0.865±0.03	0.862±0.03	0.816±0.04	0.887±0.03	0.931±0.03	0.751±0.05	0.929±0.03	0.917±0.03	0.853±0.04	0.838±0.04	0.948±0.03
	breastcancer	0.896±0.03	0.895±0.03	0.853±0.03	0.850±0.04	0.912±0.03	0.947±0.02	0.793±0.04	0.945±0.02	0.932±0.02	0.898 ± 0.04	0.892±0.03	0.953±0.03
	pima	0.810±0.04	0.798±0.05	0.794±0.04	0.776±0.03	0.816±0.04	0.820±0.03	0.822±0.04	0.812±0.04	0.814±0.04	0.790±0.04	0.839±0.04	0.859±0.03
AUC	segment	0.863±0.02	0.859±0.02	0.852±0.02	0.739±0.02	0.874±0.02	0.910±0.01	0.887±0.01	0.809±0.02	0.928±0.01	0.863±0.02	0.830±0.02	0.937±0.01
	svmguide1	0.803±0.02	0.789±0.01	0.788±0.01	0.683±0.02	0.773±0.01	0.794±0.01	0.799±0.02	0.834±0.02	0.939±0.01	0.768±0.02	0.782±0.01	0.950±0.01
	mushrooms	0.924±0.01	0.930±0.01	0.923±0.01	0.897±0.01	0.940 ± 0.01	0.953±0.01	0.768±0.03	0.951±0.01	0.957±0.01	0.929 ± 0.01	0.914±0.01	0.953±0.01
	page-blocks0	0.829±0.01	0.822±0.01	0.808 ± 0.01	0.749±0.02	0.844±0.01	0.884 ± 0.01	0.817±0.01	0.920±0.01	0.936±0.01	0.845±0.01	0.808±0.01	0.949±0.01
	magic	0.738±0.01	0.737±0.01	0.735±0.01	0.684±0.01	0.809±0.01	0.866±0.01	0.736±0.01	0.925±0.01	0.920±0.01	0.759±0.01	0.704±0.01	0.943±0.01
	Average	0.837±0.03	0.831±0.03	0.825±0.03	0.778±0.03	0.848±0.02	0.883±0.02	0.810±0.03	0.879±0.03	0.9±0.03	0.828±0.03	0.826±0.03	0.927±0.02
	Win-Lose	0-11	0-11	0-11	0-11	0-11	0-11	0-11	0-11	1-10	0-11	0-11	N/A
	ecoli	0.779±0.05	0.760±0.05	0.779±0.06	0.716±0.07	0.788±0.05	0.837±0.05	0.825±0.04	0.821±0.04	0.859±0.04	0.788±0.05	0.811±0.05	0.911±0.03
	haberman	0.645±0.07	0.634±0.06	0.588±0.09	0.635±0.06	0.641±0.06	0.652±0.08	0.670±0.06	0.720 ± 0.06	0.654±0.09	0.634±0.05	0.651±0.06	0.770±0.04
	creditApproval	0.826±0.04	0.808±0.04	0.809±0.04	0.777±0.05	0.826±0.03	0.864±0.04	0.826±0.04	0.802±0.03	0.858±0.04	0.800±0.03	0.780±0.04	0.877±0.03
	wisconsin	0.790±0.03	0.790 ± 0.04	0.785±0.03	0.740±0.04	0.827±0.04	0.888±0.03	0.681±0.05	0.890±0.03	0.894±0.03	0.788±0.04	0.753±0.04	0.940±0.02
	breastcancer	0.835±0.04	0.827±0.03	0.755±0.04	0.760±0.05	0.845±0.04	0.915±0.03	0.721±0.05	0.928±0.02	0.901±0.03	0.861±0.03	0.837±0.03	0.936±0.03
	pima	0.742±0.05	0.730±0.05	0.718±0.03	0.705±0.04	0.741±0.04	0.750±0.03	0.747±0.04	0.734±0.04	0.743±0.04	0.712±0.04	0.768±0.04	0.780±0.03
G-mean	segment	0.799±0.02	0.794±0.02	0.794±0.02	0.667±0.02	0.811±0.02	0.845±0.02	0.827±0.02	0.747±0.02	0.876±0.02	0.807±0.02	0.759±0.02	0.896±0.01
	svmguide1	0.737±0.02	0.725±0.01	0.717±0.01	0.603±0.02	0.692±0.02	0.717±0.01	0.724±0.02	0.775±0.02	0.908±0.01	0.703±0.02	0.707±0.01	0.929±0.01
	mushrooms	0.856±0.01	0.862±0.01	0.861±0.01	0.844±0.01	0.899±0.01	0.941±0.01	0.715±0.04	0.922±0.01	0.952±0.01	0.907±0.01	0.836±0.01	0.946±0.01
	page-blocks0	0.773±0.01	0.764±0.01	0.719 ± 0.01	0.689 ± 0.02	0.777±0.01	0.822±0.01	0.738±0.01	0.859 ± 0.01	0.897±0.01	0.792±0.01	0.749 ± 0.01	0.925±0.01
	magic	0.665 ± 0.01	0.664 ± 0.01	0.527 ± 0.01	0.619 ± 0.01	0.732±0.01	0.795 ± 0.01	0.672 ± 0.01	0.877±0.01	0.878 ± 0.01	0.692 ± 0.01	0.633 ± 0.01	0.917±0.00
	Average	0.768±0.03	0.760±0.03	0.732±0.03	0.705±0.03	0.780±0.03	0.821±0.03	0.741±0.03	0.825±0.03	0.856±0.03	0.771±0.03	0.753±0.03	0.893±0.02
	Win-Lose	0-11	0-11	0-11	0-11	0-11	0-11	0-11	0-11	1-10	0-11	0-11	N/A

methods. One explanation for this could be that OOSI fully
 mines the data space information and adaptively obtains

a specific clustering space with the characteristics of the dataset. Additionally, reasonable sample generalization is 710

Metrics Datasets STRL SPRST ADASYN MWMOTE Adaps DBSMOTE means-St RSMOTE SG SW OOSI laberman 0.6844007 0.6644007 0.6644007 0.6924007 0.8274006 0.759406 0.579406 0.7264007 0.578406 0.579406 0.7264007 0.578406 0.579406 0.7264007 0.578406 0.579406 0.7264007 0.578406 0.579406 0.7264007 0.7264007 0.578406 0.578406 0.578406 0.578406 0.578406 0.578406 0.578406 0.578406 0.578406 0.578406 0.578406 0.578406 0.578406 0.578406 0.578406 0.578406 0.578406 0.578406														
end 0.664±007 0.664±007 0.664±007 0.692±007 0.729±006 0.759±006 0.759±006 0.697±008 6.691±007 0.693±008 0.664±005 0.759±005 0.697±008 6.691±007 0.873±008 6.691±007 0.873±008 6.691±007 0.873±008 0.691±007 0.873±008 0.691±007 0.873±008 0.691±007 0.873±007 0.87	Metrics	Datasets	STkL	SIPF	SFRST	ADASYN	MWMOTE	AdaptS.	DBSMOTE	means-S.	RSMOTE	SG	SSW	OOSI
haberma 0.5342.00 0.5482.00 0.5722.00 0.6032.00 0.6032.00 0.5032.00 0.5302.00 0.5320.00		ecoli	0.684±0.07	0.666±0.07	0.684±0.07	0.664±0.07	0.692±0.07	0.827±0.03	0.729±0.06	0.765±0.05	0.759±0.06	0.697±0.06	0.711±0.06	0.837±0.06
reditApproval 0.693±0.05 0.679±0.05 0.794±0.05 0.794±0.04 0.735±0.04 0.713±0.06 0.724±0.04 0.874±0.04 risconsin 0.735±0.05 0.658±0.06 0.774±0.04 0.612±0.05 0.744±0.04 0.612±0.05 0.744±0.04 0.698±0.01 0.875±0.01 0.752±0.04 0.752±0.04 0.752±0.04 0.752±0.04 0.752±0.04 0.752±0.04 0.752±0.04 0.752±0.04 0.752±0.05 0.865±0.01 0.878±0.01 0.752±0.04 <td>haberman</td> <td>0.583±0.08</td> <td>0.548±0.08</td> <td>0.702±0.04</td> <td>0.528±0.10</td> <td>0.603±0.08</td> <td>0.666±0.05</td> <td>0.599±0.09</td> <td>0.643±0.08</td> <td>0.562±0.09</td> <td>0.530±0.08</td> <td>0.630±0.08</td> <td>0.691±0.07</td>		haberman	0.583±0.08	0.548±0.08	0.702±0.04	0.528±0.10	0.603±0.08	0.666±0.05	0.599±0.09	0.643±0.08	0.562±0.09	0.530±0.08	0.630±0.08	0.691±0.07
wisconsin0.60240050.605420000.79140.000.60340.000.60940.000.80340.000.8940.000.73640.000.7564.0000.8754.0000.86754.0030.8754.0010.8754.003 <th< td=""><td></td><td>creditApproval</td><td>0.693±0.05</td><td>0.687±0.06</td><td>0.799±0.03</td><td>0.686±0.06</td><td>0.736±0.04</td><td>0.846±0.03</td><td>0.768±0.05</td><td>0.696±0.06</td><td>0.765±0.04</td><td>0.713±0.06</td><td>0.723±0.05</td><td>0.801±0.04</td></th<>		creditApproval	0.693±0.05	0.687±0.06	0.799±0.03	0.686±0.06	0.736±0.04	0.846±0.03	0.768±0.05	0.696±0.06	0.765±0.04	0.713±0.06	0.723±0.05	0.801±0.04
breastcancer 0.7334.005 0.6744.00.0 0.6124.005 0.7544.00.0 0.8784.003 0.5994.00 0.8519.04 0.7524.00.0 0.7224.00.0 0.7224.00.0 0.7224.00.0 0.7224.00.0 0.7224.00.0 0.6724.00.0 0.6934.00.0 0.6934.00.0 0.6734.00.0 0.6724.00.0 0.7224.00.0 0.6724.00.0 0.6724.00.0 0.6724.00.0 0.6724.00.0 0.6724.00.0 0.6724.00.0 0.6724.00.0 0.6724.00.0 0.6724.00.0 0.6724.00.0 0.6724.00.0 0.6724.00.0 0.6724.00.0 0.6724.00.0 0.6724.00.0 0.7244.00.0 0.8734.00.0 0.7244.00.0 0.8734.00.0 0.7244.00.0 0.8734.00.0 0.7244.00.0 0.7244.00.0 0.7244.00.0 0.7244.00.0 0.7244.00.0 0.7244.00.0 0.7244.00.0 0.7244.00.0 0.7244.00.0 0.7244.00.0 0.7244.00.0 0.7244.00.0 0.7244.00.0 0.7744.00.0 0.7744.00.0 0.7744.00.0 0.7744.00.0 0.7744.00.0 0.7744.00.0 0.7744.00.0 0.7744.00.0 0.7744.00.0 0.7744.00.0 0.7744.00.0 0.7744.00.0 0.7744.00.0 0.7744.00.0 0.7744.00.0 0.7744.00.0 <th< td=""><td></td><td>wisconsin</td><td>0.620±0.05</td><td>0.685±0.06</td><td>0.791±0.02</td><td>0.630±0.06</td><td>0.699±0.06</td><td>0.850±0.03</td><td>0.612±0.05</td><td>0.844±0.04</td><td>0.786±0.05</td><td>0.615±0.06</td><td>0.598±0.07</td><td>0.867±0.03</td></th<>		wisconsin	0.620±0.05	0.685±0.06	0.791±0.02	0.630±0.06	0.699±0.06	0.850±0.03	0.612±0.05	0.844±0.04	0.786±0.05	0.615±0.06	0.598±0.07	0.867±0.03
F1-measure main 0.6754:003 0.6641:003 0.6641:003 0.6674:003 0.6774:004 0.7724:003 0.7824:003 0.7824:003 0.7824:003 0.7824:003 0.7824:003 0.7824:003 0.7824:003 0.7824:003 0.7824:003 0.7824:003 0.7824:003 0.7824:003 0.7824:003 0.7824:003 0.7824:003 0.7824:003 0.7824:003 0.7824:003 0.7824:003 0.7724:013 0.7724:013 0.7724:013 0.7724:013 0.7724:013 0.7724:013 0.7724:013 0.7724:013 0.7724:013 0.7724:013 0.7724:013 0.7724:013 0.7724:013 0.7724:013 0.7724:013 0.7724:013 0.7724:013 0.7724:013 <td></td> <td>breastcancer</td> <td>0.733±0.05</td> <td>0.696±0.05</td> <td>0.744±0.04</td> <td>0.612±0.05</td> <td>0.754±0.04</td> <td>0.868±0.03</td> <td>0.596±0.06</td> <td>0.859±0.04</td> <td>0.815±0.04</td> <td>0.762 ± 0.04</td> <td>0.726±0.05</td> <td>0.865±0.04</td>		breastcancer	0.733±0.05	0.696±0.05	0.744±0.04	0.612±0.05	0.754±0.04	0.868±0.03	0.596±0.06	0.859±0.04	0.815±0.04	0.762 ± 0.04	0.726±0.05	0.865±0.04
F1-measure symputed signment optimization 0.6692-0.03 0.6522+0.03 0.6722-0.02 0.7222-0.02 0.7545-0.02 0.6972-0.02 0.6972-0.02 0.6972-0.02 0.6972-0.02 0.8722-0.02 0.8542-0.03 0.8524-0.03 0.8524-0.03 0.8524-0.01 0.7545-0.02 0.6972-0.02 0.6572-0.02 0.6972-0.02 0.6572-0.02 0.6572-0.02 0.6572-0.02 0.6572-0.02 0.6572-0.02 0.6572-0.01 0.0722-0.01 0.8526-0.01 0.7212-0.02 0.8526-0.01 0.0722-0.01 0.8526-0.01 0.0722-0.01 0.8526-0.01 0.0722-0.01 0.8526-0.01 0.0722-0.01 0.8526-0.01 0.0722-0.01 0.8526-0.01 0.0722-0.01 0.8526-0.01 0.0722-0.01 0.8526-0.01 0.0722-0.01 0.8526-0.01 0.0722-0.01 0.8526-0.01 0.0524-0.02 0.8526-0.01 0.0524-0.02 0.8526-0.01 0.0524-0.01 0.8526-0.01 0.8526-0.01 0.8526-0.01 0.8526-0.01 0.8526-0.01 0.8526-0.01 0.8526-0.01 0.8526-0.01 0.8526-0.01 0.8526-0.01 0.8526-0.01 0.8526-0.01 0.8526-0.01 0.8526-0.01 0.8526-0.01 0.8526-0.01 0.85		pima	0.675±0.05	0.666 ± 0.05	0.661±0.06	0.660 ± 0.04	0.670±0.04	0.772 ± 0.03	0.699 ± 0.04	0.693±0.04	0.695±0.05	0.675±0.04	0.727±0.04	0.720±0.05
Number symguidel 0.5784+00.3 0.5584+00.2 0.6782+00.2 0.772±00.2 0.7782±00.2 0.782±00.2 0.782±00.2 0.5584±00.2 0.8784±00.2 0.8782±00.1 0.7782±00.2 0.782±00.2 0.782±00.2 0.782±00.2 0.782±00.2 0.782±00.2 0.782±00.2 0.878±00.1 0.772±00.2 0.782±00.2 0.878±00.1 0.772±00.2 0.782±00.2 0.878±00.1 0.772±00.2 0.782±00.2 0.878±00.1 0.772±00.2 0.878±00.1 0.772±00.2 0.878±00.1 0.772±00.2 0.878±00.1 0.772±00.1 0.872±00.1 0.872±00.1 0.872±00.1 0.872±00.1 0.872±00.2 0.878±00.2 0.872±00.1 0.872±00.2 0.872±00.1 0.872±00.2 0.872±00.1 0.872±00.2 0.872±00.1 0.872±00.1 0.872±00.2 0.872±00.1 0.872±00.2 0.872±00.1 0.872±00.1 0.872±00.2 0.872±00.1 0.872±00.1 0.872±00.1 0.872±00.1 0.872±00.1 0.872±00.1 0.872±00.1 0.872±00.1 0.872±00.1 0.872±00.1 0.872±00.1 0.872±00.1 0.872±00.1 0.872±00.1 0.872±00.1 0.872±00.1 0.87	E1-measure	segment	0.660±0.03	0.652±0.03	0.667±0.03	0.583±0.03	0.707±0.03	0.825±0.01	0.687±0.02	0.722±0.02	0.765±0.02	0.697±0.02	0.622±0.03	0.827±0.02
musfixoms 0.750±0.02 0.754±0.02 0.764±0.01 0.876±0.01 0.772±0.02 0.876±0.01 0.712±0.02 0.876±0.01 0.876±0.01 0.874±0.01 0.874±0.01 0.874±0.01 0.874±0.01 0.874±0.01 0.874±0.01 0.874±0.01 0.874±0.01 0.874±0.01 0.524±0.01 0.874±0.01 0.872±0.01 0.882±0.01 0.882±0.01 0.882±0.01 0.882±0.01 0.882±0.01 0.882±0.01 0.882±0.01 0.882±0.01 0.882±0.01 0.882±0.01 0.882±0.01 0.882±0.01 0.882±0.01 0.882±0.01 0.882±0.01 0.882±0.01 0.882±0.01 0.882±0.	r r meusure	symguide1	0.554±0.03	0.545±0.02	0.569 ± 0.02	0.482±0.03	0.568±0.02	0.737±0.01	0.578±0.02	0.772±0.02	0.782 ± 0.02	0.553±0.02	0.558±0.02	0.862 ± 0.01
page-blocks0 0.6394.0.0 0.6254.0.0 0.7994.0.0 0.6224.0.0 0.7994.0.0 0.6724.0.0 0.6642.0.0 0.6724.0.0 0.6642.0.0 0.6724.0.0 0.6642.0.0 0.6724.0.0 0.6724.0.0 0.6724.0.0 0.6724.0.0 0.6624.0.0 0.6724.0.0 0.6624.0.0 0.6724.0.0 0.6624.0.0 0.6724.0.0 0.6624.0.0 0.6724.0.0 0.6324.0.0 0.6624.0.0 0.6624.0.0 0.6624.0.0 0.6724.0.0 0.6324.0.0 0.6324.0.0 0.6624.0.0 0.6624.0.0 0.6624.0.0 0.6624.0.0 0.6624.0.0 0.6624.0.0 0.6624.0.0 0.6624.0.0 0.6624.0.0 0.6624.0.0 0.6624.0.0 0.662		mushrooms	0.750±0.02	0.745±0.02	0.796 ± 0.01	0.744±0.01	0.809 ± 0.01	0.876±0.01	0.472±0.05	0.824±0.02	0.881 ± 0.02	0.826 ± 0.01	0.712±0.02	0.876±0.01
Imagic 0.5364:0.0 0.5324:0.0 0.7814:0.0 0.6324:0.0 0.8374:0.0 0.7324:0.0 0.5834:0.0 0.5994:0.0 0.5834:0.0 0.5994:0.0 0.5834:0.0 0.5994:0.0 0.5834:0.0 0.5994:0.0 0.5834:0.0 0.5994:0.0 0.5834:0.0 0.5994:0.0 0.5994:0.0 0.5834:0.0 0.5834:0.0 0.5834:0.0 0.5834:0.0 0.5834:0.0 0.5834:0.0 0.5834:0.0 0.5834:0.0 0.5834:0.0 0.5834:0.0 0.5834:0.0 0.5834:0.0 0.5834:0.0 0.5834:0.0 0.5834:0.0 0.5834:0.0 0.5834:0.0 0.5834:0.0 0.5744:0.0<		page-blocks0	0.639±0.02	0.625±0.02	0.793±0.01	0.584±0.02	0.654±0.02	0.799±0.01	0.622±0.02	0.825±0.01	0.795±0.01	0.672±0.02	0.609 ± 0.02	0.861±0.01
Average 0.648±0.04 0.6703±0.03 0.668±0.04 0.868±0.04 0.805±0.02 0.836±0.04 0.71±0.03 0.760±0.04 0.648±0.04 0.825±0.06 0.825±0.07 0.816±0.04 0.836±0.04 0.836±0.04 0.836±0.04 0.825±0.03 0.825±0.03 0.846±0.05 0.818±0.04 0.885±0.03 0.846±0.05 0.818±0.04 0.836±0.04 0.835±0.03 0.835±0.03 0.836±0.04 0.835±0.03 0.835±0.01		magic	0.536±0.02	0.530 ± 0.01	0.526 ± 0.01	0.517±0.02	0.642 ± 0.01	0.784±0.01	0.632 ± 0.01	0.837±0.01	0.752 ± 0.01	0.583±0.01	0.509 ± 0.02	0.853±0.01
Win-Lose 0-11 0-11 1-0 0-11 <		Average	0.648 ± 0.04	0.640 ± 0.04	0.703±0.03	0.608±0.05	0.685±0.04	0.805±0.02	0.636±0.04	0.771±0.03	0.760±0.04	0.666±0.04	0.648±0.04	0.824±0.03
ecoli 0.794±005 0.77±007 0.814±005 0.814±005 0.882±0.06 0.84±0.07 0.61±0.08 0.63±0.07 0.61±0.08 0.65±0.08 0.65±0.08 0.65±0.08 0.61±0.08 0.63±0.07 0.81±0.04 0.65±0.08 0.61±0.08 0.63±0.07 0.61±0.08 0.63±0.07 0.61±0.08 0.63±0.07 0.61±0.08 0.63±0.07 0.61±0.08 0.63±0.07 0.61±0.04 0.80±0.05 0.78±0.04 0.63±0.07 0.81±0.04 0.63±0.07 0.63±0.07 0.63±0.07 0.63±0.07 0.63±0.07 0.63±0.05 0.78±0.04 0.80±0.05 0.78±0.05 0.77±0.04 0.81±0.04 0.83±0.01 0.83±0.01 0.83±0.01 0.83±0.01 0.83±0.01 0.83±0.01 0.83±0.01 0.83±0.01 0.83±0.01 0.83±0.01 0.83±0.01 0.75±0.04 0.75±0.04 0.75±0.04 0.75±0.04 0.75±0.04 0.75±0.04 0.75±0.04 0.75±0.04 0.75±0.04 0.75±0.04 0.75±0.04 0.75±0.04 0.87±0.02 0.72±0.01 0.71±0.02 0.85±0.01 0.75±0.04 0.87±0.01 0.75±0.04 0.87±0.01 0.75±0.01 0.		Win-Lose	0-11	0-11	1-10	0-11	0-11	3-8	0-11	0-11	1-10	0-11	1-10	N/A
haberman 0.643±0.07 0.619±0.07 0.581±0.10 0.573±0.09 0.652±0.08 0.633±0.07 0.613±0.08 0.653±0.07 0.613±0.08 0.653±0.07 0.613±0.08 0.653±0.07 0.613±0.08 0.653±0.07 0.613±0.08 0.653±0.07 0.613±0.08 0.633±0.07 0.613±0.08 0.633±0.07 0.613±0.08 0.633±0.07 0.613±0.08 0.633±0.07 0.613±0.08 0.633±0.07 0.613±0.08 0.633±0.07 0.613±0.08 0.633±0.07 0.613±0.08 0.633±0.07 0.613±0.08 0.633±0.07 0.613±0.08 0.633±0.07 0.613±0.08 0.633±0.07 0.613±0.08 0.633±0.07 0.613±0.08 0.633±0.07 0.613±0.08 0.633±0.07 0.613±0.08 0.633±0.07 0.613±0.08 0.633±0.01 0.633±0.01 0.833±0.01 0.833±0.01 0.833±0.01 0.833±0.01 0.833±0.01 0.833±0.01 0.833±0.01 0.833±0.01 0.813±0.01 0.813±0.01 0.813±0.01 0.833±0.01 0.833±0.01 0.833±0.01 0.833±0.01 0.833±0.01 0.833±0.01 0.833±0.01 0.833±0.01 0.833±0.01 0.833±0.01 0.833±0.01 0.833±0.0		ecoli	0.794±0.05	0.776±0.05	0.782±0.06	0.725±0.06	0.777±0.07	0.816±0.05	0.817±0.05	0.808 ± 0.06	0.844±0.05	0.800 ± 0.05	0.825±0.06	0.882±0.04
creditApproval 0.79±0.05 0.78±0.05 0.81±0.04 0.768±0.03 0.846±0.05 0.784±0.05 0.836±0.04 0.836±0.05 0.835±0.04 0.836±0.05 0.835±0.04 0.836±0.05 0.784±0.05 0.836±0.04 0.812±0.04 0.812±0.04 0.812±0.04 0.812±0.04 0.835±0.02 0.825±0.01 0.770±0.02 0.806±0.01 0.745±0.04 0.732±0.04 0.724±0.03 0.873±0.02 0.852±0.01 0.704±0.04 0.873±0.01 0.873±0.01 0.835±0.01 0.724±0.01 0.835±0.01 0.724±0.01 0.835±0.01 0.835±0.01 0.873±0.01 0.852±0.01 0.873±0.01 0.852±0.01 0.873±0.01 0.873±0.01 0.873±0.01 0.873±0.01 0.873±0.01 0.873±0.01 0.873±0.01 0.873±0.01 0.873±0.01 0.873±0.01 0.873±0.01 0.873±		haberman	0.643±0.07	0.619±0.07	0.581±0.10	0.573±0.09	0.657±0.08	0.659±0.06	0.645±0.08	0.713±0.08	0.633±0.07	0.615±0.08	0.656±0.08	0.762±0.07
wisconsin 0.772±0.04 0.819±0.04 0.778±0.04 0.759±0.05 0.794±0.05 0.885±0.03 0.681±0.04 0.831±0.04 0.751±0.05 0.749±0.04 0.895±0.03 breastcancer 0.813±0.04 0.800±0.03 0.809±0.04 0.726±0.04 0.775±0.04 0.751±0.04 0.769±0.02 0.769±0.02 0.769±0.02 0.769±0.02 0.769±0.02 0.769±0.02 0.769±0.01 0.831±0.01 0.831±0.01 0.831±0.01 0.831±0.01 0.831±0.01 0.831±0.01 0.831±0.01 0.831±0.01 0.831±0.01 0.891±0.01 0.831±0.01 0.831±0.01 0.891±0.01 0.831±0.01 0.891±0.01 0.831±0.01 0.891±0.01 0.891±0.01 0.891±0.01 0.831±0.01 0.891±0.01 0.891±0.01 0.891±0.01		creditApproval	0.791±0.05	0.778±0.05	0.811±0.03	0.768±0.05	0.821±0.04	0.868±0.03	0.846±0.05	0.784±0.05	0.836±0.04	0.804±0.05	0.803±0.05	0.855±0.04
breastcancer 0.813±0.04 0.800±0.03 0.809±0.04 0.73±0.05 0.818±0.04 0.899±0.05 0.877±0.04 0.861±0.04 0.816±0.01 0.775±0.04 0.775±0.04 0.776±0.04 0.776±0.04 0.776±0.04 0.776±0.04 0.776±0.04 0.776±0.04 0.776±0.04 0.776±0.04 0.776±0.04 0.776±0.04 0.776±0.04 0.776±0.04 0.776±0.04 0.776±0.04 0.776±0.04 0.776±0.04 0.776±0.04 0.876±0.01 0.776±0.04 0.876±0.01 0.776±0.04 0.876±0.01 0.776±0.04 0.876±0.01 0.776±0.04 0.876±0.01 0.776±0.04 0.876±0.01 0.876±0.01 0.876±0.01 0.876±0.01 0.876±0.01 0.876±		wisconsin	0.772±0.04	0.819±0.04	0.778±0.04	0.759±0.05	0.794±0.05	0.885±0.03	0.681±0.04	0.881±0.04	0.831±0.04	0.751±0.05	0.749 ± 0.04	0.895±0.03
pima 0.745±0.05 0.732±0.04 0.735±0.05 0.707±0.04 0.742±0.02 0.774±0.03 0.674±0.03 0.742±0.02 0.774±0.03 0.674±0.03 0.782±0.01 0.775±0.04 0.775±0.04 0.763±0.05 0.764±0.04 0.796±0.04 0.775±0.04 0.763±0.05 0.746±0.04 0.796±0.04 0.775±0.04 0.763±0.02 0.852±0.02 0.852±0.02 0.852±0.02 0.852±0.02 0.852±0.02 0.852±0.02 0.852±0.02 0.852±0.02 0.852±0.01 0.853±0.01 0.853±0.01 0.853±0.01 0.874±0.01 <td></td> <td>breastcancer</td> <td>0.813±0.04</td> <td>0.800±0.03</td> <td>0.809±0.04</td> <td>0.726±0.05</td> <td>0.818 ± 0.04</td> <td>0.895±0.03</td> <td>0.679±0.05</td> <td>0.877±0.04</td> <td>0.861±0.04</td> <td>0.817±0.04</td> <td>0.810±0.05</td> <td>0.886±0.04</td>		breastcancer	0.813±0.04	0.800±0.03	0.809±0.04	0.726±0.05	0.818 ± 0.04	0.895±0.03	0.679±0.05	0.877±0.04	0.861±0.04	0.817±0.04	0.810±0.05	0.886±0.04
AUC segment 0.747±0.02 0.747±0.02 0.747±0.03 0.675±0.02 0.782±0.02 0.782±0.01 0.770±0.02 0.855±0.02 0.785±0.02 0.769±0.02 0.769±0.02 0.782±0.03 0.873±0.02 0.873±0.02 0.864±0.02 0.684±0.01 0.873±0.02 0.884±0.01 0.864±0.01		pima	0.745±0.05	0.732±0.04	0.735±0.05	0.707±0.04	0.742±0.04	0.776±0.04	0.757±0.04	0.775±0.04	0.763±0.05	0.746±0.04	0.793±0.04	0.796±0.04
svnguidel 0.691±0.02 0.681±0.02 0.678±0.02 0.678±0.02 0.720±0.01 0.701±0.02 0.8852±0.02 0.884±0.01 0.8852±0.02 0.685±0.02 0.685±0.02 0.689±0.01 0.893±0.01 mushrooms 0.853±0.01 0.849±0.01 0.849±0.01 0.828±0.01 0.870±0.01 0.734±0.01 0.734±0.01 0.734±0.01 0.734±0.01 0.830±0.01 0.870±0.01 0.734±0.01 0.652±0.01 0.893±0.01 0.868±0.01 0.884±0.01 0.881±0.01 0.868±0.01 0.734±0.01 0.742±0.02 0.898±0.01 magic 0.655±0.01 0.649±0.01 0.652±0.01 0.674±0.00 0.672±0.01 0.814±0.01 0.804±0.01 0.831±0.01 0.693±0.01 0.639±0.04 0.891±0.01 win-Lose 0-11 0-11 0-11 0-11 0.11 0.40 0.649±0.05 0.585±0.06 0.691±0.02 0.724±0.05 0.724±0.05 0.724±0.05 0.845±0.01 0.734±0.01 0.734±0.01 0.832±0.01 0.832±0.02 0.663±0.05 0.678±0.05 0.678±0.05 0.678±0.05 0.678±0.05 0.724±0.05	AUC	segment	0.747±0.02	0.742±0.02	0.747±0.03	0.667±0.03	0.782±0.02	0.852 ± 0.01	0.770±0.02	0.806±0.02	0.835±0.02	0.769 ± 0.02	0.720±0.03	0.873±0.02
mushrooms 0.833±0.01 0.849±0.01 0.849±0.01 0.876±0.01 0.976±0.01 0.972±0.03 0.893±0.01 0.904±0.01 0.870±0.01 0.830±0.01 0.901±0.01 page-hlocks0 0.742±0.01 0.754±0.01 0.679±0.01 0.679±0.01 0.816±0.01 0.734±0.01 0.880±0.01 0.860±0.01 0.870±0.01 0.860±0.01 0.870±0.01 0.870±0.01 0.870±0.01 0.870±0.01 0.860±0.01		svmguide1	0.691±0.02	0.681±0.02	0.677±0.02	0.623±0.02	0.678±0.02	0.720 ± 0.01	0.701±0.02	0.852±0.02	0.846±0.02	0.685±0.02	0.690 ± 0.02	0.893±0.01
page-blocks0 0.732±0.01 0.732±0.01 0.732±0.01 0.754±0.01 0.699±0.02 0.760±0.01 0.816±0.01 0.734±0.01 0.860±0.01 0.733±0.01 0.7754±0.02 0.898±0.01 magic 0.655±0.01 0.659±0.01 0.652±0.01 0.652±0.01 0.760±0.01 0.814±0.01 0.690±0.01 0.880±0.01 0.881±0.01 0.693±0.01 0.715±0.01 0.715±0.05 0.744±0.01 0.727±0.05 0.784±0.03 0.721±0.05 0.715±0.05 0.714±0.01 0.814±0.01 0.724±0.05 0.649±0.01 0.714±0.01 0.715±0.05 0.714±0.01 0.714±0.01 0.714±0.01 0.714±0.01 0.714±0.01 0.714±0.01 0.724±0.05 0.674±0.01		mushrooms	0.853±0.01	0.849 ± 0.01	0.849±0.01	0.828 ± 0.01	0.876±0.01	0.903±0.01	0.672±0.03	0.893±0.01	0.904±0.01	0.870±0.01	0.830±0.01	0.901±0.01
magic 0.655±0.01 0.649±0.01 0.652±0.01 0.632±0.01 0.736±0.01 0.814±0.01 0.690±0.01 0.881±0.01 0.633±0.01 0.630±0.01 0.891±0.01 Average 0.750±0.04 0.743±0.03 0.743±0.04 0.706±0.04 0.767±0.04 0.811±0.03 0.727±0.04 0.832±0.03 0.822±0.03 0.822±0.03 0.757±0.05 0.754±0.05 0.754±0.05 0.754±0.05 0.754±0.05 0.754±0.05 0.754±0.05 0.754±0.05 0.754±0.05 0.754±0.05 0.754±0.05 0.754±0.05 0.754±0.05 0.754±0.05 0.864±0.05 0.822±0.05 0.864±0.05 0.754±0.05 0.754±0.05 0.724±0.05 0.864±0.05 0.754±0.06 0.754±0.05 0.724±0.05 0.874±0.05 0.724±0.05 0.864±0.05 0.874±0.06 0.754±0.05 0.724±0.05 0.874±0.04 0.774±0.05 0.724±0.05 0.874±0.03 0.754±0.04 0.754±0.04 0.774±0.05 0.724±0.05 0.874±0.03 0.754±0.04 0.754±0.04 0.754±0.04 0.754±0.04 0.754±0.04 0.754±0.04 0.754±0.04 0.754±0.04 <th0.754±0.04< th=""> 0.754±0.04 <</th0.754±0.04<>		page-blocks0	0.742 ± 0.01	0.732±0.01	0.754±0.01	0.699 ± 0.02	0.760 ± 0.01	0.816 ± 0.01	0.734±0.01	0.880 ± 0.01	0.860 ± 0.01	0.773±0.01	0.726±0.02	0.898 ± 0.01
Average 0.750±0.04 0.743±0.03 0.743±0.04 0.700±0.04 0.767±0.04 0.819±0.03 0.727±0.04 0.832±0.03 0.822±0.03 0.757±0.05 0.748±0.04 0.867±0.03 win-Lose 0-11 0.752±0.06 0.752±0.06 0.752±0.06 0.722±0.05 0.723±0.05 0.652±0.02 0.723±0.05 0.723±0.05 0.723±0.05 0.723±0.05 0.723±0.05 0.723±0.05 0.723±0.05 0.723±0.05 0.723±0.05 0.723±0.05 0.723±0.05 0.723±0.05		magic	0.655±0.01	0.649±0.01	0.652±0.01	0.629±0.01	0.736±0.01	0.814±0.01	0.690±0.01	0.884±0.01	0.831±0.01	0.693±0.01	0.630 ± 0.01	0.891±0.01
G-mean 0 0 1 0 1 0 1 0 1 0 1 3 8 0 1 1 0 1 0 1 0 1 0 1 0 1 N/A ecoli 0.694±0.06 0.675±0.06 0.692±0.06 0.692±0.00 0.691±0.07 0.694±0.05 0.725±0.06 0.725±0.06 0.765±0.06 0.758±0.00 0.715±0.06 0.724±0.05 0.724±0.05 0.711±0.06 0.728±0.05 0.598±0.04 0.711±0.05 0.724±0.05 0.744±0.04 0.800±0.04 0.699±0.06 0.772±0.04 0.731±0.05 0.723±0.05 0.807±0.04 0.807±0.04 0.801±0.04 0.815±0.03 0.616±0.07 0.723±0.05 0.734±0.04 0.874±0.03 0.616±0.05 0.874±0.03 0.874±0.03 0.875±0.04 0.875±0.04 0.875±0.04 0.875±0.04 0.875±0.04 0.875±0.05 0.692±0.04 0.875±0.04 0.875±0.05 0.723±0.05 0.733±0.04 0.875±0.05 0.723±0.05 0.733±0.04 0.875±0.01 0.724±0.05 0.723±0.05 <td></td> <td>Average</td> <td>0.750±0.04</td> <td>0.743±0.03</td> <td>0.743±0.04</td> <td>0.700 ± 0.04</td> <td>0.767±0.04</td> <td>0.819±0.03</td> <td>0.727±0.04</td> <td>0.832±0.03</td> <td>0.822±0.03</td> <td>0.757 ± 0.05</td> <td>0.748 ± 0.04</td> <td>0.867±0.03</td>		Average	0.750±0.04	0.743±0.03	0.743±0.04	0.700 ± 0.04	0.767±0.04	0.819±0.03	0.727±0.04	0.832±0.03	0.822±0.03	0.757 ± 0.05	0.748 ± 0.04	0.867±0.03
ecoli 0.694±0.06 0.675±0.06 0.692±0.06 0.694±0.07 0.697±0.06 0.727±0.06 0.745±0.06 0.768±0.05 0.715±0.06 0.712±0.05 0.724±0.05 0.725±0.06 0.768±0.05 0.715±0.06 0.724±0.05 0.884±0.05 haberman 0.590±0.07 0.585±0.06 0.261±0.10 0.544±0.09 0.612±0.07 0.604±0.05 0.589±0.08 0.661±0.07 0.582±0.06 0.756±0.05 0.622±0.08 0.715±0.05 0.724±0.05 0.724±0.05 0.724±0.05 0.724±0.05 0.724±0.05 0.724±0.05 0.724±0.05 0.724±0.05 0.724±0.05 0.724±0.05 0.724±0.05 0.724±0.05 0.724±0.05 0.724±0.05 0.724±0.05 0.724±0.05 0.724±0.05 0.724±0.05 0.725±0.04 0.755±0.04 0.663±0.05 0.664±0.05 0.664±0.05 0.664±0.05 0.679±0.05 0.664±0.04 0.722±0.04 0.679±0.04 0.772±0.05 0.723±0.04 0.735±0.04 0.732±0.05 0.732±0.04 0.734±0.04 0.722±0.04 0.674±0.04 0.722±0.04 0.674±0.05 0.679±0.04 0.734±0.04 0.722±0.05 0.792±0.04		Win-Lose	0-11	0-11	0-11	0-11	0-11	3-8	0-11	0-11	1-10	0-11	0-11	N/A
haberman 0.559±0.07 0.585±0.06 0.261±0.10 0.541±0.07 0.612±0.07 0.582±0.08 0.661±0.07 0.582±0.06 0.562±0.07 0.622±0.08 0.711±0.06 0.711±0.05 0.723±0.05 0.622±0.08 0.711±0.05 0.723±0.05 0.723±0.05 0.711±0.06 0.771±0.05 0.723±0.0		ecoli	0.694±0.06	0.675±0.06	0.692±0.06	0.649±0.06	0.691±0.07	0.697±0.06	0.727±0.06	0.745±0.06	0.768±0.05	0.715±0.06	0.724±0.05	0.843±0.05
creditApproval 0.707±0.05 0.698±0.05 0.699±0.06 0.774±0.04 0.774±0.05 0.74±0.04 0.800±0.04 0.782±0.05 0.74±0.05 0.74±0.05 0.74±0.04 0.800±0.04 0.770±0.05 0.774±0.05 0.74±0.05 0.68±0.05 0.699±0.06 0.770±0.04 0.731±0.05 0.723±0.05 0.807±0.04 breastcancer 0.759±0.04 0.729±0.04 0.722±0.04 0.659±0.04 0.658±0.05 0.616±0.05 0.866±0.04 0.825±0.03 0.616±0.05 0.866±0.04 0.863±0.03 0.663±0.03 0.663±0.03 0.663±0.04 0.663±0.04 0.872±0.04		haberman	0.590±0.07	0.585±0.06	0.261±0.10	0.544±0.09	0.612±0.07	0.604±0.05	0.598±0.08	0.661±0.07	0.582±0.06	0.566±0.07	0.622±0.08	0.711±0.06
wisconsin 0.666±0.04 0.72±0.05 0.602±0.04 0.672±0.05 0.828±0.03 0.613±0.04 0.851±0.03 0.795±0.04 0.663±0.05 0.648±0.06 0.874±0.03 breastcancer 0.759±0.04 0.722±0.04 0.672±0.04 0.672±0.04 0.872±0.04 0.851±0.03 0.613±0.04 0.827±0.04 0.827±0.04 0.664±0.05 0.664±0.05 0.664±0.05 0.664±0.05 0.664±0.05 0.664±0.05 0.664±0.04 0.672±0.04 0.872±0.04 0.827±0.04 0.827±0.04 0.673±0.04 0.871±0.04 0.871±0.04 0.827±0.05 0.782±0.02 0.672±0.04 0.722±0.05 0.781±0.02 0.715±0.02 0.673±0.04 0.732±0.02 0.827±0.02 0.827±0.01 0.827±0.04 0.732±0.02 0.823±0.01 0.827±0.01 0.827±0.04 0.732±0.02 0.823±0.01 0.821±0.02 0.823±0.01 0.827±0.01 0.827±0.01 0.834±0.01 0.835±0.01 0.835±0.01 0.835±0.01 0.835±0.01 0.835±0.01 0.835±0.01 0.835±0.01 0.835±0.01 0.835±0.01 0.835±0.01 0.835±0.01 0.835±0.01 0.835±0.01 0.835±0.01		creditApproval	0.707±0.05	0.698±0.05	0.690±0.04	0.690±0.05	0.744±0.04	0.800 ± 0.04	0.768±0.05	0.699±0.06	0.770±0.04	0.731±0.05	0.723±0.05	0.807±0.04
breastcancer 0.759±0.04 0.729±0.04 0.729±0.04 0.672±0.04 0.675±0.04 0.871±0.04 0.871±0.04 0.871±0.04 0.871±0.04 0.882±0.03 0.664±0.05 0.882±0.04 0.753±0.04 0.871		wisconsin	0.666 ± 0.04	0.724±0.05	0.602 ± 0.04	0.672±0.05	0.728±0.05	0.828±0.03	0.613±0.04	0.851±0.03	0.795±0.04	0.663±0.05	0.648 ± 0.06	0.874±0.03
pima 0.676±0.05 0.668±0.04 0.663±0.05 0.674±0.04 0.670±0.05 0.702±0.04 0.697±0.04 0.694±0.05 0.679±0.02 0.724±0.04 0.727±0.05 G-mean segment 0.679±0.02 0.680±0.02 0.676±0.02 0.674±0.02 0.679±0.02 0.719±0.02 0.702±0.01 0.679±0.02 0.734±0.04 0.727±0.05 germent 0.679±0.02 0.680±0.02 0.676±0.02 0.676±0.02 0.679±0.02 0.709±0.02 0.730±0.02 0.731±0.02 0.731±0.02 0.653±0.02 0.683±0.02 0.882±0.01 mustrooms 0.772±0.02 0.782±0.02 0.763±0.02 0.674±0.01 0.882±0.01 0.881±0.01 0.678±0.01 0.684±0.01 0.682±0.01 0.882±0.01 page-blocks0 0.681±0.02 0.763±0.02 0.633±0.02 0.667±0.01 0.667±0.01 0.667±0.01 0.667±0.01 0.674±0.01 0.792±0.01 0.882±0.01 magic 0.580±0.01 0.580±0.01 0.667±0.01 0.667±0.01 0.667±0.01 0.674±0.01 0.775±0.01 0.627±0.01 0.622±0.01 0.882±0.01		breastcancer	0.759±0.04	0.729±0.04	0.722±0.04	0.659±0.04	0.775±0.04	0.853±0.03	0.616±0.05	0.866±0.04	0.827±0.04	0.783±0.03	0.753±0.04	0.871±0.04
G-mean segment 0.679±0.02 0.680±0.02 0.676±0.02 0.607±0.03 0.719±0.02 0.799±0.02 0.701±0.02 0.739±0.02 0.731±0.02 0.715±0.02 0.653±0.02 0.832±0.02 svmguidel 0.605±0.02 0.598±0.02 0.599±0.02 0.599±0.02 0.607±0.02 0.599±0.02 0.617±0.02 0.799±0.01 0.899±0.01 0.604±0.01 0.604±0.01 0.604±0.01 0.869±0.01 0.889±0.01 0.879±0.01 0.799±0.01 0.799±0.01 0.799±0.01 0.799±0.01 0.799±0.01 0.799±0.01 0.799±0.01 0.799±0.01 0.627±0.01 0.627±0.01 0.627±0.01 0.627±0.01 0.627±0.01 0.627±0.01		pima	0.676±0.05	0.668±0.04	0.663±0.05	0.654±0.04	0.670±0.04	0.692±0.05	0.702±0.04	0.697±0.04	0.694±0.05	0.679±0.04	0.734±0.04	0.727±0.05
svmguide1 0.605±0.02 0.598±0.02 0.599±0.02 0.607±0.02 0.599±0.02 0.607±0.02 0.599±0.02 0.607±0.02 0.599±0.02 0.679±0.02 0.799±0.02 0.799±0.01 0.604±0.01 0.608±0.02 0.688±0.02 0.869±0.01 mushrooms 0.772±0.02 0.678±0.02 0.763±0.01 0.824±0.01 0.879±0.01 0.837±0.01 0.604±0.01 0.608±0.02 0.869±0.01 page-blocks0 0.681±0.02 0.679±0.01 0.634±0.02 0.690±0.02 0.722±0.01 0.659±0.02 0.887±0.01 0.772±0.01 0.606±0.02 0.869±0.01 magic 0.586±0.01 0.589±0.01 0.607±0.01 0.722±0.01 0.638±0.01 0.847±0.01 0.775±0.01 0.627±0.01 0.562±0.01 Average 0.674±0.04 0.671±0.03 0.621±0.04 0.634±0.04 0.743±0.03 0.656±0.04 0.779±0.03 0.694±0.03 0.654±0.04 0.861±0.01 Win-Lose 0-11 0-11 0-11 0-11 0-11 0-11 0-11 0-11 0-11 0.10 0.672±0.01 0.654±0.04	G-mean	segment	0.679±0.02	0.680 ± 0.02	0.676±0.02	0.607±0.03	0.719±0.02	0.769±0.02	0.701±0.02	0.739±0.02	0.781±0.02	0.715±0.02	0.653±0.02	0.832±0.02
mushrooms 0.772±0.02 0.768±0.02 0.782±0.02 0.763±0.01 0.824±0.01 0.830±0.01 0.835±0.01 0.839±0.01 0.839±0.01 0.742±0.01 0.882±0.01 page-blocks0 0.651±0.02 0.670±0.01 0.569±0.02 0.633±0.02 0.690±0.02 0.72±0.01 0.659±0.02 0.838±0.01 0.810±0.01 0.702±0.01 0.669±0.02 0.869±0.01 magic 0.586±0.01 0.582±0.01 0.565±0.01 0.656±0.01 0.667±0.01 0.673±0.01 0.638±0.01 0.810±0.01 0.702±0.01 0.669±0.02 0.869±0.01 0.638±0.01 0.810±0.01 0.775±0.01 0.627±0.01 0.625±0.01 0.869±0.01 0.869±0.01 0.875±0.04 0.775±0.01 0.627±0.01 0.869±0.01 0.869±0.01 0.869±0.01 0.875±0.04 0.825±0.01 0.869±0.01 0.869±0.01 0.869±0.01 0.875±0.04 0.825±0.01 0.869±0.01 0.869±0.01 0.869±0.01 0.825±0.04 0.869±0.01 0.869±0.01 0.869±0.01 0.869±0.01 0.869±0.01 0.869±0.01 0.869±0.01 0.869±0.01 0.862±0.01 0.862±0.01 0.		svmguide1	0.605±0.02	0.598±0.02	0.599±0.02	0.539±0.02	0.607±0.02	0.599±0.02	0.617±0.02	0.790±0.02	0.798±0.01	0.604 ± 0.01	0.608±0.02	0.869 ± 0.01
page-blocks0 0.681±0.02 0.670±0.01 0.569±0.02 0.633±0.02 0.690±0.02 0.722±0.01 0.659±0.02 0.838±0.01 0.810±0.01 0.709±0.01 0.660±0.02 0.869±0.01 magic 0.586±0.01 0.582±0.01 0.580±0.01 0.667±0.01 0.731±0.01 0.639±0.01 0.812±0.01 0.672±0.01 0.562±0.01 0.814±0.01 0.731±0.01 0.675±0.01 0.627±0.01 0.562±0.01 0.814±0.01 0.775±0.01 0.627±0.01 0.562±0.01 0.814±0.01 0.775±0.01 0.674±0.03 0.674±0.04 0.775±0.01 0.674±0.03 0.814±0.01 0.814±0.01 0.775±0.01 0.674±0.03 0.674±0.04 0.814±0.01 0.775±0.01 0.674±0.03 0.674±0.04 0.814±0.01 0.775±0.01 0.674±0.03 0.674±0.04 0.814±0.01 0.814±0.01 0.814±0.01 0.775±0.01 0.674±0.03 0.674±0.04 0.814±0.01 0.775±0.01 0.674±0.03 0.674±0.04 0.814±0.01 0.775±0.01 0.674±0.03 0.674±0.04 0.814±0.01 0.775±0.01 0.674±0.03 0.674±0.04 0.814±0.01 0.775±0.01 0.674±0.03		mushrooms	0.772±0.02	0.768±0.02	0.782±0.02	0.763±0.01	0.824±0.01	0.880 ± 0.01	0.573±0.04	0.836±0.01	0.887 ± 0.01	0.839±0.01	0.742 ± 0.01	0.882±0.01
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		page-blocks0	0.681±0.02	0.670±0.01	0.569±0.02	0.633±0.02	0.690±0.02	0.722±0.01	0.659±0.02	0.838±0.01	0.810±0.01	0.709±0.01	0.660±0.02	0.869 ± 0.01
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		magic	0.586 ± 0.01	0.582±0.01	0.580 ± 0.01	0.565 ± 0.01	0.667±0.01	0.731±0.01	0.638±0.01	0.847±0.01	0.775±0.01	0.627±0.01	0.562 ± 0.01	0.861±0.01
Win-Lose 0–11 0–11 0–11 0–11 0–11 0–11 0–11 0–1		Average	0.674 ± 0.04	0.671±0.03	0.621±0.04	0.634±0.04	0.702±0.03	0.743±0.03	0.656±0.04	0.779±0.03	0.772±0.03	0.694±0.03	0.675±0.04	0.831±0.03
		Win-Lose	0-11	0-11	0-11	0-11	0-11	0-11	0-11	0-11	1-10	0-11	1-10	N/A

TABLE 5. Mean and variance of 12 oversampling methods under 5 classifiers on each real-world dataset (nI = 20%).

performed by merging the intra-cluster sparsity and multi-711 class density information of the samples. For clustering-712 based methods, particularly means-S. and RSMOTE, even 713 though they combine clustering with synthetic sample 714 size assignment. However, OOSI utilizes oriented weights 715 containing multi-class information levels of samples to 716 effectively guide the improvement of the sample synthesis 717 path, generating new samples close to information-rich areas 718 and preventing the development of extra noise samples and 719 overlapping samples. These extensive results demonstrate the 720 overall advantage of OOSI in handling imbalanced and noisy 721 data 722

Tables 3-5 present, due to limited space, the mean 723 and standard deviation of each real dataset for the ten 724 methods under five classifiers and three metrics. In each 725 row of Tables 3-5, the method that outperform OOSI 726 are highlighted in bold. The rows labeled "Average" contain the results for all datasets as a whole. The rows 728 labeled "Win-Lose" represent the cumulative results of the 729 method outperforming or underperforming OOSI across all 730 datasets. 731

Overall, it can be seen from Tables 3-5 that for all noise levels, metrics, and datasets, the "Win-Lose" of the comparison methods is almost "0-11". It demonstrates that for all noise levels, metrics, and comparison methods, OOSI outperforms the comparison method on 11 datasets in most cases. Additionally, the bolded portion, which is slightly better than OOSI's comparison method, is almost

TABLE 6. The results of p-value for the friedman test.

Noise levels	F-measure	AUC	G-mean
0%	3.80E-02 *	1.81E-02 *	4.07E-02 *
5%	1.84E-03 *	1.26E-02 *	1.75E-03 *
10%	2.30E-05 *	4.43E-03 *	6.77E-05 *
15%	4.43E-05 *	2.76E-04 *	2.43E-05 *
20%	4.72E-07 *	1.24E-04 *	1.24E-06 *

concentrated in relatively small datasets, which shows that 739 the OOSI performs better with larger datasets. The possible 740 reason is that larger datasets contain more information, and 741 the OOSI fully excavates and utilizes the data information 742 to guide reasonable sampling. Even in the absence of 743 noise, the OOSI method improves F-measure, AUC, and 744 G-mean by 2.6%, 2%, and 3.2%, respectively. When there 745 is noise, that is, the noise level is 10%, the OOSI method 746 improves F-measure, AUC, and G-mean by 11.5%, 8.4%, and 747 11.7%, respectively. Particularly in comparison to ADASYN, 748 the greatest improvement has been made. When there is 749 no noise, the F-measure, AUC, and G-mean increase by 750 5.3%, 3.9%, and 5.6%, respectively, whereas they increase 751 by 21.6%, 16.7%, and 19.2% when the noise level is 752 20%. It emonstrates that the OOSI method outperforms the 753 comparison algorithms of 11 different strategies and achieves 754 better performance improvements on the noisy imbalanced 755 dataset. 756



FIGURE 4. The average rank sums of comparing algorithms on five classifiers and 11 datasets.

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TABLE 7. Average running time of comparative oversampling algorithms (Sec).

Datasets	STkL	SIPF	SFRST	ADASYN	MWMOTE	AdaptS.	DBSMOTE	means-S.	RSMOTE	SG	SSW	OOSI
ecoli	0.401	0.605	0.499	0.411	0.492	0.456	0.391	0.444	0.370	0.150	0.769	0.324
haberman	0.547	0.524	0.422	0.592	0.253	0.629	0.443	0.485	0.374	0.370	0.588	0.373
creditApproval	0.176	0.504	0.305	0.514	0.419	0.955	0.257	0.323	0.347	0.241	0.152	0.279
wisconsin	0.266	0.391	0.461	0.602	0.413	0.600	0.411	0.403	0.380	0.290	0.758	0.478
breastcancer	0.265	0.384	0.441	0.325	0.420	1.276	0.347	0.403	0.429	0.256	0.813	0.419
pima	0.164	0.168	0.384	0.132	0.750	3.242	0.286	0.340	0.433	0.201	0.296	0.359
segment	0.671	1.313	0.252	0.342	0.782	18.77	0.492	0.336	0.726	0.180	0.578	0.634
svmguide1	0.696	0.667	0.949	0.347	0.979	15.02	1.504	0.663	0.634	0.200	0.692	0.139
mushrooms	9.987	1.561	6.456	0.602	6.809	483.8	0.209	0.154	1.562	0.353	5.018	4.524
page-blocks0	0.223	1.800	1.309	0.549	2.281	51.57	1.334	0.500	0.595	0.256	1.272	0.186
magic	0.902	10.13	23.88	0.241	19.14	357.1	0.806	0.299	0.341	0.731	5.333	0.635
Mean rank	5.182	7.455	7.636	5.455	8.636	11.45	5.545	4.818	5.727	2.364	7.909	4.728

757 E. NONPARAMETRIC STATISTICAL ANALYSIS

To verify whether the performance of different algorithms 758 has a statistically significant difference, the non-parametric 759 friedman test is used to analyze the experimental results of 760 12 methods on five classifiers and 11 datasets. The Friedman 761 test contributes significantly to experimental analysis. It can 762 be used to compare whether or not three or more related 763 samples differ substantially without making any assumptions 764 about the samples' distributions [45]. The fundamental concept of the Friedman test is to arrange each algorithm's 766 experimental data on distinct datasets in ascending order 767 and designate ranks. The ranks with the greatest and worst 768 performance are 1 and 12, respectively, at this time. Then, 769 statistics and p-values are calculated based on the rank sums 770 determined for each algorithm. If the statistic exceeds the 771 critical value or the p-value is less than the significance 772 level (typically 0.05), the null hypothesis is rejected and the 773 performance of distinct algorithms is deemed significantly 774 different. 775

Figure 4 depicts the average rank sums of the contrasted 776 algorithms on five classifiers and 11 datasets. The red and 777 blue columns, respectively, represent OOSI and comparison 778 algorithms. The crimson bars are consistently larger than the 779 blue bars for all noise levels and metrics. It demonstrates that 780 the OOSI algorithm's average rank sum is superior to the 781 comparison algorithm's. Additionally, Table 6 displays the 782 p-value results of the Friedman test on five classifiers and 783 eleven data sets. The * indicators reject the null hypothesis at 784 a significance level of 0.05. For all noise levels and metrics, 785 the calculated p-values are less than 0.05, indicating that the performance of the various algorithms differs significantly. 787 Likewise, the smaller the p-value, the more significant the 788 difference. It can be observed from the table that as the noise 789 level increases, the p-value continues to decrease, indicating 790 that the performance difference between the algorithms is 791 also intensified. 792

793 F. VALIDATING AVERAGE RUNNING TIME

The average running time of ten executions of the compared
oversampling algorithms is shown in Table 7. Each dataset's
least time-consuming algorithm is highlighted in bold. In the

column designated "Mean rank", the friedman test's mean 797 rank sum is analyzed. The method with the lowest rank 798 is the fastest, and the algorithm with the lowest average 799 rank sum is highlighted in red bold. From Table 7, it can 800 be seen that OOSI achieves four of the quickest running 801 efficiencies across 11 datasets, as well as the most victories. 802 Although the OOSI algorithm is not the least time-consuming 803 on every data set, in most cases, the difference between it 804 and the least time-consuming algorithm is tiny, and it is 805 almost always ranked highly in terms of time-consumption 806 relative to other comparable algorithms. Consequently, 807 by integrating all eleven data sets, the OOSI algorithm 808 achieves the lowest average time-consuming ranking. As a 809 whole, the OOSI algorithm's average running time is 810 competitive. 811

V. CONCLUSION

To cope with both imbalance and noise problems, an adaptive 813 and robust oriented oversampling method with spatial 814 information (OOSI) is proposed. It is an adaptive and 815 rare sampling method that can guide rational sample 816 generalization and sample synthesis path boosting with 817 spatial information. First, the dataset-specific clustering 818 space is adaptively partitioned to mine the data distribution 819 information. After that, OOSI integrates intra-cluster sparsity 820 and multi-class density information to quantify spatial infor-821 mation to guide reasonable sample generalization in different 822 clusters, which not only prevents over-generalization in 823 specific regions but also effectively alleviates intra-class 824 inter-class imbalance. Finally, to avoid noisy samples from 825 introducing deteriorating generalization, sample synthesis 826 paths are guided according to the level of multi-class 827 information among non-noisy seed samples, avoiding the 828 uncontrollability associated with random linear interpolation. 829 The main advantages of OOSI compared to existing methods 830 are that a) It is a rare adaptive and robust oversampling 831 method; b) it can prevent noise hazards with the innovative 832 three-stage noise suppression strategy rather than removing 833 them; c) it can create safe synthetic minority samples with 834 spatial information to avoid overgeneralization and sampling 835 blindness of SMOTE. 836

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Extensive comparative experiments were performed with 837 11 sampling algorithms with different strategies. Experi-838 ments demonstrated that (a) OOSI outperforms comparative 839 sampling algorithms in 5 baseline classifiers on extensive 840 real-world datasets with varying noise levels; (b) OOSI 841 with the lowest average rank is statistically superior to the 842 comparison algorithms; (c) the average running time of OOSI 843 is competitive due to its lowest average time-consuming 844 ranking. 845

In the future, these results encourage the development 846 of OOSI as a useful tool for improving the sampling 847 mechanism to rebalance the dataset by generating high 848 quality artificial data. In addition, OOSI may not have 849 optimal runtime on certain complex datasets. To overcome 850 this limitation, efficient clustering improvement strategies 851 will be further explored. Furthermore, while oversampling 852 equalizes class imbalances and improves the learning ability 853 of unrepresented classes and reduces overfitting. However, 854 the potential drawbacks that have received little attention i.e., 855 local ambiguity and unnaturalness may introduce ambiguous 856 and deviating samples from the data distribution. Although 857 the proposed OOSI not only prevents the intrusion of 858 noisy or unsuitable samples through a three-stage noise suppression strategy, but also guides rational and data-860 distribution-compliant sampling through the quantization of 861 spatial information. While this mitigates local ambiguity 862 and unnaturalness to some extent, further attention and 863 exploration of more solutions are critical.

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