<span id="page-0-8"></span>

Received 1 September 2023, accepted 18 October 2023, date of publication 27 October 2023, date of current version 3 November 2023. *Digital Object Identifier 10.1109/ACCESS.2023.3328234*

## **RESEARCH ARTICLE**

# Design and Implementation of Spectrally Efficient Frequency Division Multiplexing Receiver

#### YUANJ[I](https://orcid.org/0009-0003-6234-7712)N[G](https://orcid.org/0009-0000-5755-1995) QI<sup>®1</sup>, TINGTING ZHANG®2, YUAN F[E](https://orcid.org/0000-0002-5429-3318)NG<sup>3</sup>, ZHEN QIN<sup>1</sup>, AND DONGXUAN HE<sup>®1,4</sup>

<sup>1</sup> School of Information and Electronics, Beijing Institute of Technology, Beijing 100081, China

<sup>2</sup>School of Integrated Circuits and Electronics, Beijing Institute of Technology, Beijing 100081, China

<sup>3</sup>China Research and Development Academy of Machinery Equipment, Beijing 100089, China

<sup>4</sup>Cooperative Detection and Control Center for Complex Networked Systems (CDCC), Yangtze Delta Region Academy, Beijing Institute of Technology, Jiaxing 314000, China

Corresponding author: Yuan Feng (13810535152@139.com)

This work was supported in part by the National Natural Science Foundation of China under Grant 62101306.

**ABSTRACT** Compared to orthogonal frequency division multiplexing (OFDM), spectrally efficient frequency division multiplexing (SEFDM) provides higher spectrum efficiency, which has been regarded as a promising waveform for future wireless communications. Against this background, the design of SEFDM receiver is investigated in this paper, considering its sampling frequency synchronization (SFS), timing synchronization, phase recovery, and detector design. Specifically, a two-step SFS module, which consists of a coarse sampling frequency offset (SFO) compensation and a frequency domain zero-forcing based fine estimation, is proposed first. Next, a low-complexity timing synchronization scheme is designed to avoid excessive multipliers and look-up-tables. Furthermore, an SFO-based phase recovery is proposed, which shares the compensation and SFO estimation with SFS module, thus further reducing the complexity of SEFDM receiver. Moreover, the truncated singular value decomposition-fixed sphere decoder (TSVD-FSD) based detector has been studied to efficiently eliminate intercarrier interference. Simulation results demonstrate the superiority of our proposed SEFDM receiver, where the transmission rate can be improved by 25% at a loss of only 0.7dB bit error ratio compared to OFDM. Finally, field programmable gate array (FPGA) based implementation is carried out to verify the effectiveness of our proposed SEFDM receiver in practice.

**INDEX TERMS** Spectrally efficient frequency division multiplexing (SEFDM), sampling frequency synchronization (SFS), low-complexity implementation structure, field programmable gate array (FPGA).

#### **I. INTRODUCTION**

<span id="page-0-0"></span>With the rapid development of wideband emerging services, such as cloud computing, virtual reality, metaverse, digital twin, etc., next generation wireless communication faces great challenges on the ever-increasing demand of transmission throughput [\[1\]. A](#page-8-0)s a result, an increasing focus has been paid to spectral efficient transmission schemes exemplified by faster-than-Nyquist (FTN) and spectrally efficient frequency division multiplexing (SEFDM) [\[2\],](#page-8-1) [\[3\],](#page-8-2) [\[4\]. In](#page-8-3) particular, the SEFDM [\[5\], wh](#page-8-4)ich reduces the spacing between subcarriers compared to orthogonal frequency division multiplexing (OFDM), can enhance the spectral

<span id="page-0-3"></span>The associate editor coordinating the r[evie](https://orcid.org/0000-0003-3924-227X)w of this manuscript and approving it for publication was Yiming Huo $^{\circ}$ .

<span id="page-0-5"></span>efficiency significantly. To be noticed, such spectral efficient enhancement approach has shown that the signaling rate can be increased by 25% without performance degradation compared to its OFDM counterpart [\[6\]. In](#page-8-5) recent years, SEFDM has been studied to facilitate several communication scenarios such as wireless communication [\[7\]](#page-8-6) and optical communication [\[8\].](#page-8-7)

<span id="page-0-7"></span><span id="page-0-6"></span><span id="page-0-4"></span><span id="page-0-2"></span><span id="page-0-1"></span>Benefiting from the non-orthogonality between subcarriers, SEFDM shows extremely high bandwidth efficiency. However, such non-orthogonality also introduces severe intercarrier interference (ICI), which deteriorates the transmission performance significantly. To tackle this problem, many works concerning signal detection have been proposed to improve the reception performance of SEFDM system. For example, a maximum likelihood (ML) detector for

#### <span id="page-1-0"></span>**TABLE 1.** Comparison of different receiver schemes.



<span id="page-1-2"></span><span id="page-1-1"></span>SEFDM was proposed in [\[5\]](#page-8-4) to guarantee optimal reliable signal detection at the cost of unacceptable complexity. To reduce the complexity, the sphere decoding (SD) and fixed SD (FSD) based detectors were proposed, which avoid redundant operations by setting a limited search radius [\[9\],](#page-8-8) [\[10\].](#page-8-9) In addition, the simple linear detectors, such as zero-force (ZF) detector and minimum mean square error (MMSE) detector, were proposed [\[11\],](#page-8-10) [\[12\]. H](#page-8-11)owever, both ZF detector and MMSE detector are sensitive to the ill-conditional subcarrier correlation matrix, thus leading to serious performance degradation. To address this issue, the truncated singular value decomposition (TSVD) was utilized to handle the subcarrier correlation matrix, which improves the detection performance obviously [\[13\].T](#page-8-12)o further enhance the performance of FSD detector, the TSVD-FSD detector was proposed, which applies the estimation of TSVD detector as the initialization of FSD detector [\[14\]. S](#page-8-13)ubsequently, several improved detectors, such as ID-FSD detector [\[15\],](#page-8-14)  $[16]$ , trellis detector  $[17]$ , and factor graph-based iterative detector [\[18\], w](#page-9-2)ere proposed to improve detection performance. Nevertheless, the above SEFDM detectors highly relies on a perfect synchronization, which is hard to realize in practice.

<span id="page-1-8"></span><span id="page-1-7"></span>To be noticed, the multicarrier systems are typically sensitive to synchronization error, which makes accurate synchronization important to SEFDM system. Due to the severe ICI caused by SEFDM modulation and demodulation, the synchronization performance of SEFDM is usually limited. To solve this problem, the method of [\[20\]](#page-9-3) utilized the OFDM symbol preambles for synchronization, which ignores the effect of ICI. However, to guarantee the demodulation performance, a specific preambles structure is required, which increases the complexity of SEFDM receiver obviously. Furthermore, the SEFDM receiver suffers from a large resource consumption when existing detector algorithms are adopted. Thus, the low-complexity structure of synchronization based on SEFDM symbol preambles should be studied for SEFDM system.

To realize effective timing synchronization, the Schmidl and Cox (S&C) timing synchronization algorithm [\[21\]](#page-9-4) was commonly utilized in SEFDM system, where the correlation of two specific part of preamble is employed to estimate the timing offset [\[19\]. D](#page-9-5)ue to their similarity in cyclic prefixes and synchronization metric functions, SEFDM and OFDM exhibit similar timing metric curves with flat top. Accordingly, there exists a large estimation error for S&C algorithm. Aiming at reducing the estimation <span id="page-1-17"></span><span id="page-1-13"></span><span id="page-1-12"></span><span id="page-1-11"></span><span id="page-1-10"></span>error, several timing synchronization methods, such as Minn algorithm, Park algorithm, etc., were applied in OFDM system [\[22\],](#page-9-6) [\[23\],](#page-9-7) [\[25\],](#page-9-8) [\[26\],](#page-9-9) [\[31\]. B](#page-9-10)y designing appropriate timing synchronization preamble and synchronization metric function, the peak of timing metric curve became more sharp and recognizable, thus leading to an improve timing synchronization accuracy. In particular, the methods in [\[22\],](#page-9-6) [\[23\],](#page-9-7) [\[25\],](#page-9-8) [\[26\], a](#page-9-9)nd [\[31\]](#page-9-10) can also be adopted in SEFDM system by setting an SEFDM symbol preamble. However, the above algorithms need two parts of preamble, which reduces the throughput especially under small signal to noise ratio (SNR).

<span id="page-1-14"></span><span id="page-1-6"></span><span id="page-1-5"></span><span id="page-1-4"></span><span id="page-1-3"></span>The above timing synchronization algorithm cannot eliminate the sampling frequency offset (SFO) caused by the difference between oscillator frequencies at transmitter and receiver. The authors in [\[27\]](#page-9-11) show that the SFO in multicarrier system can be expressed as a phase rotation in frequency domain. Subsequently, several sampling frequency synchronization (SFS) algorithms were proposed to estimate the SFO with the help of pilot signals [\[28\],](#page-9-12) [\[29\]. H](#page-9-13)owever, these works only utilize the phase differences to estimate the SFO, the performance of which is limited when SFO is large. Furthermore, the SFO estimation suffers from severe inherent ICI in SEFDM system, thus leading to an inevitable accuracy degradation.

<span id="page-1-16"></span><span id="page-1-15"></span>In this paper, we design and implement a novel SEFDM receiver structure. Our main contributions are boldly and explicitly contrasted to the state-of-the-art in Table [1](#page-1-0) at a glance as well as in more detail below:

- A two-step SFS module concerning both frequency domain and time domain processing is proposed. In particular, a ZF-SFS algorithm is utilized for fine SFO estimation in frequency domain, and a coarse adjustment controlled by fine SFO estimation is designed in time domain.
- SFO based phase recovery method is investigated for the proposed SEFDM receiver. By sharing the SFO estimator and compensator with the SFS module, the implementation complexity of our proposed phase recovery module can be greatly reduced.
- <span id="page-1-9"></span>• The implementation structure of the proposed SEFDM receiver using field programmable gate arrays (FPGAs) is presented. Compared to OFDM, the bit error rate (BER) performance loss of our proposed SEFDM is only 1.2 dB when packing factor  $\alpha = 0.8$ .

The remainder of this paper is organized as follows. In Section [II,](#page-2-0) we present the system model of SEFDM system.

<span id="page-2-2"></span>

<span id="page-2-4"></span>**FIGURE 1.** The block diagram of the SEFDM modem structure.



**FIGURE 2.** Frame structure for SEFDM.

In Section [III,](#page-2-1) a novel SEFDM receiver structure is designed. In Section [IV,](#page-6-0) simulation results and implementation results are presented. Finally, conclusions are drawn in Section [V.](#page-8-15)

#### <span id="page-2-0"></span>**II. SYSTEM MODEL**

The proposed SEFDM system structure is depicted in Fig. [1.](#page-2-2) At the transmitter, the information bits are mapped into multiple phase shift keying (MPSK) or multiple quadrature amplitude modulation (MQAM) symbols. The mapped symbols are allocated into *N* subcarriers by a serial-toparallel (S/P) conversion and fed to the inverse fractional Fourier transform (IFrFT) module.<sup>[1](#page-2-3)</sup>

Consequently, the equivalent baseband SEFDM signals can be presented as

$$
x(t) = \sqrt{\frac{1}{T}} \sum_{n=0}^{N-1} s_n e^{\frac{i2\pi\alpha nt}{T}},
$$
 (1)

where  $s_n$  is the transmitted symbol of the *n*th subcarrier,  $0 < \alpha \leq 1$  is the packing factor, and *T* is the SEFDM signal duration.

The frame structure of the proposed SEFDM system is given in Fig. [2.](#page-2-4) The preamble is inserted every  $N_d$  SEFDM symbols, where the first preamble duration *PRE*1 contains  $N_s$  symbols and the second preamble duration  $PRE2$  =  $\text{conj}(PRE1)$  with  $\text{conj}(\cdot)$  denoting the conjugate operation.

The received signal at time *t* can be expressed as

<span id="page-2-5"></span>
$$
r(t) = x(t) + w(t),
$$
\n(2)

where *w*(*t*) denotes additive white Gaussian noise (AWGN) with zero mean and variance  $\sigma_0^2$ .

At the receiver, the output matrix of the fractional Fourier transform (FrFT) module can be expressed as

$$
Y = CS + W,\t\t(3)
$$

where  $S = [s_0, s_1, \ldots, s_{N-1}]$  denotes the  $N \times 1$  transmitted symbol, and *W* is the  $N \times 1$  independent Gaussian noise samples. **C** is the  $N \times N$  sub-carrier correlation matrix, given by

$$
\mathbf{C} = \begin{bmatrix} c_{0,0} & c_{0,1} & \cdots & c_{0,N-1} \\ c_{1,0} & c_{1,1} & \cdots & c_{1,N-1} \\ \vdots & \vdots & \ddots & \vdots \\ c_{N-1,0} & c_{N-1,1} & \cdots & c_{N-1,N-1} \end{bmatrix},
$$
 (4)

where  $c_{m,n}$  is the cross correlation between the *m*th and *n*th element, given by

$$
c_{m,n} = \frac{1}{N} \sum_{k=0}^{N-1} f_{n,k} \hat{f}_{k,m},
$$
 (5)

where  $f_{n,k} = e^{-\frac{j2\pi n k\alpha}{N}}$  and  $\hat{f}_{k,m} = e^{\frac{j2\pi k m\alpha}{N}}$ .

#### <span id="page-2-1"></span>**III. LOW-COMPLEXITY SEFDM RECEIVER**

In this section, a novel SEFDM receiver structure is proposed, which consists of a two-step SFS, a low-complexity timing synchronization, a phase recovery, and a TSVD-FSD detector.

#### A. SAMPLING FREQUENCY SYNCHRONIZATION

The received signal with SFO can be expressed as  $y(t \Delta \phi nT'$ , where  $\Delta \phi = \phi_n - \phi_{n-1}$  represents the SFO with  $\phi_n$ denoting the phase of *n*th subcarrier. *T* ′ denotes the sampling clock at receiver. The output of the FrFT can be expressed as

$$
Y_n = \sqrt{\frac{1}{N}} \int_0^{T'} y(t - \Delta \phi n T') e^{-\frac{i2\pi \omega n t}{N}} dt
$$
  
=  $\sqrt{\frac{1}{N}} \int_0^{T'} y(t - \Delta t n T' - \Delta \hat{\phi} n T') e^{-\frac{-i2\pi \omega n t}{N}} dt$   
=  $A \sqrt{\frac{1}{N}} \int_0^{T'} y(t - \Delta t n T') e^{-\frac{-i2\pi \omega n t}{N}} dt$ , (6)

where  $\Delta t nT'$  is a multiple of *T*, and  $\Delta t$  is the integral part of SFO.  $\Delta \hat{\phi}$  is the decimal part of SFO.  $A = e^{\frac{-i2\pi \alpha \Delta \hat{\phi} nT}{N}}$ indicates phase rotation caused by the decimal part. The integral part results in a input sequence disruption as  $y(t \Delta t nT'$ ), which influences all the subcarriers and is hard to eliminate.

To estimate the SFO accurately, a two-step SFS, as shown in Fig. [3,](#page-3-0) is proposed for SEFDM receiver. The newly proposed SFS consists of a time domain coarse adjustment and a frequency domain fine estimation, which will be detailed as follows.

#### 1) TIME DOMAIN COARSE ADJUSTMENT

The time domain coarse adjustment is designed for eliminating the integral part of SFO, which can be realized by

<span id="page-2-3"></span><sup>&</sup>lt;sup>1</sup>The transmitted symbols can be implemented by IFrFT operation, which can also be replaced by an inverse fast Fourier transform (IFFT) with higher implementation efficiency [\[30\].](#page-9-14)

<span id="page-3-0"></span>

**FIGURE 3.** The structure of SFS module.

controlling the location of the input data *r*. To implement the coarse adjustment, a data selector is utilized in the time domain, which contains a S/P convertor and a switch. The S/P converter groups the serial data into  $N_{ds} = R_{ua}/R_{ud}$ blocks, where  $R_{ua}$  is the upsampling rate of analog-to-digital converter (ADC), and  $R_{ud}$  is the upsampling rate of the input data of timing synchronization.

The data selector should be adjusted according to the *adjust*\_*flag* provided by the frequency domain fine estimation. The switch is used to select the output path. When *adjust*\_*flag* is setting as 0 or 1, the switch would move forward or backward, respectively.

#### 2) FREQUENCY DOMAIN FINE ESTIMATION

The integral part of SFO has been eliminated by the time domain coarse adjustment. As a result, the signal calculated by FrFT can only be influenced by the decimal part of SFO, given by

$$
Y_n = e^{\frac{-i2\pi\alpha\Delta\hat{\phi}nT'}{N}} \sqrt{\frac{1}{N}} \int_0^{T'} y(t)e^{\frac{-i2\pi\alpha nt}{N}} dt.
$$
 (7)

The traditional preamble-based SFS algorithms calculate the phase difference between adjacent subcarriers of *Yn*. However, owing to the loss of orthogonality between subcarriers, the constellation points from FrFT deviate from their ideal locations, which influences the calculation of phase difference and causes a performance degradation in SFS module. To mitigate ICI, the inverse of the inherent ICI matrix is used to eliminate the inherent ICI before the preamble-based SFS algorithm, which can be mathematically expressed as

$$
F = \mathbf{C}^{-1}Y. \tag{8}
$$

For the *m*th SEFDM preamble symbol, the estimated SFO can be expressed as

$$
\Delta \phi_m = \frac{1}{N-1} \sum_{n=1}^{N-1} \arctan \frac{D_{m,n} - D_{m,n-1}}{1 + D_{m,n} D_{m,n-1}},
$$
(9)

where  $D_{m,n} = \text{imag}(F_{m,n}\tilde{F}_{m,n})/\text{real}(F_{m,n}\tilde{F}_{m,n}), \text{ real}(\cdot)$ means the real operation, *imag*(·) means the imaginary operation. *Fm*,*<sup>n</sup>* is the input preamble of *n*th subcarrier and  $\tilde{F}_{m,n}$  is the *n*th stored frequency domain subcarrier preamble.

The final estimated SFO can be calculated as

<span id="page-3-1"></span>
$$
\Phi = \frac{1}{2N_s} \sum_{m=0}^{2N_s - 1} \Delta \phi_m,
$$
\n(10)

The structure of the SFS is shown in Fig. [3.](#page-3-0) More specially, the inverse of the inherent ICI matrix **C** and the frequency domain preamble are stored in the read-only memories (ROMs), and the phase differences are calculated by the CORDIC core. Because the phase differences calculated by CORDIC core are between  $-\pi$  and  $\pi$ , the accumulated value should be compensated. When the phase difference is more than  $\pi$  or less than  $-\pi$ , the accumulation *q* will be extended to  $2\pi$  or  $-2\pi$  as follows.

$$
q = \begin{cases} q - 2\pi & e_m > \pi \\ q + 2\pi & e_m < -\pi \\ q & otherwise, \end{cases}
$$
 (11)

where  $e_m$  denotes the calculated phase difference.

The Judgement module controls the *adjust*\_*flag*. When the estimated SFO is less than a lower threshold, *adjust*\_*flag* is set as 0. Besides, when the estimated SFO is greater than an upper threshold, *adjust*\_*flag* is set as 1. The lower threshold and upper threshold can be set as  $-\pi/2$  and  $\pi/2$ , respectively.

<span id="page-4-0"></span>

**FIGURE 4.** The correlation curves in the different data sample ratio as (a)  $R_c = 1$ , (b)  $R_c = 2$ .

#### B. TIMING SYNCHRONIZATION

The timing synchronization can estimate the timing offset in the SEFDM system. The existing algorithms, such as S&C algorithm, Minn algorithm, Park algorithm, etc., typically require two halves of time domain preambles, thus reducing the length of correlation. To fully utilize the preamble in timing synchronization, the designed timing synchronization technique needs to store the whole preambles. To find the starting of the SEFDM symbol, the maximum point of the timing metric should be estimated. In the designed timing synchronization, the timing metric is given by

$$
M_d(d) = \frac{|P(d)|^2}{B^2(d)},
$$
\n(12)

where *d* is a time index, *B*(*d*) denotes the average energy of the input data  $[b_d, b_{d-1}, \ldots, b_{d-2N_s+1}]$ , and  $P(d)$  is given by

$$
P(d) = \frac{1}{2N_s} \sum_{m=0}^{2N_s - 1} (b_{d-m} \check{b}_m^*),
$$
 (13)

where  $\dot{b}_m$  denotes the *m*th stored time domain preamble, and (·) ∗ indicates the conjugate operation.

<span id="page-4-2"></span>

**FIGURE 5.** The structure of timing synchronization.

<span id="page-4-3"></span>

**FIGURE 6.** The structure of carrier recovery.

Due to the sampling bias, the input data gradually deviates from its best sampling point. Thus, the data upsampling rate will influence the maximum point of the timing metric. Fig. [4](#page-4-0) shows the timing metric  $M_d$  in the different data upsampling rate. To visualize the changes in correlation peaks, the input data is set as the period of the preamble. The data upsampling ratio are set as  $R_{uc} = 1$  and  $R_{uc} = 2$ , respectively. It can be seen that the correlation peaks in Fig. [4\(b\)](#page-4-0) are higher than that in Fig.  $4(a)$ . To find the maximum point of the timing metric more accurately, the data upsampling rate in the designed timing synchronization structure must be equal or greater than 2.

From  $(13)$ , it can be known that the calculation of  $P(d)$ requires  $L_s$  =  $2NN_d$  complex multipliers. To reduce the computational complexity, we quantize the signal amplitude and then employ shift operation to approximate the multiplication. The structure of timing synchronization is shown in Fig. [5,](#page-4-2) and the output preamble can be obtained directly from the D flip-flop without waiting for long serial output.

#### C. CARRIER RECOVERY

The parallel preamble obtained by timing synchronization is divided into two groups  $[a_0, a_1, \cdots, a_{N/2-1}]$  and  $[a_{N/2}, a_{N/2+1}, \cdots, a_{N-1}]$ . The accumulation of conjugate multiplication with two groups of preamble is expressed as

$$
E = \sum_{n=0}^{N/2-1} a_n a_{N/2+n}.
$$
 (14)

<span id="page-4-1"></span>By calculating the angle of the *E*, i.e.  $O = \angle E$  with  $\angle(\cdot)$ representing the angle operation, the carrier frequency offset can be obtained.

<span id="page-5-0"></span>

**FIGURE 7.** The structure of joint sampling frequency synchronization and phase recovery.

<span id="page-5-1"></span>

**FIGURE 8.** The block diagram of detector.

The structure of carrier recovery is shown in Fig. [6,](#page-4-3) where the signal can be compensated by a direct digital synthesizer module according to the estimated carrier frequency offset.

#### D. PHASE RECOVERY

In this section, we design an SFO based phase recovery structure. To reduce its complexity, modules exemplified by first-in first-out (FIFO), CORDIC core, and multiplier in phase recovery are shared with SFS module.

The relationship between the phase offset and the SFO in the *l*th SEFDM symbol and *n*th subcarrier can be obtained as

$$
e_{l,n} + \hat{\Phi}_n = \angle(Y_{l,n} \check{Y}_{l,n}^*), \tag{15}
$$

where  $e_{l,n}$  is the phase offset.  $\check{Y}_{l,n}$  denotes the stored frequency domain preamble sequence.  $\hat{\Phi}_n$  is the accumulation

of SFO, which can be expressed as  $\hat{\Phi}_n = n\Phi$ . The  $\Phi$  can be gained by [\(10\).](#page-3-1) Accordingly, the estimated phase offset can be presented as

$$
e_{l,n} = \angle(Y_{l,n} \check{Y}_{l,n}^*) - n\Phi. \tag{16}
$$

By averaging the phase offsets, the estimated phase offset in each frame can be expressed as

$$
\overline{e} = \frac{1}{L_s} \sum_{n=0}^{N-1} \sum_{l=0}^{N_d-1} e_{l,n}.
$$
 (17)

The structure of SFO based phase recovery is shown in Fig. [7,](#page-5-0) where *SHIFT* 1 and *SHIFT* 2 represent the formula *n*8 and 1/*L<sup>s</sup>* , respectively.

#### E. DETECTOR

We employ the TSVD-FSD algorithm to detect the signals, which can achieve acceptable detection performance with low implementation complexity. In TSVD-FSD algorithm, the initial radius of the search hypersphere in FSD algorithm is calculated by TSVD algorithm, which can be expressed as

$$
g = \|R - \mathbf{C}S_{TSVD}\|^2,\tag{18}
$$

where  $R$  is the input data of detector, and the estimation of TSVD algorithm *STSVD* is expressed as

$$
S_{TSVD} = \lfloor \mathbf{C}_{\xi} R \rceil, \tag{19}
$$

where  $|\cdot|$  is the slicing operation. The TSVD based pseudoinverse of **C**, denoted by  $C_{\xi}$ , can be calculated as

$$
\mathbf{C}_{\xi} = \mathbf{V} \Sigma_{\xi}^{-1} \mathbf{U}^*,\tag{20}
$$

where  $\Sigma_{\xi} = diag(1/\sigma_1, 1/\sigma_2, \cdots, 1/\sigma_{\xi}, 0, \cdots, 0)$  and  $\xi$  < *N* is truncation index. Using the SVD operation to the

<span id="page-6-1"></span>

**FIGURE 9.** BER performance of the proposed SEFDM system.

inherent ICI matrix **C**, the perematers **V**,  $\Sigma_{\xi}$ , and **U** can be executed as

$$
C = U\Sigma V^*,\tag{21}
$$

where  $\Sigma = diag(\sigma_1, \sigma_2, \cdots, \sigma_N)$ ,  $\sigma_i$  is the *i*th singular value of **C**.

By calculating initial radius, the TSVD-FSD algorithm is defined as

$$
S_{TSVD-FSD} = arg \min_{\tilde{S} \in Q} ||R - \tilde{CS}||^2 \le g
$$
  
= arg \min\_{\tilde{S} \in Q} ||\mathbf{L}(\tilde{S}\_{TSVD} - \tilde{S})||^2 \le g (22)

where **L** is an  $N \times N$  upper triangular matrix defined by chol $\{C^*C\}$  =  $L^*L$ , chol $\{\cdot\}$  donates the Cholesky decomposition, and *Q* is the constellation cardinality.

The block diagram of TSVD-FSD is shown in Fig. [8.](#page-5-1) The processing element (PE) calculates the partial Euclidean distance (PED), while the AED, which means the accumulated PED, is calculated by sorting. The  $\tilde{S}_o$  means the ordered constellation points.

#### <span id="page-6-0"></span>**IV. SIMULATION RESULTS AND IMPLEMENTATION**

In this section, the performance of the proposed SEFDM receiver is presented, as well as the experiential results of its FPGA implementation.

#### <span id="page-6-4"></span>A. SIMULATION RESULTS

According to previous studies[\[31\],](#page-9-10) [\[32\], th](#page-9-15)e parameters of the simulation are shown as follows. The number of subcarriers is  $N = 12$ , and the modulation scheme is quadrature phase shift keying (QPSK). The preamble is inserted every  $N_d$  = 60 SEFDM symbols, where the length of each preamble is  $N_s$  = 5 SEFDM symbols. To adapt the proposed two-step SFS structure, the upsampling rate of ADC is  $R_{ua} = 8$ , and the upsampling rate of the data selector is  $R_{ud} = 2$ .

The BER performance of the proposed SEFDM receiver structure is shown in Fig. [9,](#page-6-1) where the packing factors  $\alpha$ 

<span id="page-6-2"></span>

**FIGURE 10.** MSE of SFOs in ZF-SFS algorithm and SFS algorithm.

<span id="page-6-3"></span>

**FIGURE 11.** False alarm rate of Park algorithm, traditional correlation algorithm and designed algorithm in timing synchronization.

are set as 0.8 and 0.9, respectively. It can be seen that the BER performance of the proposed SEFDM receiver with  $\alpha$  = 0.9 is close to that of the OFDM system, while the transmission rate can be increased by 11%. When  $\alpha = 0.8$ , the BER performance loss is only 0.7dB with transmission rate increasing 25%, which suggests the proposed structure can achieve considerable transmission rate with acceptable BER performance loss.

<span id="page-6-5"></span>In Fig. [10,](#page-6-2) the sampling frequency performance realized by SFS algorithm in [\[28\]](#page-9-12) and our proposed ZF-SFS are compared, where the performance of OFDM system with SFS algorithm is also plotted as a benchmark. It can be observed that the proposed ZF-SFS algorithm outperforms SFS. In particular, the performance gain becomes more apparent as the packing factor  $\alpha$  becomes smaller, which validates the superiority of the proposed method.

The timing synchronization performance is presented in Fig. [11.](#page-6-3) The judgement threshold of correlation is set as

<span id="page-7-0"></span>

**FIGURE 12.** The comparison of EVM performance.

<span id="page-7-1"></span>

**FIGURE 13.** The BER performance with the proposed SFO based phase recovery and the independent phase recovery.

 $T_h = (C_{max,1} + C_{max,2})/2$  without noise.  $C_{max,1}$  and  $C_{max,2}$ represent the maximum peak value and the second-maximum peak value of timing metric in one frame, respectively. The complex multipliers in traditional timing synchronization structure will be replaced by adders, thus reducing hardware cost.

The comparison of the false alarm rates between the designed timing synchronization algorithm, the traditional correlation algorithm and the Park algorithm are shown in Fig. [11.](#page-6-3) Because of the same length of preambles, the correlation length of Park algorithm is half of the other two algorithms, resulting in a worse timing synchronization performance. Particularly, the false alarm rate gap between designed algorithm and Park algorithm is about 4.5 dB. By contrast, the false alarm rate of designed algorithm is similar to traditional correlation algorithm with the gap at about 0.2 dB.

In Fig. [12,](#page-7-0) we compare the error vector magnitude (EVM) of the proposed synchronization structure with SFO based

<span id="page-7-2"></span>

**FIGURE 14.** The experimental setup of the proposed SEFDM communication system.

<span id="page-7-3"></span>

**FIGURE 15.** The measured spectrum: (a) SEFDM spectrum, (b) OFDM spectrum.

phase recovery and independent phase recovery, where the EVM achieved by ideal synchronization is also plotted as a benchmark. It is observed that the proposed SFO based phase recovery has a similar EVM to the independent method, and the complexity of the proposed structure is much lower. Compared to the ideal synchronization, the proposed synchronization structure leads to a 0.5 dB loss. To further verify the effectiveness of the SFO based phase recovery, the BER performance of the SEFDM system with the proposed SFO based phase recovery is shown in Fig. [13.](#page-7-1) It can be seen that the SEFDM receiver with SFO based phase recovery performs a similar BER performance compared to the independent phase recovery. The proposed phase recovery structure ignores the phase offset caused by the SFS module, which leads to a 0.1 dB loss of BER performance.

#### B. FPGA IMPLEMENTATION

Finally, Zynq UltraScale+ RFSoC ZCU208 Evaluation Kit and Zynq UltraScale+ RFSoC ZCU111 Evaluation Kit are utilized to implement the SEFDM transmitter and receiver, respectively. Fig. [14](#page-7-2) depicts the experimental setup of our designed SEFDM communication system.

Moreover, the sampling rate of ADC is configured as  $R_{adc} = 140MSPS$ , and the bit data rate is  $R_b = 35Mbps$ , which means that the QPSK symbol rate is  $R_s = 17.5$ MSPS. After the data selector, the sampling rate is set as  $R_c$  = 35MHz. The carrier frequency is  $f_c$  = 280MHz. Other parameters are the same as that in Section [IV-A.](#page-6-4)

The spectrum of OFDM signal and SEFDM signal based on the above system parameters are shown in Fig. [15.](#page-7-3) It can

<span id="page-8-16"></span>**TABLE 2.** Resource utilization of the proposed SEFDM receiver hardware design.

Resource	Utilization	Available	Utilization rate
<b>LUTs</b>	129938	425280	30.6%
FFs.	213939	850560	$25.1\%$
<b>BRAM</b>	44	1080	4%
DSP48s	2958	4772	69.2%

<span id="page-8-17"></span>**TABLE 3.** Computational complexity of timing synchronization.



<span id="page-8-18"></span>

**FIGURE 16.** The BER performance of the proposed SEFDM system implemented in FPGA.

be seen that the SEFDM signal has a smaller bandwidth compared with the OFDM signal. Table [2](#page-8-16) shows the resource utilization of the FPGA-implemented proposed SEFDM receiver structure in terms of LUTs, FFs, DSP48s and block RAM (BRAM). To have a comprehensive understanding of the computational complexity of the proposed SEFDM receiver, the total numbers of complex multipliers and complex adders in timing synchronization are detailed in Table [3.](#page-8-17) From Table [3,](#page-8-17) it is evident that the designed timing synchronization algorithm requires less complex multipliers when compared to the Park algorithm and traditional correlation algorithm.

The implemented BER performance as a function of  $E_b/N_0$  for the proposed SEFDM system in FPGA is shown in Fig. [16.](#page-8-18) The parameter  $\alpha$  is set to 0.9 and 0.8, respectively. It can be seen that the performance gap between the implementation structure and simulation structure is about 0.5 dB, which is caused by the performance loss of analog devices. Compared with the BER performance of the OFDM system, the implemented SEFDM receiver with  $\alpha$  = 0.9 has a loss of 0.8 dB and the implemented SEFDM receiver with  $\alpha$  = 0.8 has a loss of 1.2 dB. Nevertheless, the spectrum efficiency gain is 11% and 25%, respectively.

#### <span id="page-8-15"></span>**V. CONCLUSION**

In this paper, we proposed a low-complexity SEFDM receiver, consisting of synchronization modules and detector design. As for synchronization, a novel two-step SFS is presented and a ZF-SFS algorithm is proposed for the SEFDM system. Then, a low-complexity timing synchronization structure and an SFO based phase recovery structure are proposed to reduce resources cost. The performance of the proposed SEFDM receiver was evaluated by simulations and then implemented in FPGA. It is demonstrated that the proposed SEFDM receiver is able to improve the spectrum efficiency by 25% with about 1.2 dB BER performance loss, which verifies the effectiveness of our proposed SEFDM receiver.

#### **REFERENCES**

- <span id="page-8-0"></span>[\[1\] A](#page-0-0). Ibrahim, E. Bedeer, and H. Yanikomeroglu, "A novel low complexity faster-than-Nyquist (FTN) signaling detector for ultra high-order QAM,'' *IEEE Open J. Commun. Soc.*, vol. 2, pp. 2566–2580, 2021.
- <span id="page-8-1"></span>[\[2\] Y](#page-0-1). Ma, N. Wu, J. A. Zhang, B. Li, and L. Hanzo, ''Parametric bilinear iterative generalized approximate message passing reception of FTN multicarrier signaling,'' *IEEE Trans. Commun.*, vol. 69, no. 12, pp. 8443–8458, Dec. 2021.
- <span id="page-8-2"></span>[\[3\] W](#page-0-2). Yuan, N. Wu, Q. Guo, Y. Li, C. Xing, and J. Kuang, ''Iterative receivers for downlink MIMO-SCMA: Message passing and distributed cooperative detection,'' *IEEE Trans. Wireless Commun.*, vol. 17, no. 5, pp. 3444–3458, May 2018.
- <span id="page-8-3"></span>[\[4\] Y](#page-0-3). Chen, T. Xu, and I. Darwazeh, ''Index modulation pattern design for non-orthogonal multicarrier signal waveforms,'' *IEEE Trans. Wireless Commun.*, vol. 21, no. 10, pp. 8507–8521, Oct. 2022.
- <span id="page-8-4"></span>[\[5\] M](#page-0-4). Rodrigues and I. Darwazeh, "A spectrally efficient frequency division multiplexing based communications system,'' in *Proc. 8th Int. OFDM Workshop*, Hamburg, Germany, 2003, pp. 48–49.
- <span id="page-8-5"></span>[\[6\] J](#page-0-5). E. Mazo, ''Faster-than-nyquist signaling,'' *Bell Syst. Tech. J.*, vol. 54, no. 8, pp. 1451–1462, Oct. 1975.
- <span id="page-8-6"></span>[\[7\] T](#page-0-6). Xu and I. Darwazeh, "Transmission experiment of bandwidth compressed carrier aggregation in a realistic fading channel,'' *IEEE Trans. Veh. Technol.*, vol. 66, no. 5, pp. 4087–4097, May 2017.
- <span id="page-8-7"></span>[\[8\] Y](#page-0-7). Wang, Y. Zhou, T. Gui, K. Zhong, X. Zhou, L. Wang, A. P. T. Lau, C. Lu, and N. Chi, ''Efficient MMSE-SQRD-based MIMO decoder for SEFDMbased 2.4-Gb/s-spectrum-compressed WDM VLC system,'' *IEEE Photon. J.*, vol. 8, no. 4, pp. 1–9, Aug. 2016.
- <span id="page-8-8"></span>[\[9\] I](#page-1-1). Kanaras, A. Chorti, M. R. D. Rodrigues, and I. Darwazeh, ''Spectrally efficient FDM signals: Bandwidth gain at the expense of receiver complexity,'' in *Proc. IEEE Int. Conf. Commun.*, Jun. 2009, pp. 1–6.
- <span id="page-8-9"></span>[\[10\]](#page-1-2) S. Isam and I. Darwazeh, ''Design and performance assessment of fixed complexity spectrally efficient FDM receivers,'' in *Proc. IEEE 73rd Veh. Technol. Conf. (VTC Spring)*, May 2011, pp. 1–5.
- <span id="page-8-10"></span>[\[11\]](#page-1-3) I. Kanaras, A. Chorti, M. R. D. Rodrigues, and I. Darwazeh, ''A combined MMSE-ML detection for a spectrally efficient non orthogonal FDM signal,'' in *Proc. 5th Int. Conf. Broadband Commun., Netw. Syst.*, Sep. 2008, pp. 421–425.
- <span id="page-8-11"></span>[\[12\]](#page-0-8) S. Osaki, M. Nakao, T. Ishihara, and S. Sugiura, ''Differentially modulated spectrally efficient frequency-division multiplexing,'' *IEEE Signal Process. Lett.*, vol. 26, no. 7, pp. 1046–1050, Jul. 2019.
- <span id="page-8-12"></span>[\[13\]](#page-1-4) R. C. Grammenos, S. Isam, and I. Darwazeh, "FPGA design of a truncated SVD based receiver for the detection of SEFDM signals,'' in *Proc. IEEE 22nd Int. Symp. Pers., Indoor Mobile Radio Commun.*, Sep. 2011, pp. 2085–2090.
- <span id="page-8-13"></span>[\[14\]](#page-1-5) S. Isam, I. Kanaras, and I. Darwazeh, "A truncated SVD approach for fixed complexity spectrally efficient FDM receivers,'' in *Proc. IEEE Wireless Commun. Netw. Conf.*, Cancun, Mexico, Mar. 2011, pp. 1584–1589.
- <span id="page-8-14"></span>[\[15\]](#page-1-6) T. Xu, R. C. Grammenos, F. Marvasti, and I. Darwazeh, ''An improved fixed sphere decoder employing soft decision for the detection of nonorthogonal signals,'' *IEEE Commun. Lett.*, vol. 17, no. 10, pp. 1964–1967, Oct. 2013.

### **IEEE** Access

- <span id="page-9-0"></span>[\[16\]](#page-0-8) I. Darwazeh, R. C. Grammenos, and T. Xu, "Spectrally efficient frequency division multiplexing for 5G,'' in *5G Mobile Communications*, W. Xiang, K. Zheng, and X. S. Shen, Eds. Cham, Switzerland: Springer, 2017, pp. 261–297.
- <span id="page-9-1"></span>[\[17\]](#page-1-7) A. Rashich, A. Kislitsyn, D. Fadeev, and T. N. Nguyen, "FFT-based trellis receiver for SEFDM signals,'' in *Proc. IEEE Global Commun. Conf. (GLOBECOM)*, Dec. 2016, pp. 1–6.
- <span id="page-9-2"></span>[\[18\]](#page-1-8) Y. Feng, Y. Ma, Z. Li, C. Yan, and N. Wu, "Low-complexity factor graphbased iterative detection for RRC-SEFDM signals,'' in *Proc. 10th Int. Conf. Wireless Commun. Signal Process. (WCSP)*, Hangzhou, China, Oct. 2018, pp. 1–6.
- <span id="page-9-5"></span>[\[19\]](#page-0-8) W. Ozan, H. Ghannam, P. A. Haigh, and I. Darwazeh, "Experimental implementation of real-time non-orthogonal multi-carrier systems in a realistic fading channel,'' in *Proc. IEEE Radio Wireless Symp. (RWS)*, Jan. 2018, pp. 121–124.
- <span id="page-9-3"></span>[\[20\]](#page-0-8) H. Ghannam, D. Nopchinda, M. Gavell, H. Zirath, and I. Darwazeh, ''Experimental demonstration of spectrally efficient frequency division multiplexing transmissions at E-band,'' *IEEE Trans. Microw. Theory Techn.*, vol. 67, no. 5, pp. 1911–1923, May 2019.
- <span id="page-9-4"></span>[\[21\]](#page-1-9) T. M. Schmidl and D. C. Cox, ''Robust frequency and timing synchronization for OFDM,'' *IEEE Trans. Commun.*, vol. 45, no. 12, pp. 1613–1621, Dec. 1997.
- <span id="page-9-6"></span>[\[22\]](#page-1-10) H. Minn, M. Zeng, and V. K. Bhargava, "On timing offset estimation for OFDM systems,'' *IEEE Commun. Lett.*, vol. 4, no. 7, pp. 242–244, Jul. 2000.
- <span id="page-9-7"></span>[\[23\]](#page-1-11) B. Park, H. Cheon, C. Kang, and D. Hong, ''A novel timing estimation method for OFDM systems,'' *IEEE Commun. Lett.*, vol. 7, no. 5, pp. 239–241, May 2003.
- [\[24\]](#page-0-8) X. Fan, J. Yang, and W. Zhang, "Time-frequency synchronization design of OFDM systems based on CAZAC sequence,'' in *Proc. Int. Conf. Commun., Inf. Syst. Comput. Eng.*, 2020, pp. 55–58.
- <span id="page-9-8"></span>[\[25\]](#page-1-12) K. Wang, Y. Liu, and Z. Hong, "A novel timing synchronization method for DCO-OFDM-based VLC systems,'' *IEEE Photon. J.*, vol. 13, no. 4, pp. 1–9, Aug. 2021.
- <span id="page-9-9"></span>[\[26\]](#page-1-13) K. Wang, Y. Liu, Z. Hong, and Z. Zeng, ''Efficient timing offset estimation method tailored for ACO-OFDM VLC systems,'' *J. Lightw. Technol.*, vol. 40, no. 8, pp. 2307–2320, Apr. 15, 2022.
- <span id="page-9-11"></span>[\[27\]](#page-1-14) D.-K. Kim, S.-H. Do, H.-K. Lee, and H.-J. Choi, "Performance evaluation of the frequency detectors for orthogonal frequency division multiplexing,'' *IEEE Trans. Consum. Electron.*, vol. 43, no. 3, pp. 776–783, Aug. 1997.
- <span id="page-9-12"></span>[\[28\]](#page-1-15) B. Yang, Z. Ma, and Z. Cao, ''ML-oriented DA sampling clock synchronization for OFDM systems,'' in *Proc. Int. Conf. Commun. Technol.*, 2000, pp. 781–784.
- <span id="page-9-13"></span>[\[29\]](#page-1-16) J. Kim, E. J. Powers, and Y. Cho, "A non-synchronized sampling scheme,'' in *Proc. 36th Asilomar Conf. Signals, Syst., Comput.*, Nov. 2002, pp. 1900–1904.
- <span id="page-9-14"></span>[\[30\]](#page-2-5) S. Isam and I. Darwazeh, "Simple DSP-IDFT techniques for generating spectrally efficient FDM signals,'' in *Proc. 7th Int. Symp. Commun. Syst., Netw. Digit. Signal Process. (CSNDSP)*, Jul. 2010, pp. 20–24.
- <span id="page-9-10"></span>[\[31\]](#page-1-17) X. Liu, T. Xu, and I. Darwazeh, "Coexistence of orthogonal and nonorthogonal multicarrier signals in beyond 5G scenarios,'' in *Proc. 2nd 6G Wireless Summit (6G SUMMIT)*, Mar. 2020, pp. 1–5.
- <span id="page-9-15"></span>[\[32\]](#page-6-5) E. Kim, J. Yang, and J. Kim, ''Novel OFDM frame synchronization and frequency offset compensation scheme for wireless multimedia communication systems,'' *IEEE Trans. Consum. Electron.*, vol. 55, no. 3, pp. 1141–1148, Aug. 2009.



TINGTING ZHANG received the Ph.D. degree from the Institute of Information Engineering, Chinese Academy of Sciences, in 2016. She is currently an Assistant Research Fellow with the School of Information and Electronics, Beijing Institute of Technology. Her research interests include terrestrial-satellite networks, software defined networks, network functions virtualization, and intelligent networking.



YUAN FENG received the B.S. and Ph.D. degrees from the Beijing Institute of Technology (BIT), Beijing, China, in 2003 and 2011, respectively. He is currently an Associate Research Fellow with the China Research and Development Academy of Machinery Equipment. His research interests include signal processing in wireless communication networks and system engineering.



**ZHEN QIN** received the B.S. degree in information and communication engineering from the Beijing Institute of Technology (BIT), in 2017, where he is currently pursuing the Ph.D. degree in information and communication engineering. His current research interests include terahertz high speed communication systems and digital signal processing algorithms.



YUANJING QI received the B.S. degree in communication engineering from Shandong University, Jinan, China, in 2018, and the M.S. degree from the Beijing Institute of Technology (BIT), Beijing, China, in 2021, where he is currently pursuing the Ph.D. degree with the School of Information and Electronics. His research interest includes the design and implementation of digital communication receivers.



DONGXUAN HE received the B.S. degree in automation and the Ph.D. degree in information and communication systems from the Beijing Institute of Technology (BIT), in 2013 and 2019, respectively. From 2017 to 2018, he was a Visiting Student with the Singapore University of Technology and Design (SUTD). From 2019 to 2022, he was a Postdoctoral Researcher with the Department of Electronic Engineering, Tsinghua University. He is currently an Assistant Professor with the

School of Information and Electronics, BIT. His current research interests include terahertz communication, AI empowered wireless communications, and physical layer security. He was an Exemplary Reviewer of IEEE WIRELESS COMMUNICATIONS LETTERS.