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# **Mixed Coded RF/FSO EH-Based Communication System Subject to Multiuser Interference and Residual Hardware Impairments**

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**ABSTRACT** To increase spectral and power efficiencies, network coverage, and reduce outage probability, this study investigated the end-to-end performance of a coded dual-hop RF/FSO wireless communication system that operates across both Nakagami-m fading and Malaga- $\mathcal{M}$  atmospheric turbulence channels and is supplied with an amplify-and-forward semi-blind energy harvesting fixed-gain relay in order to increase spectral and power efficiencies, network coverage, and outage probability. We examine the use of CSOC codes at the source and a majority logic decoding method (MLGD) at the destination. Interestingly, our goal is to obtain an average bit error probability analytically by accounting for various interferers in the first hop as well as residual hardware impairments at the relay and destination receivers. As a consequence, the decoding method used in this investigation was shown to be adequate for the SWIPT/TS-assisted RF/FSO-coded AF cooperative communication system, requiring excellent accuracy while having a low computational cost.

**INDEX TERMS** Average bit error probability, energy harvesting, Málaga- $\mathcal{M}$  channels, maximal-ratio combining, mixed RF/FSO system, majority logic decoding, Nakagami-m fading channels, convolutional self orthogonal codes, residual hardware impairments.

#### I. INTRODUCTION

Intuitive networked communication environments are provided by fifth-generation (5G) mobile technology, connecting people, things, data, applications, transportation systems, and cities. The networks should be able to handle extraordinarily large volumes of data in record time, link a very large number of devices reliably, and transfer a significant amount of data more quickly. These lofty goals pose several difficulties for 5G networks. To handle more traffic and a faster data rate, the 5G network will need to use technology that is more spectrally efficient and has a substantially wider

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range of frequencies than the 3G and four-generation (4G) systems do [1].

Free space optical (FSO) communication requires a line of sight, high bandwidth, immunity to interference from other users' signals, ease of installation, and narrow beam width, which results in high physical layer security against potential listeners trying to overhear the lawful connection. To this end, FSO communication technology is the most appropriate technology to fulfill all the aforementioned requirements for a successful rollout of 5G, according to [2].

Despite all of the above benefits, there are still several barriers that hinder FSO from being widely used. Particularly, optical signals are substantially hampered by path-loss caused by atmospheric particles and molecules scattering [3]. Then, this scattering results in photon dispersion and

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multipath fading [4]. Additionally, atmospheric turbulence and transceiver misalignment further reduce the average bit error probability's (ABEP) efficacy [5].

Importantly, it is crucial to provide an evolved strategy that combines both radio frequency (RF) and free space optical (FSO) links inside of a single platform due to the significant atmospheric limits placed upon FSO links. When the weather is clear, FSO links are often enabled to transfer the data, while RF links are employed when the atmosphere becomes less stable [6]. In this context, mixed dual-hop RF/FSO systems have drawn the interest of many study areas because they combine the robustness of RF communications in difficult situations with both the cost-effectiveness and capabilities of FSO connections [7].

On the other hand, one of the primary aims of the forthcoming wireless communication systems (WCSs) (such as 5G and beyond, internet of things (IoT) [2]) is energy harvesting (EH), which has earned widespread attention as a potential means of developing self-sustaining and energy-efficient transmissions. It was recently suggested to use EH, which would allow the relaying node to collect wireless energy from the source and use it for re-transmission, to overcome the problem of a battery's short lifespan [8]. In particular, EH is viewed as a bright solution for IoT devices because one of these devices' main limitations is the finite battery capacity. This is because IoT devices consume a lot of energy when communicating with each other, limiting the amount of time that they can operate for as long as the battery lasts [9]. However, the majority of studies that evaluated the effectiveness of dual-hop EH-based WCS, including both [10], [11], are considered to be uncoded WCS.

Another crucial component of every WCS is security. Due to the variety of technologies and the amount of equipment connected to the system, it is a challenging process to do. To this purpose, all genuine WCS should include error-correcting codes in order to enhance physical layer security and boost efficiency [12], [13], [14], [15].

#### A. RELATED WORK

Numerous publications have evaluated the usefulness of uncoded WCSs while accounting for residual hardware impairments (RHI). For example, in [16], [17], [18], [19], and [20], the authors focused on the performance of uncoded WCS in single-hop or dual-hop configurations. Actually, in [21], the performance of a dual-hop mixed RF/FSO system with co-channel interference is explored for both fixed-gain and variable-gain amplify-and-forward (AF) relaying conditions. Furthermore, the authors of [22] investigate the performance of a cooperative network of unmanned aerial vehicles (UAVs) in which a source UAV sends data to a destination via intermediate relays using a 2-time slot transmission

<sup>1</sup>Mixed coded RF/FSO EH-based communication system, in which information is communicated between two terminals (nodes) via an EH-based relay, is regarded as a promising approach for increasing spectral and power efficiencies, network coverage, and reducing outage probability in infrastructure-less networks.

scheme, half duplexed (HD) transmission mode, and decodeand-forward (DF) protocol of relaying over Rayleigh fading channels using orthogonal frequency division multiple access (OFDMA).

Moreover, uncoded mixed RF/FSO performance under the effect of co-channel interference assumed at both relay and destination nodes [23] and asymmetric RF/FSO dual-hop cognitive amplify-and-forward (AF) relay networks affected by primary network interference [24] are among the studies investigating WCS efficiency under the effect of interference.

From another front, a few research studies, including [25], [26], [27], and [28] have explored the end-to-end (e2e) performance study of coded dual-hop WCS systems. For instance, using the Monte-Carlo simulation method, the authors in [29] and [30] studied the performance of lowdensity parity check (LDPC) codes over a hybrid FSO/RF parallel WCS and the evaluation of the polar codes across a few 5G scenarios, respectively. Additionally, hybrid FSO/RF communication systems can be improved using the EXIT Chart method, switching techniques and routing protocols as mentioned in [31] and [32]. Also, as studied in [33], the hybrid FSO/RF system outperforms the individual FSO and RF systems and gives a power gain of 3dB over a distinct number of receive antennas. Finally, performance analysis in [34] shows improved performance under strong turbulence, high pointing errors, and adverse weather conditions due to the RF backup link.

As previously stated, the bulk of research investigating the coded WCS are primarily focused with the simulation technique to assess efficiency [35], [30]. Additionally, the simulation script's execution period is crucial since the system must generate and manage a huge number of random samples. In order to address this major issue, the analytical representation for the metrics must be greatly reduced in order to considerably minimise the computing time necessary for ABEP evaluation purposes. To the best of our knowledge, no one has investigated the ABEP analysis of a mixed RF/FSO AF cooperative relaying system (i) employing error correcting codes, (ii) outfitted with energy harvesting, and (iii) taking interference into account.

#### **B. MOTIVATION AND CONTRIBUTIONS**

In light of the aforementioned explanation, we evaluate in this paper the ABEP performance of a coded dual-hop amplify-and-forward based RF/FSO system which is vulnerable to interference and RHI by taking into account convolutional self-orthogonal codes (CSOC) at the source and majority logic decoding (MLGD) at the destination. This later can efficiently decode CSOC codes with a higher number of memory registers in comparison with the Viterbi decoder, which is commonly used for convolutional codes with a short constraint length since its complexity rises with the number of encoder memory registers. Pointedly, the source node *S* in the system under study interacts with the destination node *D* through a relay node *R*. This latter amplifies the coded signal



that was received from an RF fading channel and broadcasts it to D through an FSO channel. Specifically, the ABEP is presented in terms of the system and channel characteristics based on the cumulative distribution function (CDF) of the e2e signal-to-noise ratio (SNR). So, the methodology of this paper work is to first compute the end-to-end CDF of the entire uncoded transmission, for which we need to discover the distributions of SNRs of both RF and FSO connections while accounting for both scenarios of the energy harvesting process at the relay side. Then, the calculated e2e CDF is then used to produce the ABEP formulas for both uncoded and coded circumstances.

A basic description of this paper's main contributions is provided below:

- Under the assumption of EH' scenarios at the relay, Fox's H-function (FHF) is used to characterize the CDF of the e2e SNR.
- The ABEP expressions are then produced for the system under consideration's coded and uncoded scenarios.
- A significant decrease in the ABEP is produced in function of the number of antennas used at the relay, relay transmit power, the number of orthogonal equations, coding rate, RHI severity coefficient and pointing errors coefficient in order to get further insight into the performance of the proposed system.

#### C. ORGANIZATION

This article's remaining sections are organized as follows. Section II provides a description of the dual-hop system concept that is being suggested. Section III presents the e2e CDF computation in detail. For both coded and uncoded cases, Section IV presents the ABEP formulations. In Section V, the computational findings and instructive remarks are presented. Section VI, which also presents some suggestions for additional research, serves as the paper's final conclusion.

#### D. NOTATIONS

A list of the various notations used in this research is provided in Table 1.

#### **II. SYSTEM AND CHANNEL MODEL**

As shown in Fig. 1, the communication from  $S_1$  to D through R is subject to the presence of interference and RHI at the relay and destination nodes. Thus, the received signal  $r_i$  $\{r_{i,k}\}_{1 \le k \le N_c}$  at the *i*th antenna of *R* during  $(1 - \varepsilon)T_1$  seconds is expressed as

$$r_{i,k} = \sqrt{L_1 P_{S_1}} h_{i,k}^{(S_1 R)} x_k^{(1)} + \sum_{l=2}^{N_s} \sqrt{L_l P_{S_l}} h_{i,k}^{(S_l R)} x_k^{(l)} + v_{i,k}^{(R_r)} + n_{i,k}; i = 1, \dots, N_R,$$
(1)

•  $L_l = G_{S_l}G_R \left(\frac{c}{4\pi d_0 f_l}\right)^2 \left(\frac{d_0}{d_{R_l}}\right)^{\delta}$ ;  $l = 1, ..., N_s$ , where  $G_{S_l}$ and  $G_R$  are S and R's antennas gains,  $d_0$  a reference distance,  $d_{R_l}$  denote the distance of the links  $S_l - R$ ,

c is the speed of light,  $f_l$  is the operating frequency, and  $\delta$  is the path loss exponent,

- $v_{i,k}^{(R_r)}$  is the additive noise due to hardware impairment at R, with the variance  $\sigma_{v_{R_r}}^2 = R_c L_1 P_{S_1} (h_{i,k}^{(S_1R)})^2 \kappa_{v_{R_r}}^2$ , •  $n_{i,k}$  is AWGN vector with zero-mean and variance
- $N = \sigma^2$ .  $h_{i,k}^{(S_i,R)}$  as the complex fading coefficient vectors corre-
- sponding to the  $S_l R$  links, assumed independent and non-identically distributed (i.n.i.d) Nakagami-m random variables (RVs).
- $N_R$  denotes the number of antennas at R,
- $x^{(l)} = \{x_k^{(l)}\}_{1 \le k \le N_c, 1 \le l \le N_s}$  as the modulated sequence, represented in the case of binary phase shift keying (BPSK) modulation as  $x^{(l)} = 2c^{(l)} 1$ ,
- N<sub>c</sub> as the CSOC codeword length,
  c<sup>(l)</sup> = {c<sub>k</sub><sup>(l)</sup>}<sub>1≤k≤N<sub>c</sub>,1≤l≤N<sub>s</sub></sub> as the encoded data corresponding to the information sequence d<sup>(l)</sup>,

Consequently, the corresponding instantaneous SINR of the  $S_1 - R$  hop can be expressed as

$$\gamma_{i,k}^{(S_1R)} = \frac{\gamma_{i,k}^{(1)}}{\sum_{l=2}^{N_s} \gamma_{i,k}^{(l)} + \gamma_{i,k}^{(1)} \kappa_{v_{Rr}}^2 + 1},$$
 (2)

where

$$\gamma_{i,k}^{(l)} = \frac{R_c L_l P_{S_l}}{N} \left| h_{i,k}^{(S_l R)} \right|^2, \tag{3}$$

being the instantaneous SNR for the ideal hardware scenario.

#### A. SNR OF S<sub>1</sub>-R HOP

The received signals from  $S_1$  are combined at the relay node using the MRC diversity combiner's  $N_R$  antennas. The overall SNR at the combiner's output can be evaluated as

$$\gamma_{S_1R} = \sum_{i=1}^{N_R} \gamma_i^{(S_1R)}.$$
 (4)

For the sake of clarity, the index k will be removed in the variables in what follows. Specifically,  $\gamma_{i,k}^{(S_1R)} = \gamma_i^{(S_1R)}$ . The PDF/CDF of  $\gamma_{S_1R}$  can be tightly approximated by [36]

$$f_{\gamma S_1 R}(x) \approx a_1 G_{1,2}^{2,0} \left[ \frac{x}{a_2} \middle| \begin{array}{c} -; a_3 \\ a_4, a_5 \end{array} \right],$$
 (5)

$$F_{\gamma_{S_1R}}(x) \approx a_1 x G_{2,3}^{2,1} \left[ \frac{x}{a_2} \middle| \begin{array}{c} 0; a_3 \\ a_4, a_5; -1 \end{array} \right],$$
 (6)

where

$$a_{1} = \frac{\Gamma(a_{3} + 1)}{a_{2}\Gamma(a_{4} + 1)\Gamma(a_{5} + 1)},$$

$$a_{3} = \frac{4\varphi_{4} - 9\varphi_{3} + 6\varphi_{2} - \mu_{1}}{-\varphi_{4} + 3\varphi_{3} - 3\varphi_{2} + \mu_{1}},$$
(8)

$$a_3 = \frac{4\varphi_4 - 9\varphi_3 + 6\varphi_2 - \mu_1}{-\varphi_4 + 3\varphi_3 - 3\varphi_2 + \mu_1},\tag{8}$$

$$a_2 = \frac{a_3}{2} \left( \varphi_4 - 2\varphi_3 + \varphi_2 \right) + 2\varphi_4 - 3\varphi_3 + \varphi_2, \tag{9}$$

$$a_4 = \frac{\bar{a_6} + a_7}{2},\tag{10}$$

$$a_5 = \frac{a_6 - a_7}{2},\tag{11}$$



**TABLE 1.** List of functions and symbols.

Symbol	Meaning	Symbol	Meaning
$\overline{r}$	Detection type	ε	Harvester efficiency
$\overline{N_I}$	Source information length	$T_1, T_2$	First and second communication time
$\overline{N_c}$	Coded signal length	$P_{S_l}$	$S_l$ power
$\delta$	Free space path-loss coefficient	$G_0$	Relay amplification gain
$\phantom{aaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaa$	Power conversion efficiency	$F_{X}\left( .\right)$	CDF of the RV X
$\overline{N_R}$	Number of antennas	$f_{X}\left( .\right)$	PDF of X
$\overline{}$	Path-loss parameter	.	Absolute value
$\overline{d_{min}}$	Minimum distance	$\gamma_{inc}(.)$	Lower incomplete Gamma function
$\overline{B_R}$	Battery capacity	E[.]	Expectation operator
$-\xi$	Pointing error parameter	$\Gamma(.)$	Gamma function
$\alpha, \beta$	Málaga-ℳ fading parameters	$G_{:,:}[. :]$	Meijer's G-function
$\overline{n_c}$	CSOC encoder output bits	$H_{\cdots}$ $[. :]$	Bivariate FHF
$\overline{K_i}$	Degree of a generator polynomial of a CSOC code	$E_R$	Harvested Energy
$\overline{R_c}$	Coding rate	$P_R$	Harvested power
$\overline{T}$	MLGD decoder correction capability	J	Number of orthogonal parity check-sums
$\overline{m_c}$	CSOC encoder memory order	$m_i^{(l)}, \Omega_i^{(l)}$	Nakagami-m parameters
$\kappa_{v_{R_r}}$	RHI severity coefficient at $R$	$\kappa_{v_{D_r}}$	RHI severity coefficient at D
$G_{S_l}$	Source gain	$d_{R_l}$	$S_l - R$ distance
$\overline{G_R}$	Relay gain	$\gamma_{S_1R}, \gamma_{RD}^{(\ell)}$	SNRs of the first and second hop, respectively
$\overline{c}$	Speed of light	$\gamma_{eq}$	System's e2e SNR
$\overline{d_0}$	Reference distance	$f_l$	The operating frequency
$\overline{N_s}$	Number of interference sources		

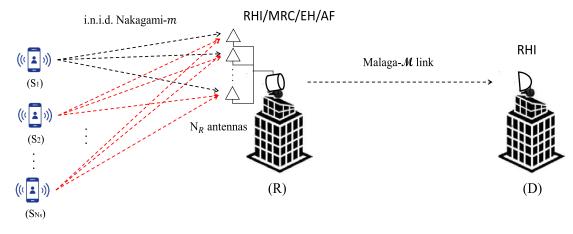


FIGURE 1. Communication system model.

$$a_{6} = \frac{a_{3} (\varphi_{2} - \mu_{1}) + 2\varphi_{2} - \mu_{1}}{a_{2}} - 3,$$

$$a_{7} = \sqrt{\left(\frac{a_{3} (\varphi_{2} - \mu_{1}) + 2\varphi_{2} - \mu_{1}}{a_{2}} - 1\right)^{2} - 4\frac{\mu_{1} (a_{3} + 1)}{a_{2}}},$$

$$(12)$$

and

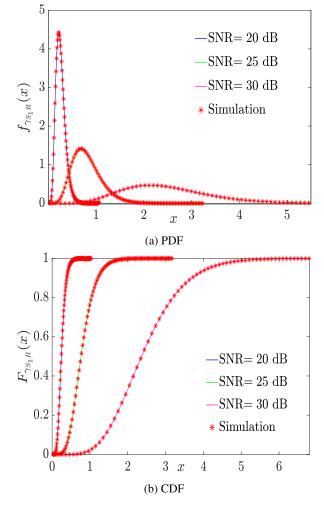
$$\varphi_i = \frac{\mu_i}{\mu_{i-1}}, i \ge 1,\tag{14}$$

where  $\mu_i$  is the *i*th moment of the RV  $\gamma_{S_1R}$ , and  $\Gamma$  (.) represents the Gamma function. Fig. 2 depicts the simulated and approximated PDF in (5) for different values of SNR.

# B. SNR OF R-D HOP

Considering time switching (TS) protocol of EH, the energy harvested from the source  $S_1$  and the interferers  $S_2, \ldots, S_{N_s}$  during  $\varepsilon T_1$  seconds is given by

$$E_{R} = \theta \varepsilon T_{1} \sum_{l=1}^{N_{s}} L_{l} P_{S_{l}} \sum_{i=1}^{N_{R}} \left| h_{i,k}^{(S_{l}R)} \right|^{2},$$
 (15)



**FIGURE 2.** Approximated and simulated PDF/CDF of the sum of  $\gamma_{S_1R}$ .

where  $0 < \varepsilon < 1$  and  $\theta$  denoting the conversion efficiency of the energy harvester at the relay.

Throughout the second communication time  $T_2$ , the relay will use  $E_R$  to convey the signal to D. Given that the amount of energy gathered may be less or greater than the battery's capacity  $B_R$ . The transmit power is provided by  $P_R = P_B = B_R/T_2$  if  $E_R \geq B_R$ , and  $P_R = P_E = E_R/T_2$  otherwise. The PDF/CDF of  $P_E$  when  $E_R < B_R$  can be accurately approximated by [37]

$$f_{P_R}(z) \approx \Psi^{m_I} \frac{z^{m_I - 1}}{\Gamma(m_I)} \exp\left(-\Psi z\right),$$
 (16)

$$F_{P_R}(z) \approx \frac{\gamma_{inc}(m_I, \Psi z)}{\Gamma(m_I)},$$
 (17)

where  $\gamma_{inc}(.)$  represents lower incomplete Gamma function [38],

$$\Psi = \frac{\mathbb{E}[P_R]}{\mathbb{E}[P_R^2] - \mathbb{E}^2[P_R]},\tag{18}$$

$$m_I = \frac{\mathbb{E}^2[P_R]}{\mathbb{E}[P_R^2] - \mathbb{E}^2[P_R]},$$
 (19)

$$\mathbb{E}[P_R] = \theta \varepsilon \frac{T_1}{T_2} \sum_{l=1}^{N_s} L_l P_{S_l} \sum_{i=1}^{N_R} \Omega_i^{(l)}, \tag{20}$$

and  $\mathbb{E}[P_R^2]$  is written as in (21), shown at the bottom of the page, with  $(l, i) \neq (l_0, i_0)$ .

At D, the received information signal from R considering both heterodyne and IM/DD detection techniques can be written as

$$r_k^{(d)} = G_0 \sqrt{P_R} \left( \sqrt{\eta h_k^{(d)}} \right)^r r_k + v_k^{(D_r)} + n_k^{(d)},$$
 (22)

where

- $\sigma_{v_{D_r}}^2 = G_0^2 \left( \eta h_k^{(d)} \right)^r P_R \kappa_{v_{D_r}}^2$ , as the variance of the additive noise  $v_k^{(D_r)}$  due to hardware impairments at D,
- $\eta$  denotes the photo-detector efficiency,
- $\{r_k\}_{1 \le k \le N_c}$  as the MRC combiner's output vector,
- $\{h_k^{(d)}\}_{1 \le k \le N_c}$  as the Málaga- $\mathcal{M}$  distributed light irradiance vector with the presence of pointing errors  $\xi$  [39], [40],
- $\{n_k^{(d)}\}_{1 \le k \le N_c}$  as AWGN vector with zero-mean and variance  $N_2$ .
- r represents the detection technique category (either IM/DD or heterodyne detection) and
- $G_0^2 = \frac{\mathbb{E}[P_R]}{NC}$  represents the fixed-gain semi-blind relaying where  $C = \overline{\gamma}_{S_1R} + 1$  [41].

The corresponding SNR of the R-D link can be obtained from (22) as

$$\gamma_{RD} = \frac{\gamma_{RD}^{(id)}}{\gamma_{RD}^{(id)} \kappa_{\nu_{D_r}}^2 + 1},\tag{23}$$

where

$$\gamma_{RD}^{(id)} = P_R \gamma_2 
= \frac{P_R \left( \eta h_k^{(d)} \right)^r}{N_r}.$$
(24)

By using (15), one obtains

$$\overline{\gamma}_{RD}^{(id)} = \begin{cases} \frac{m_I}{\Psi} \mu_r, E_R < B_R \\ P_B \mu_r, E_R \ge B_R, \end{cases}$$
 (25)

$$\mathbb{E}[P_R^2] = \left(\theta \varepsilon \frac{T_1}{T_2}\right)^2 \left(\sum_{l=1}^{N_s} \sum_{i=1}^{N_R} \left(L_l P_{S_l}\right)^2 (m_i^{(l)} + 1) \Omega_i^{(l)} + \sum_{l=1}^{N_s} \sum_{i=1}^{N_R} L_l P_{S_l} \Omega_i^{(l)} \sum_{l_0=1}^{N_s} \sum_{i_0=1}^{N_R} L_{l_0} P_{S_{l_0}} \Omega_{i_0}^{(l_0)}\right),\tag{21}$$

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where

$$\mu_r = \begin{cases} \overline{\gamma}, r = 1\\ \frac{(\xi^2 + 2)(\xi^2 + 1)^{-2} \xi^2 (\Omega' + g)^2}{(\alpha + 1)\alpha^{-1} [\Omega'^2 (1 + \beta^{-1}) + 4\Omega' g + 2g^2]} \overline{\gamma}, r = 2, \end{cases}$$
(26)

To characterize the statistical distribution of  $\gamma_{RD}$ , the distributions of RVs  $P_R = P_E$  and  $\gamma_2$  are required. The PDF for  $\gamma_2$  is given as follows [42]

$$f_{\gamma_2}(\gamma_2) = \frac{\xi^2 A}{2r\gamma_2} \sum_{m_1=1}^{\beta} b_{m_1} G_{1,3}^{3,0} \left[ B \left( \frac{\gamma_2}{\mu_r} \right)^{\frac{1}{r}} \middle| \begin{array}{c} \xi^2 + 1 \\ \xi^2, \alpha, m_1 \end{array} \right],$$
(27)

while the PDF of  $P_R$  is being represented in (16).

Remark 1: It is worth mentioning that for the case of ideal hardware impairments, we have  $\kappa_{v_{R_r}}^2 = \kappa_{v_{D_r}}^2 = 0$ .

#### C. CSOC CODES AND MLGD DECODER

The coding method for a CSOC code with the coding rate  $R_c = (n_c - 1)/n_c$  entails creating a parity symbol for each instant that corresponds to  $(n_c - 1)$  information bits.

Essentially, the minimum distance  $d_{min} = J + 1$  and a group of J equations describe these CSOC codes. Such codes are identified by the coding rate  $R_c$  and memory order  $m_c$  respectively, which are supplied by the formulas  $R_c =$  $(n_c-1)/n_c$  and  $m_c=\max_{1\leq i\leq n_c-1}K_i$ , where  $K_i$  stands for the *i*th generator polynomial. Importantly, the input and output sequence lengths are indicated by  $N_I \ge m_c + 1$  and  $N_c =$  $n_c(N_I + m_c)$ , respectively. We denote the CSOC code using the syntax  $CSOC(n_c, n_c - 1, m_c)$  for simplicity, [43], [44].

CSOC's MLGD decoding technique is what's known as an algebraic process. For the following reasons, this decoding method is different from Viterbi and sequential ones. Decoding techniques for Viterbi or sequential decoding are based on probabilistic, not algebraic, considerations. Furthermore, unlike Viterbi and sequential decoding methods, threshold decoding generates a final decision on the current information bit by simply taking into account the received coded symbols over a length  $(m_c + 1)$ , instead of considering the entire sequence of received coded symbols, [43], [44].

As a result, when D received the signal  $r^{(d)}$ , the MLGD decision is computed using straightforward logical operations with a correction capacity of  $T = (d_{min} - 1)/2$  bits based on the set of J equations which are orthogonal each instant on the symbol under decoding [45].

Remark 2:

• The studied MLGD decoder can adequately decode CSOC codes [46], in contrast to other decoding techniques as the Viterbi decoder, which is usually employed for convolutional codes with a low constraint length as its complexity grows with the memory order. Interestingly, the strong resistance to the encoded information that  $m_c$  may offer is its primary advantage; hence, the higher the m<sub>c</sub>, the larger the coding gain and, consequently, the lower is the ABEP.

• Additionally, it is important to note that the greater the decoder's capacity to repair errant bits T is, the higher the number of orthogonal equations A and minimum distance, and consequently, Â the more secure the transmission.

#### **III. STATISTICAL PROPERTIES**

The analytical expressions for the PDF/CDF of the second hop's SNR and the CDF of the e2e SNR in the abovementioned  $P_R$  cases are given in this section.

Given that the relay R employs a fixed-gain AF relaying mechanism, the e2e SNR received at D is represented as [41]

$$\gamma_{eq}^{(\ell)} = \frac{\gamma_{S_1 R} \gamma_{RD}^{(\ell)}}{\gamma_{RD}^{(\ell)} + C}, \ell = 1, 2, \tag{28}$$

where  $\ell = 1$  for the case of  $E_R < B_R$  and  $\ell = 2$  for  $E_R \ge$  $B_R$ . By considering the two possible scenarios  $E_R < B_R$  and  $E_R \ge B_R$ , the CDF of  $\gamma_{eq}$  may be derived as [42]

$$F_{\gamma_{eq}}(z) = F_{\gamma_{eq}^{(1)}}(z) \operatorname{Pr} \left( P_R < \frac{B_R}{T_2} \right)$$

$$+ F_{\gamma_{eq}^{(2)}}(z) \operatorname{Pr} \left( P_R \ge \frac{B_R}{T_2} \right)$$

$$= \mathcal{D}F_{\gamma_{eq}^{(1)}}(z) + (1 - \mathcal{D}) F_{\gamma_{eq}^{(2)}}(z), \qquad (29)$$

using and [47, Eq. 06.06.26.0004.01] as

$$\mathcal{D} = \frac{1}{\Gamma(m_I)} G_{1,2}^{1,1} \left[ \Psi \frac{B_R}{T_2} \middle| \begin{array}{c} 1 \\ m_I, 0 \end{array} \right]. \tag{30}$$

In order to obtain the CDF expression of  $\gamma_{eq}$ , we have to compute first the SNR's PDF of the R-D hop under the two circumstances of  $E_R$  stated in Section II.

Remark 3: It is worth noting from (28), that when  $\gamma_{RD}^{(\ell)}$ tends to infinity, the e2e SNR  $\gamma_{eq} \approx \gamma_{S_1R}$ . As a result, at a fixed value of  $\overline{\gamma}_{S_1R}$ , the system's ABEP performance stabilizes.

A. PDF OF 
$$\gamma_{RD}^{(id)}$$

So, to compute the PDF of  $\gamma_{RD}^{(id)}$ , we have two cases:

1) FIRST CASE  $E_R < B_R$   $\gamma_{RD_1}^{(id)}$  is the product of two RVs  $P_R$  and  $\gamma_2$ . Thus the PDF of  $\gamma_{RD_1}^{(id)}$  is obtained as

$$f_{\gamma_{RD_1}^{(id)}}(z) = \int_0^\infty \frac{1}{x} f_{P_R}\left(\frac{z}{x}\right) f_{\gamma_2}(x) dx.$$
 (31)

Proposition 1: The PDF of  $\gamma_{RD_1}^{(id)}$  can be expressed as

$$f_{\gamma_{RD_1}^{(id)}}(z) = \frac{Q_1}{z} \sum_{m_1=1}^{\beta} b_{m_1} r^{\alpha+m_1-2} \times G_{1,2r+2}^{2r+2,0} \left[ \mathcal{B}_1 z \middle| \frac{\xi^2}{\kappa_1} + 1 \right], \tag{32}$$



where 
$$\kappa_1 = \frac{\xi^2}{r}, \frac{\alpha}{r}, \dots, \frac{\alpha+r-1}{r}, \frac{m_1}{r}, \dots, \frac{m_1+r-1}{r}, m_I + 1.$$

$$\mathcal{B}_1 = \frac{B^r \Psi}{r^{2r} \mu_r}.$$
(33)

and

$$Q_1 = \frac{\xi^2 A}{2\Gamma(m_I)(2\pi)^{r-1}}.$$
 (34)

*Proof:* The proof is presented in Appendix A.

# 2) SECOND CASE $E_R \ge B_R$

 $\gamma_{RD_2}^{(id)}$  is the RV  $\gamma_2$  scaled by the constant  $P_B$ . Hence the PDF of  $\gamma_{RD_2}^{(id)}$  is expressed as

$$f_{\gamma_{RD_2}^{(2)}}(z) = \frac{1}{P_B} f_{\gamma_2} \left(\frac{z}{P_B}\right).$$
 (35)

Substituting (27) into (35), one gets

$$f_{\gamma_{RD_2}^{(id)}}(z) = \frac{Q_2}{z} \sum_{m_1=1}^{\beta} b_{m_1} G_{1,3}^{3,0} \left[ B\left(\frac{z}{P_B \mu_r}\right)^{\frac{1}{r}} \middle| \begin{array}{c} \xi^2 + 1\\ \xi^2, \alpha, m_1 \end{array} \right],$$
(36)

where

$$Q_2 = \frac{\xi^2 A}{2r}.\tag{37}$$

# B. CDF OF $\gamma_{RD}^{(id)}$

Proposition 2: The CDF of  $\gamma_{RD}^{(id)}$  for the both cases  $E_R < B_R$  and  $E_R \ge B_R$  is represented respectively as

$$F_{\gamma_{RD_1}^{(id)}}(z) = \mathcal{Q}_1 \sum_{m_1=1}^{\beta} b_{m_1} r^{\alpha+m_1-2} G_{2,2r+3}^{2r+2,1} \left[ \mathcal{B}_1 x \middle| 1, \frac{\xi^2}{r} + 1 \right].$$
(38)

and

$$F_{\gamma_{RD_2}^{(id)}}(z) = \mathcal{Q}_2 r \sum_{m_1=1}^{\beta} b_{m_1} G_{2,4}^{3,1} \left[ \mathcal{B}_2 z^{\frac{1}{r}} \middle| \begin{array}{c} 1, \xi^2 + 1 \\ \xi^2, \alpha, m_1, 0 \end{array} \right]. \quad (39)$$

where

$$\mathcal{B}_2 = B \left( \frac{1}{P_B \mu_r} \right)^{\frac{1}{r}}. \tag{40}$$

*Proof:* The proof is presented in Appendix B.

#### C. CDF OF $\gamma_{RD}$

One can easily deduce the CDF of  $\gamma_{RD}$  from the previous subsection as

$$F_{\gamma_{RD}^{(\ell)}}(z) = \begin{cases} F_{\gamma_{RD_{\ell}}^{(id)}}(z) \left(\frac{z}{1 - z\kappa_{\nu_{D_r}}^2}\right); & z < \frac{1}{\kappa_{\nu_{D_r}}^2} \\ 1; & z \ge \frac{1}{\kappa_{\nu_{D_r}}^2} \end{cases}$$
(41)

Hence

1) FIRST CASE  $E_R < B_R$ 

$$F_{\gamma_{RD}^{(1)}}(z) = \mathcal{Q}_1 \sum_{m_1=1}^{\beta} b_{m_1} r^{\alpha+m_1-2} \times G_{2,2r+3}^{2r+2,1} \left[ \mathcal{B}_1 \frac{z}{(1-z\kappa_{\nu_{D_r}}^2)} \middle| 1, \frac{\xi^2}{r} + 1 \right]. \tag{42}$$

2) SECOND CASE  $E_R \ge B_R$ 

$$F_{\gamma_{RD}^{(2)}}(z) = Q_2 r \sum_{m_1=1}^{\beta} b_{m_1} \times G_{2,4}^{3,1} \left[ \mathcal{B}_2 \left( \frac{z}{(1 - z \kappa_{\nu_{D_r}}^2)} \right)^{\frac{1}{r}} \middle| \begin{array}{c} 1, \xi^2 + 1 \\ \xi^2, \alpha, m_1, 0 \end{array} \right].$$
(43)

#### D. PDF OF $\gamma_{RD}$

The PDF of  $\gamma_{RD}$  is computed as follows

$$f_{\gamma_{RD}^{(\ell)}}(z) = \frac{1}{(1 - z\kappa_{\nu_{D_r}}^2)^2} \frac{\partial F_{\gamma_{RD}^{(id)}}\left(\frac{z}{(1 - z\kappa_{\nu_{D_r}}^2)}\right)}{\partial z}; z < \frac{1}{\kappa_{\nu_{D_r}}^2}$$
(44)

Hence, one obtains

1) FIRST CASE  $E_R < B_R$ 

$$f_{\gamma_{RD}^{(1)}}(z) = \mathcal{Q}_1 \sum_{m_1=1}^{\beta} b_{m_1} r^{\alpha+m_1-2} \frac{1}{z(1-z\kappa_{\nu_{D_r}}^2)} \times G_{1,2r+2}^{2r+2,0} \left[ \mathcal{B}_1 \frac{z}{(1-z\kappa_{\nu_{D_r}}^2)} \middle| \frac{\xi^2}{r} + 1 \right].$$
 (45)

2) SECOND CASE  $E_R \ge B_R$ 

$$f_{\gamma_{RD}^{(2)}}(z) = \frac{1}{z(1 - z\kappa_{\nu_{D_r}}^2)} \mathcal{Q}_2 \sum_{m_1 = 1}^{\beta} b_{m_1} \times G_{1,3}^{3,0} \left[ \mathcal{B}_2 \left( \frac{z}{(1 - z\kappa_{\nu_{D_r}}^2)} \right)^{\frac{1}{r}} \middle|_{\xi^2, \alpha, m_1, -}^{-, \xi^2 + 1} \right].$$
(46)

# E. CDF OF THE e2e SNR

The CDF of  $\gamma_{eq}^{(\ell)}$  can be straightforwardly obtained using (28) as

$$F_{\gamma_{eq}^{(\ell)}}(z) = \int_0^\infty F_{\gamma_{SR}}\left(z\left(1 + \frac{C}{x}\right)\right) f_{\gamma_{RD}^{(\ell)}}(x) dx. \tag{47}$$

#### 1) FIRST SCENARIO

Proposition 3: The e2e SNR's CDF for the first scenario (i.e.,  $E_R < B_R$ ) can be approximated by (48), as shown at the bottom of the next page.

*Proof: The proof is presented in Appendix C.* 



# 2) SECOND SCENARIO

Proposition 4: The e2e SNR's CDF for the second scenario (i.e.,  $E_R \ge B_R$ ) can be approximated by (49), as shown at the next page.

*Proof:* The proof is presented in Appendix A.

#### **IV. ABEP ANALYSIS**

#### A. UNCODED COMMUNICATION (UC)

#### 1) EXACT ANALYSIS

When no error-correcting code is used in the system, the ABEP can be evaluated as [48]

$$P_b^{(u)} = \frac{1}{2\mathcal{A}_1} \int_0^\infty \exp(-q\gamma) \gamma^{p-1} F_{\gamma_{eq}}(\gamma) d\gamma, \qquad (50)$$

where p and q are two modulation-dependent parameters and

$$A_1 = \frac{\Gamma(p)}{a^p}. (51)$$

The ABEP in (50) can be formulated as

$$P_b^{(u)} = \frac{\mathcal{D}P_{b,1} + (1-\mathcal{D})P_{b,2}}{2\mathcal{A}_1},\tag{52}$$

where  $P_{b,1}$  and  $P_{b,2}$  are evaluated in the next subsections.

#### First Scenario

Proposition 5:  $P_{b,1}$  can be tightly approximated by (53), as shown at the next page.

*Proof:* The proof is presented in Appendix E.

#### · Second Scenario

*Proposition 6:*  $P_{b,2}$  can be tightly approximated by (54), as shown at the next page.

*Proof:* The proof is presented in Appendix E.

#### 2) ASYMPTOTIC ANALYSIS

Proposition 7: In the high SNR regime (i.e.,  $P_s/N \to \infty$ ), the uncoded system's ABEP can be asymptotically expressed as in (55) and (56), shown at the next page, for the first and second scenario of EH, respectively, where  $z = \frac{1}{qa_2} \to 0$  and

$$\Omega^{(1)}$$

$$= \frac{\Gamma(-a_4 + a_5)\Gamma(p + a_4)}{(1 + a_4)\Gamma(-a_4 + a_3)\Gamma(-a_4)}\Gamma(-s_2 - a_4 + 1 + k),$$
(57)

$$\Omega^{(2)} = \frac{\Gamma(-a_5 + a_4)\Gamma(p + a_5)}{(1 + a_5)\Gamma(-a_5 + a_3)\Gamma(-a_5)} \Gamma(-s_2 - a_5 + 1 + k),$$
(58)

$$\Omega^{(3)} = \frac{\Gamma(s_2 - 1 - k + a_4)\Gamma(s_2 - 1 - k + a_5)\Gamma(p - s_2 + 1 + k)}{(2 - s_2 + k)\Gamma(s_2 - 1 - k + a_3)\Gamma(s_2 + 1 + k)},$$
(59)

$$p_0 = \arg\min_{j \le 3} \xi_j, \tag{60}$$

$$\Omega_1^{(1)} = \Omega^{(1)} \Gamma \left( -a_4 \right), \tag{61}$$

$$\Omega_1^{(2)} = \Omega^{(2)} \Gamma(-a_5),$$
(62)

$$= \arg\min_{j \le 2} \xi_j, \tag{63}$$

$$\Omega_2^{(1)} = \frac{\Gamma(-a_4 + a_5)\Gamma(p + a_4)}{(1 + a_4)\Gamma(-a_4 + a_3)\Gamma(-a_4)} \Gamma\left(-\frac{s_3}{r} - a_4 + 1 + k_2\right),$$
(64)

$$\Omega_2^{(2)} = \frac{\Gamma(-a_5 + a_4)\Gamma(p + a_5)}{(1 + a_5)\Gamma(-a_5 + a_3)\Gamma(-a_5)} \Gamma\left(-\frac{s_3}{r} - a_5 + 1 + k_2\right),$$
(65)

$$\Omega_2^{(3)} = \frac{\Gamma(\frac{s_3}{r} - 1 - k_2 + a_4)\Gamma(\frac{s_3}{r} - 1 - k_2 + a_5)}{(2 - \frac{s_3}{r} + k_2)\Gamma(\frac{s_3}{r} - 1 - k_2 + a_3)\Gamma(\frac{s_3}{r} + 1 + k_2)} \times \Gamma(p - \frac{s_3}{r} + 1 + k_2),$$
(66)

$$P2 = \arg\min_{j \le 3} \xi_j', \tag{67}$$

$$p_3 = \arg\min_{j \le 2} \xi_j', \tag{68}$$

$$F_{\gamma_{eq}^{(1)}}(z) \approx Ca_{1}Q_{1} \sum_{m_{1}=1}^{\beta} b_{m_{1}} r^{\alpha+m_{1}-2} \sum_{k=0}^{\infty} \frac{(-1)^{k}}{k!} \left(C\kappa_{\nu_{D_{r}}}^{2}\right)^{k}$$

$$\times H_{1,0;3,3;2,2r+4}^{0,1;2,1;2r+4,0} \left[\frac{z}{a_{2}}, C\mathcal{B}_{1} \middle| \frac{(-k,-1,1):(0,1);(a_{3},1),(0,1):\left(\frac{\xi^{2}}{r}+1,1\right),(-k,1)}{-:(a_{4},1),(a_{5},1);(-1,1):(\kappa_{1},1),(0,1),(-1-k,1)} \right]$$

$$+ \frac{a_{1}Q_{1}}{\kappa_{\nu_{D_{r}}}^{2}} \sum_{m_{1}=1}^{\beta} b_{m_{1}} r^{\alpha+m_{1}-2} G_{2,3}^{2,1} \left[\frac{z}{a_{2}} \middle| \frac{0;a_{3}}{a_{4},a_{5};-1} \right] G_{2,2r+3}^{2r+3,1} \left[\frac{\mathcal{B}_{1}}{\kappa_{\nu_{D_{r}}}^{2}} \middle| 0;\frac{\xi^{2}}{r}+1\right].$$

$$(48)$$



$$F_{\gamma_{eq}^{(2)}}(z) \approx Ca_{1}Q_{2} \sum_{m_{1}=1}^{\beta} b_{m_{1}} \sum_{k_{2}=0}^{\infty} \frac{(-1)^{k_{2}}}{k_{2}!} \left(C\kappa_{\nu_{D_{r}}}^{2}\right)^{k_{2}} \times H_{1,0;3,3;2,5}^{0,1;2,1;5,0} \left[\frac{z}{a_{2}}, \mathcal{B}_{2}C^{\frac{1}{r}}\right|_{-:(a_{4},1),(a_{5},1);(-1,1):(\xi^{2},1),(\alpha,1),(m_{1},1),(0,\frac{1}{r}),(-1-k,\frac{1}{r})}\right] + \frac{a_{1}Q_{2}}{\kappa_{\nu_{D_{r}}}^{2}} \sum_{m_{1}=1}^{\beta} b_{m_{1}}G_{2,3}^{2,1} \left[\frac{z}{a_{2}}\right|_{a_{4},a_{5};-1}^{0;a_{3}} H_{2,2r+3}^{2r+3,1} \left[\frac{\mathcal{B}_{2}}{\left(\kappa_{\nu_{D_{r}}}^{2}\right)^{\frac{1}{r}}}\right|_{(\xi^{2},1),(\alpha,1),(m_{1},1),(0,\frac{1}{r})}^{(0,\frac{1}{r});(\xi^{2}+1,1)}\right]. \tag{49}$$

$$P_{b,1} \approx \frac{Ca_{1}Q_{1}}{q^{p}} \sum_{m_{1}=1}^{\beta} b_{m_{1}} r^{\alpha+m_{1}-2} \sum_{k=0}^{\infty} \frac{(-1)^{k}}{k!} \left( C\kappa_{\nu D_{r}}^{2} \right)^{k}$$

$$\times H_{1,0;4,3;2,2r+4}^{0,1;2,2;2r+4,0} \left[ \frac{1}{qa_{2}}, C\mathcal{B}_{1} \middle| \frac{(-k,-1,1):(0,1),(1-p,1);(a_{3},1),(0,1):\left(\frac{\xi^{2}}{r}+1,1\right),(-k,1)}{-:(a_{4},1),(a_{5},1);(-1,1):(\kappa_{1},1),(0,1),(-1-k,1)} \right]$$

$$+ \frac{a_{1}Q_{1}}{q^{p}\kappa_{\nu D_{r}}^{2}} \sum_{m_{1}=1}^{\beta} b_{m_{1}} r^{\alpha+m_{1}-2} G_{3,3}^{2,2} \left[ \frac{1}{qa_{2}} \middle| \frac{0,1-p;a_{3}}{a_{4},a_{5};-1} \right] G_{2,2r+3}^{2r+3,1} \left[ \frac{\mathcal{B}_{1}}{\kappa_{\nu D_{r}}^{2}} \middle| 0;\frac{\xi^{2}}{r}+1 \right].$$

$$(53)$$

$$P_{b,2} \approx \frac{Ca_{1}Q_{2}}{q^{p}} \sum_{m_{1}=1}^{\beta} b_{m_{1}} \sum_{k_{2}=0}^{\infty} \frac{(-1)^{k_{2}}}{k_{2}!} \left( C\kappa_{\nu D_{r}}^{2} \right)^{k_{2}}$$

$$\times H_{1,0;4,3;2,5}^{0,1;2,2;5,0} \left[ \frac{1}{qa_{2}}, \mathcal{B}_{2}C^{\frac{1}{r}} \middle|_{-:(a_{4},1),(a_{5},1);(-1,1):(\xi^{2},1),(\alpha,1),(m_{1},1),(0,\frac{1}{r}),(-1-k,\frac{1}{r})} \right]$$

$$+ \frac{a_{1}Q_{2}}{q^{p}\kappa_{\nu D_{r}}^{2}} \sum_{m_{1}=1}^{\beta} b_{m_{1}}G_{3,3}^{2,2} \left[ \frac{1}{qa_{2}} \middle|_{a_{4},a_{5};-1}^{0,1-p;a_{3}} \right] H_{2,2r+3}^{2r+3,1} \left[ \frac{\mathcal{B}_{2}}{\left(\kappa_{\nu D_{r}}^{2}\right)^{\frac{1}{r}}} \middle|_{(\xi^{2},1),(\alpha,1),(m_{1},1),(0,\frac{1}{r})}^{0,\frac{1}{r}} \middle|_{(\xi^{2},1),(\alpha,1),(m_{1},1),(0,\frac{1}{r})}^{0,\frac{1}{r}} \right].$$

$$(54)$$

$$P_{b,1} \sim \frac{Ca_1 Q_1}{q^p} \sum_{m_1=1}^{\beta} b_{m_1} r^{\alpha+m_1-2} \sum_{k=0}^{\infty} \frac{(-1)^k}{k!} \left( C \kappa_{\nu D_r}^2 \right)^k \Omega^{(p_0)} z^{\xi_{p_0}} \frac{1}{2\pi j} \int_{\mathcal{C}_2} \mathcal{I}_2(s_2) ds_2$$

$$+ \frac{a_1 Q_1}{q^p \kappa_{\nu D_r}^2} \sum_{m_1=1}^{\beta} b_{m_1} r^{\alpha+m_1-2} \frac{1}{2\pi j} \Omega_1^{(p_1)} z^{\xi_{p_1}} \frac{1}{2\pi j} \int_{\mathcal{C}_2} \mathcal{I}_4(s_2) ds_2. \tag{55}$$

$$P_{b,2} \sim \frac{Ca_1 Q_2}{q^p} \sum_{m_1=1}^{\beta} b_{m_1} \sum_{k_2=0}^{\infty} \frac{(-1)^{k_2}}{k_2!} \left( C \kappa_{\nu_{D_r}}^2 \right)^{k_2} \Omega_2^{(p_2)} z^{\xi'_{p_2}} \frac{1}{2\pi j} \int_{\mathcal{C}_3} \mathcal{I}_5(s_3) ds_3 + \frac{a_1 Q_2}{q^p \kappa_{\nu_{D_r}}^2} \sum_{m_1=1}^{\beta} b_{m_1} \Omega_3^{(p_3)} z^{\xi'_{p_3}} \frac{1}{2\pi j} \int_{\mathcal{C}_3} \mathcal{I}_6(s_3) ds_3.$$
 (56)



$$\Omega_3^{(1)} = \Omega_2^{(1)} \Gamma(-a_4),$$
(69)

$$=\Omega_2^{(2)}\Gamma\left(-a_5\right),\tag{70}$$

with  $\xi_1 = a_4$ ,  $\xi_2 = a_5$  and  $\xi_3 = 1 - s_2 + k$ , and  $\xi_1' = a_4$ ,  $\xi_2' = a_5 + k$  $a_5$  and  $\xi_3' = 1 - \frac{s_3}{r} + k$ . *Proof:* The proof is represented in Appendix F.

#### B. CODED COMMUNICATION (CC)

Based on the system model considered in the presented work, and using the error probability expression obtained for the uncoded case, the ABEP of the suggested decoding procedure while using CSOC codes is supplied by [49]

$$P_b^{(c)} = \left(1 - P_b^{(u)}\right) \sum_{k=T+1}^J \binom{J}{k} \mathcal{X}^{(k)} + P_b^{(u)} \sum_{k=J-T}^J \binom{J}{k} \mathcal{X}^{(k)},$$
(71)

where

$$\mathcal{X}^{(k)} = \mathcal{P}^k (1 - \mathcal{P})^{J-k}, \tag{72}$$

$$T = \begin{cases} J/2; J \text{ is even} \\ \frac{J+1}{2}; J \text{ is odd} \end{cases} , \tag{73}$$

with

$$\mathcal{P} = \frac{1 - \left(1 - 2P_b^{(u)}\right)^{\sigma_0}}{2},\tag{74}$$

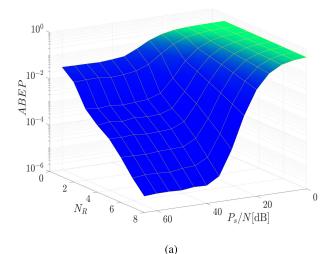
and

$$\sigma_0 = J(n-1). \tag{75}$$

# V. NUMERICAL RESULTS

This section quantitatively depicts the computed ABEP formulas for MLGD over the investigated system. Table 2 shows the default values for the system parameters used to create the numerical results. It is clear that our analytical results correspond completely with the simulation results produced using Dev C/C++ 4.9.<sup>2</sup> It is essential to note also that we primarily used 3 CSOC codes with varying coding gains,  $R_c = 1/2, 2/3$ , and 4/5, for simulation.

Fig. 3 depicts the ABEP performance of the system under study for both coded and uncoded circumstances as a function of the average SNR per symbol of the first hop for  $N_R$ ranging from 1 to 8. The ABEP decreases as the number of antenna branches increases. Also, regardless of the value of  $N_R$ , the RHI used in the system model created error floors, particularly in the uncoded scenario. For instance, the ABEP of the MLGD at SNR = 30 dB where  $N_R = 4$  is approximately  $10^{-5}$ . However, for the uncoded case, the ABEP stabilizes at  $10^{-3}$  for SNR  $\geq 30$  dB.



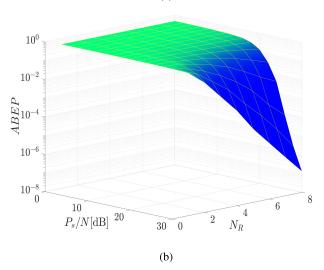


FIGURE 3. ABEP versus  $N_R$  for (a) uncoded and (b) coded communication CSOC(2,1,17).

**TABLE 2.** Simulation parameters.

Parameter	Value	Parameter	Value
ξ	6.7	$\alpha$	8
$\beta$	4	$d_0$	100 m
$\eta$	0.9	$\varepsilon$	0.7
$\overline{}$	1	$N_R$	6
$P_{S_1}$	10 w	$T_1 = T_2$	1 s
$\theta$	0.7	δ	2
$d_{R_1}$	60 m	$B_R$	500 mW
$d_{R_l}, l = 2,, N_s$	120 m	$P_{S_l}, l = 2,, N_s$	5 W
$G_{S_1}$	40 dB	$G_{S_l}, l = 2,, N_s$	10 dB
$G_R$	25 dB	$N_s$	3
$c/f_l$	28.6 mm dB	$N_I$	500 bits

In Fig. 4 (a), the ABEP performance is presented for various values of the RHI level of the destination receiver vs.  $P_s/N$ , where  $N_R = 6$ . One can plainly observe that when  $\kappa_{D_r}$  increases, the ABEP decreases substantially. Furthermore, the performance of the coded scenario utilising CSOC(5,4,26) outperforms the uncoded one, particularly in the region of small  $\kappa_{D_r}$  values.

<sup>&</sup>lt;sup>2</sup>The source codes for the simulations can be find in the following link: https://github.com/1992LAB/BER\_mixed\_CSOC\_RF\_FSO\_RHI\_ Journal2\_1/tree/545c06914e819eae9d68023db190f3e7914130de

60

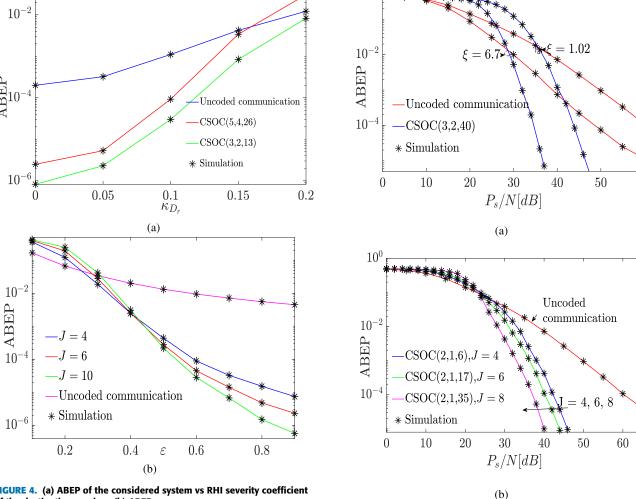


FIGURE 4. (a) ABEP of the considered system vs RHI severity coefficient of the destination receiver. (b) ABEP vs  $\varepsilon$ .

FIGURE 5. (a) ABEP performance vs pointing error parameter. (b) ABEP performance vs the number of parity check sum equations J.

Similar results are shown in Fig. 4 (b) for CSOC(3, 2, 13), CSOC(3, 2, 40) and CSOC(3, 2, 130). The ABEP is plotted in relation to the harvester efficiency  $\varepsilon$ . It is clear that when harvester efficiency improves, the ABEP decreases significantly. This indicates that when  $\varepsilon$  grows, so does the gathered power  $P_R$ , which permits the relay to deliver the information signal to D with more strength. Additionally, it is observable that there are a few points where the ABEP curves of coded and uncoded cases intersect. This problem arises mainly in the low SNRs area because of the large quantity of the recovered incorrect bits, which exceeds the decoder's correction capacity. However, after reaching a certain SNR' threshold while encountering turbulence of varying intensities, the ABEP performance of the coded system significantly increases.

For a variety of scenarios involving varying degrees of pointing error severity, the ABEP performance for the CSOC(3, 2, 40) code is displayed in Fig. 5 (a). It is worth noting that when  $\xi$  increases, the ABEP declines dramatically. It can be deduced that CSOC(3, 2, 40) earns approximately

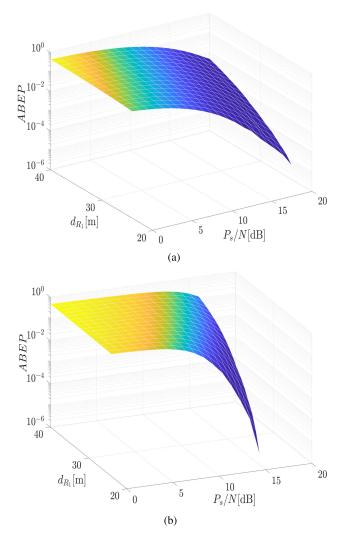
15 dB at  $10^{-4}$  when  $\xi = 1.02$ , and 13 dB when  $\xi = 6.7$  at the same ABEP.

Fig. 5 (b) depicts the ABEP evolution for certain CSOC codes by examining various values of J under IM/DD detection. Remarkably, the higher orthogonal parity check sums number J improves the ABEP, confirming **Remark. 2**. One can observe that coding improvements of approximately 16 dB, 18 dB, and 20 dB are realized for J = 4, 6 and 8, respectively.

The ABEP performance of CSOC(2, 1, 55) is displayed in Fig. 6 by changing the  $d_{R_1}$  values. Concerningly, it is noticeable that when  $d_{R_1}$  increases, the ABEP increases dramatically. This indicates that the performance of the ABEP is impacted by the nodes' distance. Therefore, the system's overall performance degrades when the distance  $d_{R_1}$ grows up.

Interestingly, it is worth noting that the curves' behavior in the previous figures is well known in the literature for



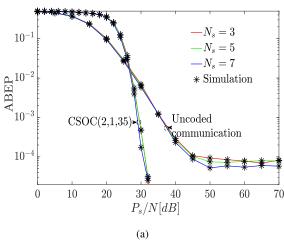


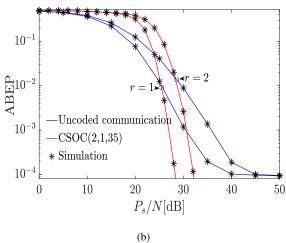
**FIGURE 6.** ABEP versus  $d_{R_1}$  for (a) uncoded and (b) coded communication CSOC(2,1,17).

coded WCS below a particular SNR threshold. In fact, this is due to the large number of erroneous bits recovered in the low SNR domain, which exceeds the decoder's capability for correction. The data is thus improperly decoded by the decoder in this SNR range. However, the number of erroneous bits rapidly drops when the SNR surpasses an SNR threshold and the coded communication performance improves.

Fig. 7 (a) depicts the ABEP performance as the number of interfering signals increases for both system model circumstances. Because we are receiving energy from the source  $S_1$  and the  $N_s - 1$  interferes, the figure shows that ABEP performance is about the same for all three  $N_s$  levels. Furthermore, error floors are significantly occurring as a result of the considered RHI at the relay and destination receivers, particularly in the uncoded situation.

The variation in ABEP for the two different kinds of detection techniques—IM/DD and heterodyne detection—is shown in Fig. 7 (b). From this figure, it is clearly seen that coherent demodulation (r=1) outperforms better than receiver systems based on direct detection (r=2).





**FIGURE 7.** (a) ABEP vs  $P_S/N$  by varying the number of interferers effecting the system. (b) ABEP of the considered system vs r.

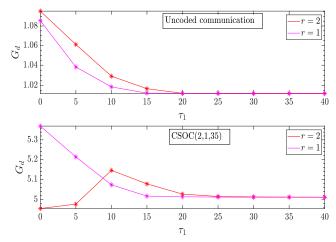


FIGURE 8. Diversity order for both heterodyne and IM/DD detection.

The diversity order of the system is depicted in Fig. 8, which was numerically assessed<sup>3</sup> and the ABEP curves of

<sup>&</sup>lt;sup>3</sup>The diversity gain was numerically evaluated using the equation:  $G_d \sim \frac{\log(P_{b_2}^{(u)}) - \log(P_{b_1}^{(u)})}{\log(\tau_1) - \log(\tau_2)}, \text{ where } \tau_i, i=1,2 \text{ are the average SNR values}.$ 



Fig. 7 (b), by adjusting the SNR  $\tau_1$  from 0 to 40 dB, while tau<sub>2</sub> remained constant. For example, the realised diversity order and coding gain of the uncoded scenario are  $G_d \approx$ 1.01 and  $G_c \approx 0.03$ , respectively, whereas  $G_d \approx 5$  and  $G_c \approx 0.0023$  for the coded case.

#### VI. CONCLUSION

In the presence of multiple interferes and RHI, the performance investigation of EH-based AF mixed coded RF/FSO dual-hop communication was examined. For both coded and uncoded cases, the analytical expression of the ABEP is derived specifically using the system's e2e CDF. Importantly, depending on how the system parameters were adjusted, the findings demonstrate that using the MLGD process for CSOC codes resulted in considerable coding improvements. Additionally, the number of relay antennas,  $S_1 - R$  distance, relay transmit power, number of orthogonal equations, RHI severity, number of interferes, and pointing error impairments all affect the system's ABEP.

One novel idea that will be looked at in future studies is the performance analysis of satellite communication adopting polar coding. In addition, it is possible to analyze the performance of an RF/FSO dual-hop coded system while non-zero boresight pointing error for the FSO connection.

#### **APPENDIX A**

#### **PROOF OF PROPOSITION 1**

When  $E_R < B_R$ , the PDF of  $\gamma_{RD_1}^{(id)}$  can be obtained by substituting (16) and (27) into (31) as

$$f_{\gamma_{RD_{1}}^{(id)}}(z) = z^{m_{I}-1} \frac{\Psi^{m_{I}}}{\Gamma(m_{I})} \frac{\xi^{2} A}{2r} \sum_{m_{1}=1}^{\beta} b_{m_{1}} \int_{0}^{\infty} x^{-m_{I}-1} \times G_{1,0}^{0,1} \left[ \frac{x}{\Psi z} \middle| \frac{1}{-} \right] G_{1,3}^{3,0} \left[ B\left(\frac{x}{\mu_{r}}\right)^{\frac{1}{r}} \middle| \frac{\xi^{2}+1}{\xi^{2},\alpha,m_{1}} \right] dx.$$

$$(76)$$

By using [47, Eq. (01.03.26.0004.01)], [50, Eq. (6.2.2)] alongside [47, Eq. (07.34.21.0013.01)], (32) is obtained.

# **APPENDIX B**

#### **PROOF OF PROPOSITION 2**

For the two cases  $E_R < B_R$  and  $E_R \ge B_R$ , the CDF of  $\gamma_{RD}^{(id)}$  is computed respectively as

A. FIRST CASE  $E_R < B_R$ 

$$F_{\gamma_{RD_1}^{(id)}}(z) = Q_1 \sum_{m_1=1}^{\beta} b_{m_1} r^{\alpha+m_1-2} \mathcal{I}_1, \tag{77}$$

where

$$\mathcal{I}_{1} = \int_{0}^{z} x^{-1} G_{1,2r+2}^{2r+2,0} \left[ \mathcal{B}_{1} x \middle| \frac{\xi^{2}}{r} + 1 \right] dx.$$
 (78)

By using [47, Eq. (07.34.21.0003.01)], we can write  $\mathcal{I}_1$  as

$$\mathcal{I}_{1} = G_{2,2r+3}^{2r+2,1} \left[ \mathcal{B}_{1} x \middle| \frac{1, \frac{\xi^{2}}{r} + 1}{\kappa_{1}, 0} \right].$$
 (79)

Hence  $F_{\gamma_{RD_1}^{(id)}}(z)$  is re-expressed as (38).

**B.** SECOND CASE  $E_R \ge B_R$ In the same manner as the first case,  $F_{\gamma_{RD_2}^{(id)}}(z)$  is expressed as

$$F_{\gamma_{RD_2}^{(id)}}(z) = \mathcal{Q}_2 \sum_{m_1=1}^{\beta} b_{m_1} \int_0^z x^{-1} \times G_{1,3}^{3,0} \left[ B \left( \frac{1}{P_B \mu_r} \right)^{\frac{1}{r}} x^{\frac{1}{r}} \middle| \frac{\xi^2 + 1}{\xi^2, \alpha, m_1} \right] dx. \quad (80)$$

By making the change of variable  $y = x^{\frac{1}{r}}$ , (80) becomes

$$F_{\gamma_{RD_2}^{(id)}}(z) = \mathcal{Q}_2 r \sum_{m_1=1}^{\beta} b_{m_1} \int_0^{z^{\frac{1}{r}}} y^{-1} \times G_{1,3}^{3,0} \left[ B \left( \frac{1}{P_B \mu_r} \right)^{\frac{1}{r}} y \middle| \begin{array}{c} \xi^2 + 1 \\ \xi^2, \alpha, m_1 \end{array} \right] dy. \quad (81)$$

Then, by using [47, Eq. (07.34.21.0003.01)], we can write  $F_{\gamma_{nn}^{(id)}}^{(2)}(z)$  as (39).

#### **APPENDIX C**

### **PROOF OF PROPOSITION 3**

By substituting (6) and (32) into (47), one obtains

$$F_{\gamma_{eq}^{(1)}}(z) \approx \int_{0}^{\frac{1}{\kappa_{\nu_{D_r}}}} F_{\gamma_{S_1R}} \left( z \left( 1 + \frac{C}{x} \right) \right) f_{\gamma_{RD}}^{(1)}(x) dx \qquad (82)$$

$$\approx a_1 \mathcal{Q}_1 \sum_{k=1}^{\beta} b_{m_1} r^{\alpha + m_1 - 2} \mathcal{I}_2(s_1, s_2), \qquad (83)$$

$$\mathcal{I}_{2}(s_{1}, s_{2}) = \int_{0}^{\frac{1}{\kappa_{\nu_{D_{r}}}}} \frac{1}{(1 - \kappa \kappa_{\nu_{D_{r}}}^{2})} \times G_{2,3}^{2,1} \left[ \left( \frac{z}{a_{2}} + \frac{z}{a_{2}} \frac{C}{x} \right) \middle| \begin{array}{c} 0; a_{3} \\ a_{4}, a_{5}; -1 \end{array} \right] \times G_{1,2r+2}^{2r+2,0} \left[ \mathcal{B}_{1} \frac{x}{(1 - \kappa \kappa_{\nu_{D_{r}}}^{2})} \middle| \begin{array}{c} \frac{\xi^{2}}{r} + 1 \\ \kappa_{1} \end{array} \right] dx. \quad (84)$$

We have (85) and (86), as shown at the bottom of the next page, hence,  $\mathcal{I}_2(s_1, s_2)$  becomes

$$\mathcal{I}_{2}(s_{1}, s_{2}) = \frac{1}{2\pi j} \int_{\mathcal{C}_{1}} \frac{\Gamma(s_{1} + a_{4})\Gamma(s_{1} + a_{5})\Gamma(1 - s_{1})}{\Gamma(s_{1} + a_{3})\Gamma(2 - s_{1})} \times \left(\frac{z}{a_{2}}\right)^{-s_{1}} \frac{1}{2\pi j} \int_{\mathcal{C}_{2}} \frac{\Gamma(s_{2} + \frac{\xi^{2}}{r})}{\Gamma(s_{2} + \frac{\xi^{2}}{r} + 1)} \mathcal{B}_{1}^{-s_{2}} \times \prod_{\ell=0}^{r-1} \Gamma\left(s_{2} + \frac{\alpha + \ell}{r}\right) \prod_{\ell=0}^{r-1} \Gamma\left(s_{2} + \frac{m_{1} + \ell}{r}\right) \times \Gamma(s_{2} + 1 + m_{1})\mathcal{I}_{3}(s_{1}, s_{2}) ds_{1} ds_{2},$$
(87)

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where

$$\mathcal{I}_{3}(s_{1}, s_{2}) = \left(\kappa_{\nu_{D_{r}}}^{2}\right)^{s_{2}-1} \int_{0}^{\frac{1}{\kappa_{\nu_{D_{r}}}^{2}}} x^{-s_{2}+s_{1}} (x+C)^{-s_{1}} \times \left(\frac{1}{\kappa_{\nu_{D_{r}}}^{2}} - x\right)^{s_{2}-1} dx.$$
(88)

By using [38, Eq. (3.197.8)], one obtains

$$\mathcal{I}_{3}(s_{1}, s_{2}) = \left(\kappa_{\nu D_{r}}^{2}\right)^{s_{2}-1} \left(\frac{1}{C\kappa_{\nu D_{r}}^{2}}\right)^{s_{1}} \frac{\Gamma(s_{2}) \Gamma(s_{1} - s_{2} + 1)}{\Gamma(s_{1} + 1)} \times {}_{2}F_{1}\left(s_{1}, s_{1} - s_{2} + 1; s_{1} + 1; -\frac{1}{C\kappa_{\nu D_{r}}^{2}}\right),$$
(89)

with  $Re(s_2 - 1) > 0$ , and  $Re(s_1 - s_2 + 1) > 0$ , where  ${}_2F_1(.;.;.)$  denotes the Gauss hypergeometric function (GHF) [38]. Now, using the Mellin-Barnes integral representation of the GHF [38, Eq. (9.113)], it yields (90), as shown at the bottom of the page. Then,  $\mathcal{I}_3(s_1, s_2)$  can be written as

$$\mathcal{I}_{3}(s_{1}, s_{2}) = \left(\kappa_{\nu_{D_{r}}}^{2}\right)^{s_{2}-1} \left(\frac{1}{C\kappa_{\nu_{D_{r}}}^{2}}\right)^{s_{1}} \frac{\Gamma(s_{2})}{\Gamma(s_{1})} \frac{1}{2\pi j} \int_{\mathcal{C}_{t}} \times \frac{\Gamma(s_{1}+t) \Gamma(s_{1}-s_{2}+1+t) \Gamma(-t)}{\Gamma(s_{1}+1+t)} \times \left(\frac{1}{C\kappa_{\nu_{D_{r}}}^{2}}\right)^{t} dt. \tag{91}$$

Hence, one gets

$$\mathcal{I}_{2}(s_{1}, s_{2}) = \frac{1}{2\pi j} \int_{\mathcal{C}_{1}} \frac{\Gamma(s_{1} + a_{4})\Gamma(s_{1} + a_{5})\Gamma(1 - s_{1})}{\Gamma(s_{1} + a_{3})\Gamma(2 - s_{1})\Gamma(s_{1})} \times \left(\frac{z}{a_{2}}\right)^{-s_{1}} \left(\frac{1}{C\kappa_{\nu_{D_{r}}}^{2}}\right)^{s_{1}} \frac{1}{2\pi j} \times \int_{\mathcal{C}_{2}} \frac{\Gamma(s_{2} + \frac{\xi^{2}}{r}) \prod_{\ell=0}^{r-1} \Gamma\left(s_{2} + \frac{\alpha+\ell}{r}\right)}{\Gamma(s_{2} + \frac{\xi^{2}}{r} + 1)}$$

$$\times \prod_{\ell=0}^{r-1} \Gamma\left(s_2 + \frac{m_1 + \ell}{r}\right) \Gamma(s_2 + 1 + m_I) \Gamma(s_2)$$

$$\times \mathcal{B}_1^{-s_2} \left(\kappa_{\nu_{D_r}}^2\right)^{s_2 - 1} \mathcal{R}_1 ds_1 ds_2, \tag{92}$$

where

$$\mathcal{R}_{1} = \frac{1}{2\pi j} \int_{\mathcal{C}_{t}} \frac{\Gamma(s_{1} + t) \Gamma(s_{1} - s_{2} + 1 + t) \Gamma(-t)}{\Gamma(s_{1} + 1 + t)} \times \left(\frac{1}{C\kappa_{\nu D_{r}}^{2}}\right)^{t} dt \\
= \frac{1}{2\pi j} \int_{\mathcal{C}_{t}} \frac{\Gamma(s_{1} - s_{2} + 1 + t) \Gamma(-t)}{s_{1} + t} \left(\frac{1}{C\kappa_{\nu D_{r}}^{2}}\right)^{t} dt. \tag{93}$$

As the conditions  $\Delta = 0$ , [51, Eq. (1.1.8)], [52, Eq. (1.1.6)] and [52, Eq. (1.2.15)] are satisfied for the third Mellin Baren's integral, thus, by applying the residues theorem [52, Eq. (1.2)] on  $\mathcal{R}_1$  it yields

$$\mathcal{R}_{1} \sim \sum_{k=0}^{\infty} \frac{(-1)^{k}}{k!} \frac{\Gamma(s_{2}-1-k) \Gamma(-s_{2}+s_{1}+1+k)}{\Gamma(s_{2}-k)} \times \left(C\kappa_{v_{D_{r}}}^{2}\right)^{-s_{2}+s_{1}+1+k} + \Gamma(1-s_{2}) \Gamma(s_{1}) \left(C\kappa_{v_{D_{r}}}^{2}\right)^{s_{1}}.$$
(94)

Consequently, substituting (94) into (92), (48) is attained in terms of bivariate FHF.

### APPENDIX D

#### **PROOF OF PROPOSITION 4**

Likewise to  $F_{\gamma_{eq}^{(1)}}(z)$ , by replacing (6) and (36) in (47), one gets

$$F_{\gamma_{eq}^{(2)}}(z) \approx a_1 Q_2 \sum_{m_1=1}^{\beta} b_{m_1} \mathcal{I}_4(s_1, s_3),$$
 (95)

where

$$\mathcal{I}_4(s_1, s_3) = \int_0^{\frac{1}{\kappa_{\nu_{D_r}}^2}} \frac{1}{(1 - \kappa \kappa_{\nu_{D_r}}^2)}$$

$$G_{2,3}^{2,1} \left[ \frac{z}{a_2} + \frac{z}{a_2} \frac{C}{x} \middle| 0; a_3 \atop a_4, a_5; -1 \right] = \frac{1}{2\pi j} \int_{\mathcal{C}_1} \frac{\Gamma(s_1 + a_4)\Gamma(s_1 + a_5)\Gamma(1 - s_1)}{\Gamma(s_1 + a_3)\Gamma(2 - s_1)} \left( \frac{z}{a_2} + \frac{z}{a_2} \frac{C}{x} \right)^{-s_1} ds_1. \tag{85}$$

$$G_{1,2r+2}^{2r+2,0} \left[ \mathcal{B}_1 \frac{x}{(1 - x\kappa_{\nu_{D_r}}^2)} \middle| \frac{\xi^2}{\kappa_1} + 1 \right] = \frac{1}{2\pi j} \int_{\mathcal{C}_2} \frac{\Gamma(s_2 + \frac{\xi^2}{r}) \prod_{\ell=0}^{r-1} \Gamma\left(s_2 + \frac{\alpha + \ell}{r}\right) \prod_{\ell=0}^{r-1} \Gamma\left(s_2 + \frac{m_1 + \ell}{r}\right) \Gamma(s_2 + 1 + m_I)}{\Gamma(s_2 + \frac{\xi^2}{r} + 1)} \times \left( \mathcal{B}_1 \frac{x}{(1 - x\kappa_{\nu_{D_r}}^2)} \right)^{-s_2} ds_2. \tag{86}$$

$${}_{2}F_{1}\left(s_{1}, s_{1} - s_{2} + 1; s_{1} + 1; -\frac{1}{C\kappa_{\nu_{D_{r}}}^{2}}\right) = \frac{\Gamma\left(s_{1} + 1\right)}{2\pi j\Gamma\left(s_{1}\right)\Gamma\left(s_{1} - s_{2} + 1\right)} \int_{\mathcal{C}_{t}} \frac{\Gamma\left(s_{1} + t\right)\Gamma\left(s_{1} - s_{2} + 1 + t\right)\Gamma\left(-t\right)}{\Gamma\left(s_{1} + 1 + t\right)} \left(\frac{1}{C\kappa_{\nu_{D_{r}}}^{2}}\right)^{t} dt. \tag{90}$$



$$\times G_{2,3}^{2,1} \left[ \frac{z\left(1 + \frac{C}{x}\right)}{a_2} \middle| \begin{array}{c} 0; a_3 \\ a_4, a_5; -1 \end{array} \right]$$

$$\times G_{1,3}^{3,0} \left[ \mathcal{B}_2 \left( \frac{x}{(1 - x\kappa_{v_{D_r}}^2)} \right)^{\frac{1}{r}} \middle| \begin{array}{c} -, \xi^2 + 1 \\ \xi^2, \alpha, m_1, - \end{array} \right] dx.$$

$$(96)$$

We have (97), as shown at the bottom of the page, so

$$\mathcal{I}_{4}(s_{1}, s_{3}) = \frac{1}{(2\pi j)^{2}} \int_{\mathcal{C}_{1}} \frac{\Gamma(s_{1} + a_{4})\Gamma(s_{1} + a_{5})\Gamma(1 - s_{1})}{\Gamma(s_{1} + a_{3})\Gamma(2 - s_{1})} \times \left(\frac{z}{a_{2}}\right)^{-s_{1}} \int_{\mathcal{C}_{3}} \frac{\Gamma(s_{3} + \xi^{2})\Gamma(s_{3} + \alpha)}{\Gamma(s_{3} + \xi^{2} + 1)} \times \Gamma(s_{3} + m_{1})\mathcal{B}_{2}^{-s_{3}}\mathcal{I}_{5}(s_{1}, s_{3})ds_{1}ds_{3},$$
(98)

where

$$\mathcal{I}_{5}(s_{1}, s_{3}) = \left(\kappa_{\nu_{D_{r}}}^{2}\right)^{\frac{s_{3}}{r} - 1} \int_{0}^{\frac{1}{\kappa_{\nu_{D_{r}}}^{2}}} x^{s_{1} - \frac{s_{3}}{r}} (x + C)^{-s_{1}} \times \left(\frac{1}{\kappa_{\nu_{D_{r}}}^{2}} - x\right)^{\frac{s_{3}}{r} - 1} dx.$$
(99)

By using [38, 3.197.8], one obtains

$$\mathcal{I}_{5}(s_{1}, s_{3}) = \left(\kappa_{\nu D_{r}}^{2}\right)^{\frac{s_{3}}{r}-1} \left(C\kappa_{\nu D_{r}}^{2}\right)^{-s_{1}} \times \frac{\Gamma\left(\frac{s_{3}}{r}\right) \Gamma\left(s_{1} - \frac{s_{3}}{r} + 1\right)}{\Gamma\left(s_{1} + 1\right)} \times {}_{2}F_{1}\left(s_{1}, s_{1} - \frac{s_{3}}{r} + 1; s_{1} + 1; -\frac{1}{C\kappa_{\nu D_{r}}^{2}}\right),$$

$$(100)$$

where  $Re(\frac{s_3}{r}) > 0$ , and  $Re(s_1 - \frac{s_3}{r} + 1) > 0$ . Now, using the Mellin-Barnes integral representation of the GHF [38, Eq. (9.113)], yields (101), as shown at the bottom of the page. Hence

$$\mathcal{I}_{5}(s_{1}, s_{3}) = \left(\kappa_{\nu_{D_{r}}}^{2}\right)^{\frac{s_{3}}{r}-1} \left(\frac{1}{C\kappa_{\nu_{D_{r}}}^{2}}\right)^{s_{1}} \frac{\Gamma\left(\frac{s_{3}}{r}\right)}{2\pi j\Gamma\left(s_{1}\right)}$$

$$\times \int_{\mathcal{C}_{\nu}} \frac{\Gamma\left(s_{1}+\nu\right)\Gamma\left(s_{1}-\frac{s_{3}}{r}+1+\nu\right)\Gamma\left(-\nu\right)}{\Gamma\left(s_{1}+1+\nu\right)}$$

$$\times \left(\frac{1}{C\kappa_{\nu_{D_{r}}}^{2}}\right)^{\nu} d\nu, \tag{102}$$

Then, one obtains

$$\mathcal{I}_{4}(s_{1}, s_{3}) = \frac{1}{2\pi j} \int_{\mathcal{C}_{1}} \frac{\Gamma(s_{1} + a_{4})\Gamma(s_{1} + a_{5})\Gamma(1 - s_{1})}{\Gamma(s_{1} + a_{3})\Gamma(2 - s_{1})\Gamma(s_{1})} \times \left(\frac{z}{a_{2}}\right)^{-s_{1}} \left(\frac{1}{C\kappa_{v_{D_{r}}}^{2}}\right)^{s_{1}} \frac{1}{2\pi j} \int_{\mathcal{C}_{3}} \times \frac{\Gamma(s_{3} + \xi^{2})\Gamma(s_{3} + \alpha)\Gamma(s_{3} + m_{1})\Gamma\left(\frac{s_{3}}{r}\right)}{\Gamma(s_{3} + \xi^{2} + 1)} \times \mathcal{B}_{2}^{-s_{3}} \left(\kappa_{v_{D_{r}}}^{2}\right)^{\frac{s_{3}}{r} - 1} \mathcal{R}_{2} ds_{1} ds_{3}.$$
(103)

where

$$\mathcal{R}_2 = \frac{1}{2\pi j} \int_{\mathcal{C}_v} \frac{\Gamma\left(s_1 - \frac{s_3}{r} + 1 + v\right) \Gamma\left(-v\right)}{s_1 + v} \left(\frac{1}{C\kappa_{v_{D_r}}^2}\right)^v dv.$$
(104)

Similarly as the CDF of the first scenario, by applying the residues theorem [52, Eq. (1.2)], one obtains

$$\mathcal{R}_{2} \sim \sum_{k_{2}=0}^{\infty} \frac{(-1)^{k_{2}}}{k_{2}!} \frac{\Gamma\left(\frac{s_{3}}{r} - 1 - k\right) \Gamma\left(-\frac{s_{3}}{r} + s_{1} + 1 + k_{2}\right)}{\Gamma\left(\frac{s_{3}}{r} - k\right)} \times \left(C\kappa_{\nu_{D_{r}}}^{2}\right)^{-\frac{s_{3}}{r} + s_{1} + 1 + k_{2}} + \Gamma\left(1 - \frac{s_{3}}{r}\right) \Gamma\left(s_{1}\right) \left(C\kappa_{\nu_{D_{r}}}^{2}\right)^{s_{1}}.$$
 (105)

Consequently, by substituting (105) into (103), (49) is attained.

#### **APPENDIX E**

# **PROOF OF PROPOSITION 5**

 $P_{b,\ell}$  is written as follows

$$P_{b,\ell} \approx \int_0^\infty \gamma^{p-1} \exp\left(-q\gamma\right) F_{\gamma_{eq}^{(\ell)}}(\gamma) d\gamma. \tag{106}$$

where  $P_{b,1}$  and  $P_{b,2}$  are computed below.

1)  $P_{b,1}$  EXPRESSION

Replacing (48) into (106) gives (107), as shown at the bottom of the next page, where

$$\mathcal{I}_{6}(s_{1}) = \int_{0}^{\infty} e^{-q\gamma} \gamma^{p-1-s_{1}} d\gamma$$
$$= \Gamma(p-s_{1})q^{-p+s_{1}}, \tag{108}$$

using [47, Eq. (07.34.21.0009.01)].

$$G_{1,3}^{3,0} \left[ \mathcal{B}_2 \left( \frac{x}{(1 - x\kappa_{\nu D_r}^2)} \right)^{\frac{1}{r}} \Big|_{\xi^2, \alpha, m_1, -}^{-, \xi^2 + 1} \right] = \frac{1}{2\pi j} \int_{\mathcal{C}_3} \frac{\Gamma(s_3 + \xi^2)\Gamma(s_3 + \alpha)\Gamma(s_3 + m_1)}{\Gamma(s_3 + \xi^2 + 1)} \left( \mathcal{B}_2 \left( \frac{x}{(1 - x\kappa_{\nu D_r}^2)} \right)^{\frac{1}{r}} \right)^{-s_3} ds_3.$$

$$(97)$$

$${}_{2}F_{1}\left(s_{1}, s_{1} - \frac{s_{3}}{r} + 1; s_{1} + 1; -\frac{1}{C\kappa_{\nu_{D_{r}}}^{2}}\right) = \frac{\Gamma\left(s_{1} + 1\right)}{2\pi j\Gamma\left(s_{1}\right)\Gamma\left(s_{1} - \frac{s_{3}}{r} + 1\right)} \int_{\mathcal{C}_{\nu}} \frac{\Gamma\left(s_{1} + \nu\right)\Gamma\left(s_{1} - \frac{s_{3}}{r} + 1 + \nu\right)\Gamma\left(-\nu\right)}{\Gamma\left(s_{1} + 1 + \nu\right)} \times \left(C\kappa_{\nu_{D_{r}}}^{2}\right)^{-\nu} d\nu. \tag{101}$$



By replacing (108) into (107), together with the use of [53], (53), is attained in terms of bivariate FHF [47].

#### 2) Pb.2 EXPRESSION

Equivalently as finding (53), (54) is derived using bivariate FHF [47].

#### **APPENDIX F**

#### **PROOF OF PROPOSITION 6**

#### A. FIRST SCENARIO

 $P_{b,1}$  defined in (53), can be written as a Mellin-Barnes integral as (109), shown at the bottom of the page, where

$$\mathcal{I}_{1}(s_{1}) = \frac{\Gamma(s_{1} + a_{4})\Gamma(s_{1} + a_{5})\Gamma(1 - s_{1})\Gamma(p - s_{1})}{\Gamma(s_{1} + a_{3})\Gamma(2 - s_{1})\Gamma(s_{1})} (qa_{2})^{s_{1}},$$
(110)

$$\mathcal{I}_{2}(s_{2}) = \frac{\Gamma(s_{2} + \frac{\xi^{2}}{r})\Gamma(s_{2})\Gamma(s_{2} - 1 - k)}{\Gamma(s_{2} + \frac{\varepsilon^{2}}{r} + 1)\Gamma(s_{2} - k)}$$

$$\times \prod_{\ell=0}^{r-1} \Gamma\left(s_{2} + \frac{\alpha + \ell}{r}\right) \prod_{\ell=0}^{r-1} \Gamma\left(s_{2} + \frac{m_{1} + \ell}{r}\right)$$

$$\times \Gamma(s_{2} + 1 + m_{I}) (CB_{1})^{-s_{2}},$$

$$\mathcal{I}_{3}(s_{1}) = \frac{\Gamma(s_{1} + a_{4})\Gamma(s_{1} + a_{5})\Gamma(1 - s_{1})\Gamma(p - s_{1})}{\Gamma(s_{1} + a_{3})\Gamma(2 - s_{1})} (qa_{2})^{s_{1}},$$
(112)

As the conditions  $\Delta_0 = 0$  and  $\delta = 1$  [51, Eqs. (1.1.8) and (1.1.9)] are satisfied, taking into account that  $s_2$  is constant, in addition to 0 < z < 1 where  $z = \frac{1}{ga_2}$ , the first part of  $P_{b,1}$ 

can be written as infinite summation of residues evaluated at the left poles of  $\mathcal{I}_1(s_1)$ . Moreover, as we are interested in the asymptotic SNR (i.e.,  $z \to 0$ ), it is sufficient to evaluate the residue corresponding to the top left poles. i.e., only for the elements  $a_4$ ,  $a_4$ ,  $1 + k - s_2$ .

It's worth noting that  $\mathcal{I}_1(s_1)$  admits only first-order (FO) LPs. Leveraging [51, Theorems 1.2, 1.4], their respective residues may be evaluated.

So, the residues of  $\mathcal{I}_1(s_1)$  at  $a_4$ ,  $a_4$  and  $1+k-s_2$  can be expressed, respectively as

$$T^{(1)} \sim \Omega^{(1)} z^{a_4},$$
 (114)

$$T^{(2)} \sim \Omega^{(2)} z^{a_5},$$
 (115)

$$\mathcal{T}^{(3)} \sim \Omega^{(3)} z^{-(s_2 - 1 - k)},$$
 (116)

where  $\Omega^{(1)}$ ,  $\Omega^{(2)}$  and  $\Omega^{(3)}$  are given by (57), (58) and (59).

For the second part of  $P_{b,1}$ , the condition  $\Delta_0=0$  is satisfied for the first Meijer function, in addition to  $0< z=\frac{1}{qa_2}<\delta=1$  [51, Eqs. (1.1.8) and (1.1.9)]. Consequently, the residues of  $\mathcal{I}_3(s_1)$  can be expressed respectively as

$$T_1^{(1)} = T^{(1)}\Gamma(-a_4),$$
 (117)

and

$$T_1^{(2)} = T^{(2)}\Gamma(-a_5).$$
 (118)

Thus, the asymptotic expression for  $P_{b,1}$  is obtained as (55).

#### **B. SECOND SCENARIO**

Similarly, as the first scenario, (56) is obtained for the second scenario.

$$P_{b,1} \approx Ca_{1}Q_{1} \sum_{m_{1}=1}^{\beta} b_{m_{1}} r^{\alpha+m_{1}-2} \sum_{k=0}^{\infty} \frac{(-1)^{k}}{k!} \left( C\kappa_{\nu_{D_{r}}}^{2} \right)^{k} \frac{1}{2\pi j} \int_{C_{1}} \frac{\Gamma(s_{1}+a_{4})\Gamma(s_{1}+a_{5})\Gamma(1-s_{1})}{\Gamma(s_{1}+a_{3})\Gamma(2-s_{1})\Gamma(s_{1})} \left( \frac{1}{a_{2}} \right)^{-s_{1}} \times \frac{1}{2\pi j} \int_{C_{2}} \frac{\Gamma(s_{2}+\kappa_{1})\Gamma(s_{2})\Gamma(s_{2}-1-k)}{\Gamma(s_{2}+\frac{\xi^{2}}{r}+1)\Gamma(s_{2}-k)} (CB_{1})^{-s_{2}} \Gamma(-s_{2}+s_{1}+1+k) \mathcal{I}_{6}(s_{1}) ds_{1} ds_{2} + \frac{a_{1}Q_{1}}{\kappa_{\nu_{D_{r}}}^{2}} \sum_{m_{1}=1}^{\beta} b_{m_{1}} r^{\alpha+m_{1}-2} \frac{1}{2\pi j} \int_{C_{1}} \frac{\Gamma(s_{1}+a_{4})\Gamma(s_{1}+a_{5})\Gamma(1-s_{1})}{\Gamma(s_{1}+a_{3})\Gamma(2-s_{1})} \left( \frac{1}{a_{2}} \right)^{-s_{1}} \times \frac{1}{2\pi j} \int_{C_{2}} \frac{\Gamma(s_{2}+\kappa_{3})\Gamma(s_{2})\Gamma(1-s_{2})}{\Gamma(s_{2}+\frac{\xi^{2}}{r}+1)} \left( \frac{B_{1}}{\kappa_{\nu_{D_{r}}}^{2}} \right)^{-s_{2}} \mathcal{I}_{6}(s_{1}) ds_{1} ds_{2}.$$

$$(107)$$

$$P_{b,1} \approx \frac{Ca_1 \mathcal{Q}_1}{q^p} \sum_{m_1=1}^{\beta} b_{m_1} r^{\alpha+m_1-2} \sum_{k=0}^{\infty} \frac{(-1)^k}{k!} \left( C\kappa_{\nu_{D_r}}^2 \right)^k \frac{1}{(2\pi j)^2} \int_{\mathcal{C}_1} \int_{\mathcal{C}_2} \mathcal{I}_1(s_1) \mathcal{I}_2(s_2) \Gamma\left( -s_2 + s_1 + 1 + k \right) ds_1 ds_2$$

$$+ \frac{a_1 \mathcal{Q}_1}{q^p \kappa_{\nu_{D_r}}^2} \sum_{m_1=1}^{\beta} b_{m_1} r^{\alpha+m_1-2} \frac{1}{(2\pi j)^2} \int_{\mathcal{C}_1} \int_{\mathcal{C}_2} \mathcal{I}_3(s_1) \mathcal{I}_4(s_2) ds_1 ds_2$$

$$(109)$$

$$\mathcal{I}_{4}(s_{2}) = \frac{\Gamma(s_{2} + \frac{\varepsilon^{2}}{r}) \prod_{\ell=0}^{r-1} \Gamma\left(s_{2} + \frac{\alpha+\ell}{r}\right) \prod_{\ell=0}^{r-1} \Gamma\left(s_{2} + \frac{m_{1}+\ell}{r}\right) \Gamma(s_{2} + 1 + m_{I}) \Gamma\left(s_{2}\right) \Gamma\left(1 - s_{2}\right)}{\Gamma(s_{2} + \frac{\varepsilon^{2}}{r} + 1)} \left(\frac{\mathcal{B}_{1}}{\kappa_{\nu_{D_{r}}}^{2}}\right)^{-s_{2}}.$$
(113)



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