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## **RESEARCH ARTICLE**

# A High Gain and Uniform Power Mushroom Antenna Using Metasurface

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**ABSTRACT** In this study, we present a simple feed-aperture coupled antenna with a high gain and flat-top radiation pattern for microwave power transmission (MPT) applications involving misalignment.  $A \, 4 \times 4$  mushroom structure is proposed to suppress the back-lobe radiation and to achieve the high gain of the aperture-coupled antenna. Additionally, to improve the flat-top radiation pattern and circular polarization (CP), an array  $4 \times 4$  metasurface is employed to obtain an equal electric field in the propagation direction. The overall dimensions are  $2.13\lambda_0 \times 2.13\lambda_0 \times 0.228\lambda_0$  at 5.8 GHz. The measurement results show that the impedance bandwidth of  $<-10$  dB of 5.5 - 6 GHz (8.69 %), a maximum realized left-hand circular polarization (LHCP) gain of 10.4 dBi with flat-top beamwidth (1-dB) of 36◦ and 38◦ for E and H plane, respectively. Moreover, the proposed transmitter antenna is tested in a realistic MPT indicating an advantage of radiating uniform power of 10 mW in the diameter range of 80 mm.

**INDEX TERMS** Circular polarization (CP), flat-topped radiation pattern (FTRP), microwave power transmission (MPT), lateral misalignment, metasurface (MS).

## **I. INTRODUCTION**

Recently, wireless power transmission (WPT) has advanced rapidly in the communication systems  $[1]$ ,  $[2]$ ,  $[3]$ ,  $[4]$ . It can power remote electronic devices where wired charging is difficult or impossible to have access. In this case, the radiation pattern of the antenna has become a necessary characteristic. In practical, the system efficiency is degraded significantly over the long distances, which, as a result, requires a high-gain antenna to achieve high efficiency. The conventional antennas typically exhibit power drop as the angle deviates from the main direction, which limits the application of the conventional antennas in systems where a uniform power level is required over a wide angle range such as WPT, beam steering, and radar.

As an alternative, flat-top radiation pattern (FTRP) antennas have emerged as a promising solution to this limitation because they can offer a nearly constant power level within

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<span id="page-0-6"></span><span id="page-0-5"></span><span id="page-0-4"></span><span id="page-0-3"></span><span id="page-0-2"></span><span id="page-0-1"></span><span id="page-0-0"></span>a certain angle range. With such the unique radiation characteristics, the FTRP antennas have proliferated in wireless communication applications such as satellite communication netowrks [\[5\], fif](#page-6-4)th-generation (5G) networks [\[6\], es](#page-6-5)pecially microwave power transmission (MPT) systems [\[7\]. M](#page-6-6)oreover, an FTRP antenna can provide efficient power transfer over a range of distances and orientations, enabling a more flexible position of mobile devices. Besides, in beamforming applications, FTRP can offer a more efficient method of directing the energy to a specific target by reducing the need for the complex beamforming algorithms [\[8\],](#page-6-7) [\[9\],](#page-6-8) [\[10\].](#page-6-9) Furthermore, it can improve target detection and reduce the effects of sidelobes that can cause interference with other radar systems [\[11\].](#page-6-10)

<span id="page-0-12"></span><span id="page-0-11"></span><span id="page-0-10"></span><span id="page-0-9"></span><span id="page-0-8"></span><span id="page-0-7"></span>Various methods have been conducted to modulate radiation or creation of flat-top beamwidth. For instance, the usage of a Fabry-érot cavity (PFC) antenna based on the ray-tracing model was proposed in  $[12]$  and  $[13]$  to enhance the gain and especially to obtain the FTRP. Uniform power radiation using leaky wave antennas (LWAs) is also introduced in <span id="page-1-4"></span><span id="page-1-2"></span><span id="page-1-1"></span>literature [\[14\]. B](#page-6-13)esides, ten-element bowtie dipoles are incorporated with the feeding network to obtain the uniform power from −12◦ to 12◦ [\[15\]. M](#page-6-14)oreover, circular polarization (CP) can be integrated with the advantage of minimizing losses and offering flexible orientation in the antenna. In [\[16\], a](#page-6-15) single rectangular dielectric resonator antenna (DRA) combining TE*<sup>y</sup>* <sup>119</sup> and TE*<sup>y</sup>* <sup>113</sup> modes was designed to obtain flat-top beamwidth of 85° and 58° at E and H planes, respectively. Besides, a flat-top radiation pattern of larger than 40° for both planes and CP is generated by using the mushroom technique [\[17\]. M](#page-6-16)etasurface (MS) is another potential way to develop antenna efficiency. In one approach, a linear graded index metasurface (LGIMS) lens was constructed to steer the main radiated beam with FTRP characteristics [\[18\]. A](#page-6-17)nother work is to use a small-size double-shell integrated lens antenna [\[19\]. T](#page-6-18)he results show that the MS structure can enhance the gain of the flat-top beam and minimize the antenna's back-lobe, whereas the drawbacks of these structures remain large structure, and exhibit linear polarization.

<span id="page-1-6"></span><span id="page-1-5"></span>This paper presents a novel FTRP antenna for misalignment WPT applications. The proposed antenna is constructed based on a 4  $\times$  4 mushroom structure, where 2  $\times$  2 shorting pin is absent to improve the side direction. In order to orient the wave energy equally and achieve uniform power and circular polarization, the antenna combines with a  $4 \times 4$  metasurface. The proposed antenna was computed and verified experimentally. As observed, the structure not only uses the metasurface to achieve the high gain and CP but also obtains uniform power radiation which indicates an advantage over our previous work [\[17\].](#page-6-16)

#### **II. ANTENNA DESIGN AND CHARACTERISTICS**

#### A. RADIATE PRINCIPLE

<span id="page-1-8"></span><span id="page-1-7"></span>The scenario and corresponding circuit for creating uniform power are shown in Fig. [1](#page-1-0) in order to explain the principle of producing a flat-top radiation antenna. A mushroom structure is used in this work. Due to its ability to function as an electromagnetic band-gap (EBG) structure when combined with a shorting via, the mushroom structure has a number of benefits such as flat-top radiation, side and back-lobe reduction, and ability to suppress the surface wave of both TE and TM polarization [\[20\],](#page-6-19) [\[21\]. I](#page-6-20)n addition, one of the simplest methods to generate a flat-top beam is to reduce the peak orientation in the 0-degree direction and to increase the radiation intensity in the lateral direction. As illustrated in Fig. [1\(a\),](#page-1-0) a metasurface is employed to fulfill this requirement. The metasurface operates as the parasitic element to promote the direct improvement of the wave radiation levels of the mushroom structure.

The total field of the proposed structure can be calculated by two equations following as [\[17\]:](#page-6-16)

$$
[E_{\phi}]_{total} = [E_{\phi}]_{Feeding} + (Ae^{j\omega})[E_{\phi}]_{radiator} + E_{\phi}\sqrt{\delta D_{\phi}}
$$
  

$$
[E_{\theta}]_{total} = [E_{\theta}]_{Feeding} + (Ae^{j\omega})[E_{\theta}]_{radiator} + E_{\theta}\sqrt{\delta D_{\theta}},
$$
  
(1)

<span id="page-1-3"></span><span id="page-1-0"></span>

**FIGURE 1.** (a) Scenario of generating uniform power antenna and (b) The E-field distribution.

where  $E_{\phi}$  and  $E_{\theta}$  are two orthogonal components of the electric field, and A and  $\omega$  are the amplitude and phase, respectively. The additional directivity δD after combining the metasurface was calculated based on the ray-tracking model as [\[12\],](#page-6-11) [\[13\]](#page-6-12)

$$
\delta D = 10 \log \frac{1 - B^2}{1 + B^2 - 2B \cos(\delta - \pi - h \frac{4\pi}{\lambda} \cos \theta)},
$$
 (2)

where  $\theta$  is the angle between the unit cell and the vertical, and B and  $\delta$  are the amplitude and phase of the reflection coefficient, respectively. In order to achieve the maximum power pattern at  $β$  direction, the distance h between the ground plane and metasurface must be satisfied as

$$
h = \frac{(2n\pi + \delta - \pi)\lambda}{4\pi \cos\beta}, \quad n = 1, 2, \dots
$$
 (3)

To radiate efficiently and exibit a low profile, it can be shown that the metasurface should be set up around a quarter wavelength above the ground plane. Furthermore, the figure for electric distribution indicates that the exception is realized based on the principle of generating flat-top radiation, as shown in Fig.  $1(b)$ . It can be seen that the proposed antenna is composed of a mushroom structure integrated with a metasurface, which provides a relatively flat amplitude distribution.

The main contribution of this idea is the use of a phasecorrected structure MS, which improves the radiation field uniformity while preserving the radiation characteristics from the mushroom structure. The paper's advantages are a low profile, high gain, uniform power radiation that is superior to most previous designs.

<span id="page-2-0"></span>

**FIGURE 2.** Configuration of the proposed FTRP antenna (a) side view, (b) top view of the mushroom structure, and (c) top view of the MS.

#### B. ANTENNA GEOMETRY

Fig. [2](#page-2-0) illustrates the configuration of the proposed FTRP antenna, which comprises an aperture coupled feed, a mushroom structure, a metasurface, and a subminiature version A (SMA) connector. The structure is designed on three substrate layers, which are Taconic TLY-5 sheets (relative dielectric constant of 2.2 and loss tangent of 0.0009). The aperture-coupled feed is printed on both sides of the bottom substrate with thickness of 0.8mm, and the mushroom structure is located directly above the substrate with thickness of 3.2mm. The mushroom structure is composed of  $4 \times 4$  square unit cells with the size  $W_{p1}$  of about a quarter wavelength. Moreover, we can utilize the mushroom structure antenna incorporating with metasurface, where the each unit cell is choosed to be a same size as radiating elements to direct the electric field. Besides, the ground plane size is optimized around  $2\lambda_0$  to obtain flat-top radiation. An air gap with a quarter wavelength is inserted between two layers to obtain the high gain and low profile. Besides, the proposed antenna was computed by using ANSYS Electronics Desktop and the geometry parameter values are listed as follows:  $L_1 = 23$ ,  $L_2 = 15$ ,  $L_c = 4.5$ ,  $L_f = 59$ ,  $W = 110$ ,  $W_1 = 3$ ,  $W_2 = 3$ ,  $C =$ 20,  $W_{p1} = 11.5$ ,  $W_{p2} = 11.5$ ,  $x_p = 19$ ,  $y_p = 19.3$ ,  $g_1 = 1.1$ ,  $g_2 = 1.1, H_{air} = 13, h_1 = 0.8, h_2 = 3.2, h_3 = 0.8, \theta_1 = 40^\circ.$ (Unit mm)

<span id="page-2-1"></span>

**FIGURE 3.** Details in design steps of proposed antenna.

#### C. DESIGN EVOLUTION

The combination of the mushroom antenna and metasurface provides a flat-top radiation enhancement, surpassing previous results found in [\[15\]](#page-6-14) and [\[17\]. T](#page-6-16)he proposed antenna is obtained by considering the reflection coefficient, and especially the flat-top radiation pattern. Throughout the design process, four distinct antenna configurations are developed in order to achieve the best performance characteristics, as illustrated in Fig. [3.](#page-2-1)

Antenna #1 is designed with an increased number of mushroom units and using four corner cuts on the ground plane, utilizing the principle established in [\[17\]](#page-6-16) to create an FTRP and improve gain. In the next stage of development, a metasurface consisting of a  $4 \times 4$  unit cell with two cut corners on an additional substrate is introduced in antenna #2. The purpose of this is to minimize the peak directivity at  $0<sup>0</sup>$  and to enhance gain in surrounding directions by using the same size of unit cells of the mushroom structure. In antenna #3, the addition of  $\theta_1$ -rotated ground slots produces the CP characteristic, while simultaneously removing the  $2 \times 2$  shorting via in the middle of the radiator to improve the impedance bandwidth. After thorough simulations using ANSYS Electronics Desktop, the final design is realized to be a combination of the antenna #2 and the antenna #3. Each unit cell is used with the same size as the radiator of the mushroom structure. All three configurations are simulated under identical conditions in terms of overall size, height, type of substrate, and parameter values, as listed in Table [1.](#page-3-0)

The performances of each antenna geometry are shown in Fig. [4.](#page-3-1) Antenna #1 exhibits poor impedance matching and an approximately 11 dB improvement in gain when the number of mushroom structures is increased, but the flat-top gain is suppressed. Antenna #2 employs a metasurface, which results in a gradually 10 dBi flat-top beamwidth



#### <span id="page-3-0"></span>**TABLE 1.** Comparison with lastest relevant works.

<span id="page-3-1"></span>

**FIGURE 4.** (a) Reflection coefficient (S<sub>11</sub>), (b) AR and (c) total gain (''dot-line: E plane, line: H plane'').

<span id="page-3-2"></span>

<span id="page-3-3"></span>**FIGURE 5.** Simulated results on S<sub>11</sub>, AR, and realized gain values according to air-gap (h) .



in the H-plane and there is an optimal matching impedance at 5.8 GHz. However, the axial ratio (AR) is still higher than 3 dB. Moreover, antenna #3 shows a wide bandwidth from 5.67 GHz to 6.48 GHz, and the axial ratio value is approximately 3 dB at 5.9 GHz. Finally, antenna #4 yields an impedance bandwidth  $(S_{11} < -10 \text{ dB})$  of 19.67% (5.5-6.7 GHz) with CP characteristic at 5.8GHz. The proposed antenna also achieves a 1-dB beamwidth of larger than  $36^\circ$  in both the E and H planes.

As aforementioned, the additional directivity of the metasurface is directly influenced by the distance h between the ground and the metasurface. Therefore, the  $S_{11}$ , AR,

**FIGURE 6.** Current distributions on the metasurface at 5.8 GHz.

gain radiation subject to the distance h are evaluated, as depicted in Fig. [5.](#page-3-2) It can be observed that good impedance matching is obtained for the whole situation. For the case where h is adjusted to 13 mm (approximately a quarter wavelength), the AR and 3 dB FTRP simultaneously achieve the best state.

Diagrams with current distribution are illustrated to clarify the circular polarization of the proposed antenna, as shown in Fig. [6.](#page-3-3) The current directions are supported with additional

<span id="page-4-0"></span>

<span id="page-4-1"></span>**FIGURE 7.** Current distributions on the ground plane and radiator at 5.8 GHz.



**FIGURE 8.** Total efficiency of the antenna.

highlighted black arrows. In the initial phase, the current intensity on the metasurface is followed upward 45◦ direction, whereas the figure for a phase of 90◦ indicates that current density is observed downward 45◦ direction. The current distribution on the ground plane and radiator with the phase current directed along the x and y axes, is shown in Fig. [7.](#page-4-0) Moreover, it can be seen that the current dispersion is most concentrated on the region with a mushroom structure. Finally, the figure for the total efficiency of the proposed structure is illustrated in Fig. [8.](#page-4-1) It is indicated that the radiation efficiency is higher than 97% at the considered frequency range. Hence, the FTRP antenna can radiate power effectively.

#### **III. MEASUREMENTS AND EXPERIMENTS**

#### A. FABRICATION AND MEASUREMENT RESULTS

For verifying the simulation results, the proposed antenna is fabricated with an overall size of  $2.13\lambda_0 \times 2.13\lambda_0 \times 0.228\lambda_0$ , as depicted in Fig. [9.](#page-4-2) The antenna is connected to a vector network analyzer (Agilent 8719D) to realize the reflection coefficient results. It is shown in Fig.  $10(a)$  that the measured results obtained the impedance bandwidth  $\left(<-10 \text{ dB}\right)$  is 7% from 5.6 to 5.9 GHz, whereas the simulated one is 8.69% (5.5–6GHz). Furthermore, a far-field measurement is set up

<span id="page-4-2"></span>

**FIGURE 9.** Fabricated geometry of the proposed FTRP antenna.

<span id="page-4-3"></span>

**FIGURE 10.** Simulated and measured results. (a) |S<sub>11</sub>|, and (b) AR and realized gain values.

with an anechoic chamber environment to evaluate the twodimension (2D) radiation patterns. As indicated in 10(b), the axial-ratio value (AR) has approximately 0 dB for simulated result at 5.8GHz and yields 1.4 dB for measured one. Besides, the realized gain is also measured, obtaining a peak gain of 10.4 dBi, which is 0.5 dBi lower than simulation. The deviation occurs when the substrate layers are stacked, which makes the spacing between them incorrect.

On the other hand, the realized radiation pattern of the proposed structure versus angle is evaluated in Fig. [11.](#page-5-0) There is a good agreement between measured and simulated results. It is clear that the measured LHCP gain is realized with the maximum directivity of 10.4 dBi in both E and H planes, whereas the simulated one achieves the maximum of

<span id="page-5-0"></span>

**FIGURE 11.** Simulated and measured results of the proposed antenna at 5.8 GHz (a) E plane pattern (b) H plane pattern.

10.88 dBi. In addition, the cross left-hand circular polarization is less than -20 dB, and the 1 dB beamwidth in the E and H planes is 36<sup>°</sup> and 38<sup>°</sup>, respectively.

#### B. COMPARISON AND DISCUSSION

Table [1](#page-3-0) summarizes the advantages of the proposed FTRP antenna compared to the other related state-of-the-art studies. The proposed antenna is highlighted for the easy observation of highly efficient FTRP, CP, and low profile. Specifically, the proposed design obtains a smaller in overall size and a CP characteristic relative to the PFC and LWAs methods in [\[13\]](#page-6-12) and [\[14\].](#page-6-13) In particular, with the support of the metasurface, the proposed design yields an performance improvement as compared to  $[15]$ ,  $[16]$ , and  $[17]$ , which are smaller size, and higher gain. The antenna using metasurface in [\[18\]](#page-6-17) and [\[19\]](#page-6-18) achieves good results in high gain and wide beamwidth, but the compactless structure size and linear polarization are disadvantegeous.

### C. MICROWAVE POWER TRANSMISSION SYSTEM

For further verification, a MPT system is built to evaluate the flat-top beam antenna, as depicted in Fig. [12.](#page-5-1) The proposed antenna is designed in the previous sections and acts as a transmitting antenna. The FTRP antenna is linked to an amplifier (SN192902007), RF signal generator (Agilent N5182A), and DC power supply (Aligent E3633A) on the transmitter side, where the radiated power at the transmitting antenna is restricted to 30dBm (1 W) because the system is executed under FCC regulations that are designed to safeguard the human body. At the receiver side, a rectenna is used in [\[4\], w](#page-6-3)hich is composed of a receiving antenna and a rectifier for verifying the received power. The receiver is placed

<span id="page-5-1"></span>

**FIGURE 12.** Experimental setup of the MPT system.

<span id="page-5-2"></span>

**FIGURE 13.** Output power at receiver (a) xoz plane (b) yoz plane.

in the light of sight with a transmitter at a distance of 200 mm because it is related to the sensitivity. The distance is fixed so that the energy received at the receiver is within the dynamic range of the rectifier for the highest power conversion efficiency achievement. The output load of the rectifier connects to a Digital Multimeter to observe the output voltage. As can be seen, the measured received power reaches a maximum value of approximately 10mW, which corresponds to the output voltage of 2.178V displayed on the multimeter and is calculated based on a resistive load of  $470\Omega$ . To demonstrate the uniform wireless powering capability of the transmitting antenna, the dc output voltage is monitored by varying the lateral misalignment of the rectenna. Fig. [13](#page-5-2) provides the output DC power at the receiver for both planes in the case of lateral misalignment within a 120 mm offset. The received output power is confirmed with the radiation pattern of the FRTP antenna. Specifically, the output dc power is almost constant for the lateral movement diameter of 80mm in both the E and H planes. As a result, the metasurface is used to create a direct electromagnetic field direction, which is a way to improve WPT efficiency while maintaining uniform radiation and enabling gain enhancement.

#### **IV. CONCLUSION**

In this letter, we have presented a high-gain uniform power antenna with metasurface for MPT applications. It comprises a  $4 \times 4$  mushrooms structure-based aperture coupled feeding and a metasurface to obtain uniform power radiation. The final design with the overall size of  $2.13\lambda_0 \times$  $2.13\lambda_0 \times 0.228\lambda_0$  achieves a measured bandwidth of 8.69 %

(5.5–6 GHz), a high gain of 10.4 dBi with flat-top radiation pattern wider than 36◦ in both E and H planes. The proposed FTRP antenna is also achieved several advantages with features such as high gain, uniform power radiation, and CP. In the MPT experiment, the system shows that the rectenna can receive 10mW uniform power at a distance of 200 mm with a lateral misalignment diameter of 80 mm. With the above advantage, the proposed antenna can be a good candidate for the MPT applications for charging multiple devices or moving devices.

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