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# **RESEARCH ARTICLE**

# Sensorless Control and Inductances Estimation of IPMSMs Using FPGA and High Bandwidth Current Measurement

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**ABSTRACT** This paper presents a sensorless control method and a very fast on-line inductances identification of an IPMSM. The current slopes (derivatives) at one active-voltage vector and one zerovoltage vector are measured every PWM cycle to estimate the rotor speed and position with the aim of increasing the estimation accuracy and reducing total harmonic distortion of the phase currents. In addition to these current slopes, the DC bus voltage of the inverter is measured to estimate the machine inductances on-line. The proposed on-line parameter identification method can overcome the drawback of the existing off-line methods, such as: the requirement of a robust mechanical clamping system and test signal generators. The proposed on-line method also addresses the limit of the existing on-line methods, such as slow update and the possibility of incorrect convergence of the estimated parameters. Extensive experimental studies were conducted to verify the effectiveness and robustness of the proposed sensorless control and parameters identification of the IPMSM.

**INDEX TERMS** Sensorless control, on-line parameter identification, current derivative measurement, IPMSM.

# **I. INTRODUCTION**

Interior Permanent magnet synchronous motors (IPMSM) have been applied widely in high performance applications due to their high power density, high efficiency and high control performance. The elimination of mechanical sensor, such as encoder or resolver can help to improve the reliability, reduce the size and cost of the control system [\[1\]. So](#page-7-0) far, the sensorless control methods can be classified into two main categories. The first category is based on the dynamic model of the IPMSM. The rotor speed and position can be estimated based on the estimation of back EMF [\[2\],](#page-7-1)  $[3]$ ,  $[4]$  or stator flux  $[5]$ ,  $[6]$ . In general, these methods utilize the parameters of the machine model, such as stator resistance, d-q axis inductances in the development of the

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<span id="page-0-4"></span><span id="page-0-3"></span><span id="page-0-0"></span>estimation model of the rotor speed and position. Therefore, the variation of machine parameters during the operation, such as magnetic saturation affects the performance of these model-based estimators. In addition, during low and very low speed operations these methods lose their robustness due to low signal to noise ratio. The second category is based on the saliency machine inductances in d- and q- axes, such as square wave signal injections [\[7\], \[](#page-7-6)[8\],](#page-7-7) pulse signal injections [\[9\], \[](#page-7-8)[10\].](#page-7-9) These methods inject a high frequency signal to the machine and estimate the rotor speed and position by processing of the high frequency response of the phase current. In general, these methods are robust at low and very low speed operation since they are independent of machine model. However, at high and very high speeds, the operating speeds are limited by the modulation index. The other drawbacks of saliency-based methods are the noise, high current and torque ripple due

to the injected signal. In order to reduce the noise and current ripples, the methods based on the measurement of current slopes (derivatives) during the excitation of the voltage vector of the standard pulse width modulation have been proposed [\[11\], \[](#page-7-10)[12\], \[](#page-7-11)[13\]. T](#page-7-12)hese methods do not use any injected signal, instead utilize the voltage vector during normal PWM as the excitation signals. However, due to the parasitic effect, the phase current oscillates at high frequency after the switching transition, hence affecting the accuracy of the current slope measurement. For the IPMSM with high inductance, this oscillation time could last for about 20 microseconds at full load condition. Therefore, the extension and compensation of the voltage vector must be required. For the conventional fundamental PWM excitation (FPE) method, the current derivatives at two active voltage vector and two zero voltage vector are measured to estimate rotor speed and position [\[12\]. F](#page-7-11)or IPMSM with high inductance, the long extension of the two active voltage vectors and two zero voltage vectors are required, thus increasing the total harmonic distortion of the phase current and limiting the maximum operating speed. In order to reduce the total harmonic distortion and increase the sensorless operating speed range, this paper proposes a method to estimate the rotor speed and current of the IPMSM by using current slopes at only one active and one zero voltage vector.

It is worth noting that the inductances of the IPMSM have a close relationship with the phase current slopes during the excitation of active and zero voltage vectors. This paper also presents a very fast online method to estimate the dand q- axis inductances based on the measurement of the current slopes and the DC bus voltage of the three phases two levels converter. This proposed method can handle the disadvantages of the off-line methods which require a rigid mechanical clamping system, the power signal generator or the mover to rotate the rotor to a certain speed. Additionally, the proposed method can overcome the weaknesses of the on-line methods based on the machine model shown in [\[14\],](#page-7-13) [15],  $[16]$ ,  $[17]$ , and  $[18]$ . The weaknesses of these methods are the sensitivity to the non-linearity of the converter, slow update of the estimated parameters due to the recursive principles, the possibility of divergence of the algorithm, and the complexity of tuning the hyperparameters of the method.

<span id="page-1-3"></span><span id="page-1-2"></span>Extensive numerical simulation and experimental study have been conducted to verify the effectiveness and robustness of the proposed sensorless control method over a full speed range from zero to rated speed and the inductances estimation methods. The conventional FPE sensorless method was used as a benchmark to evaluate the proposed methods in terms of estimation accuracy and total harmonic distortion of the phase current. The performance of the proposed inductance estimation method was compared with the off-line method in term of estimation accuracy, and with the recursive least square online methods in terms of parameter updating time.

#### <span id="page-1-0"></span>**II. PROPOSED SENSORLESS CONTROL AND INDUCTANCE ESTIMATION**

#### A. IPMSM DYNAMIC MODEL

<span id="page-1-1"></span>The three-phase model of the IPMSM can be described as:

$$
V_A = R_A i_A + \frac{d}{dt} (L_{AA} i_A + L_{AB} i_B + L_{AC} i_C + \lambda_f \cos \theta_e)
$$
  
\n
$$
V_B = R_B i_B + \frac{d}{dt} (L_{BA} i_A + L_{BB} i_B + L_{BC} i_C + \lambda_f \cos(\theta_e - 2\pi/3))
$$
  
\n
$$
V_C = R_C i_C + \frac{d}{dt} (L_{CA} i_A + L_{CB} i_B + L_{CC} i_C + \lambda_f \cos(\theta_e - 4\pi/3))
$$
\n(1)

where  $V_A$ ,  $V_B$ ,  $V_C$  are stator voltage of phase A, B and C, respectively;  $i_A$ ,  $i_B$ ,  $i_C$  are the stator current of phase A, B, and C, respectively;  $R_A$ ,  $R_B$ ,  $R_C$  are the stator resistance of phase A, B, and C respectively;  $\theta_e$  is the electrical angle of the rotor;  $\lambda_f$  is the permanent magnet flux linkage;  $L_{AA}$ , *LBB*, *LCC* are the stator self-inductance of phase A, B and C respectively;  $L_{AB}$ ,  $L_{BA}$ ,  $L_{AC}$ ,  $L_{CA}$ ,  $L_{BC}$ ,  $L_{CB}$  are the mutual inductances between respective phases.

$$
L_{AA} = L_{\Sigma} + L_{\Delta} \cos(2\theta_e)
$$
  
\n
$$
L_{BB} = L_{\Sigma} + L_{\Delta} \cos(2\theta_e + 2\pi/3)
$$
  
\n
$$
L_{CC} = L_{\Sigma} + L_{\Delta} \cos(2\theta_e + 4\pi/3)
$$
  
\n
$$
L_{BC} = L_{CB} = -\frac{L_{\Sigma}}{2} + L_{\Delta} \cos(2\theta_e)
$$
  
\n
$$
L_{AB} = L_{BA} = -\frac{L_{\Sigma}}{2} + L_{\Delta} \cos(2\theta_e - 2\pi/3)
$$
  
\n
$$
L_{AC} = L_{CA} = -\frac{L_{\Sigma}}{2} + L_{\Delta} \cos(2\theta_e - 4\pi/3)
$$
  
\n
$$
L_{\Sigma} = \frac{L_{di} + L_{qi}}{3}; \quad L_{\Delta} = \frac{L_{di} - L_{qi}}{3}
$$
 (2)

where  $L_{\sum}$ ,  $L_{\Delta}$  are the average inductance and the magnitude of the inductance variation; *Ldi*, *Lqi* are direct and quadrature incremental inductances respectively.

Assume that during a PWM cycle, the rotor angle of the machine is unchanged, thus the self and mutual inductance are unchanged. (1) can be rewritten as:

$$
V_A = R_A i_A + L_{AA} \frac{di_A}{dt} + L_{AB} \frac{di_B}{dt} + L_{AC} \frac{di_C}{dt} + e_A
$$
  
\n
$$
V_B = R_B i_B + L_{BA} \frac{di_A}{dt} + L_{BB} \frac{di_B}{dt} + L_{BC} \frac{di_C}{dt} + e_B
$$
  
\n
$$
V_C = R_C i_C + L_{CA} \frac{di_A}{dt} + L_{CB} \frac{di_B}{dt} + L_{CC} \frac{di_C}{dt} + e_C
$$
 (3)

where  $e_A$ ,  $e_B$ ,  $e_C$  are back EMF of phase A, B and C, respectively.

### B. ESTIMATION OF ROTOR SPEED AND POSITION BASED ON CURRENT SLOPES

Scalars of the position vector are defined as:

$$
p_A = \frac{2L_{\Delta}}{L_{\Sigma}} \cos(2\theta_e)
$$
  
\n
$$
p_B = \frac{2L_{\Delta}}{L_{\Sigma}} \cos(2\theta_e - \frac{2\pi}{3})
$$
  
\n
$$
p_C = \frac{2L_{\Delta}}{L_{\Sigma}} \cos(2\theta_e - \frac{4\pi}{3})
$$
\n(4)

These scalars of the position vector can be calculated based on the phase current slopes at one active and one zero voltage vector as shown in Table [1](#page-2-0) [\[19\]. T](#page-7-18)he subscript of the equations in Table [1](#page-2-0) indicates the voltage vector where the current slopes are measured. The quantity  $g$  in the equations in Table [1](#page-2-0) can be shown as the function of the DC bus voltage  $(V_{DC})$ , average inductance and the magnitude of the inductance variation as followed:

<span id="page-2-6"></span>
$$
g = \frac{9}{2V_{DC}}(L_{\Sigma}) \left(1 - \left(\frac{L_{\Delta}}{L_{\Sigma}}\right)^{2}\right) \tag{5}
$$

Quantity *g* can be calculated based on the current slopes at two active and one zero voltage vector as shown in Table [2](#page-3-0) by assuming the negligible variation of the rotor position during two consecutive PWM cycles [\[19\].](#page-7-18)

The scalars  $p_{\alpha}$ ,  $p_{\beta}$  of the position vector in the stationary reference frame can be expressed as:

$$
p_{\alpha} = \frac{2p_A - p_B - p_C}{3} = \frac{2L_{\Delta}}{L_{\Sigma}} \cos(2\theta_e)
$$
  

$$
p_{\beta} = \frac{p_B - p_C}{\sqrt{3}} = -\frac{2L_{\Delta}}{L_{\Sigma}} \sin(2\theta_e)
$$
 (6)

<span id="page-2-7"></span>The phase lock loop (PLL) is then used to estimate rotor speed and position. The design details of this PLL is shown in [\[20\].](#page-7-19)

# C. ESTIMATION OF INCREMENTAL AND APPARENT MACHINE INDUCTANCES

The incremental inductances of the machine can be found by solving  $(5)$  and  $(6)$ :

$$
L_{qi} = \frac{gV_{DC}}{3\left(1 - \frac{\sqrt{p_{\alpha}^2 + p_{\beta}^2}}{2}\right)}; \quad L_{di} = \frac{gV_{DC}}{3\left(1 + \frac{\sqrt{p_{\alpha}^2 + p_{\beta}^2}}{2}\right)} \quad (7)
$$

By taking the integral of the incremental inductance, the apparent inductance of the machine can be obtained as:

$$
L_d^{(n)} = \frac{\Phi_d^{(n)}}{I_d^{(n)}} = \frac{\sum_{k=1}^n L_{di}^{(k)} \left( I_d^{(k)} - I_d^{(k-1)} \right)}{I_d^{(n)}}
$$

$$
L_q^{(n)} = \frac{\Phi_q^{(n)}}{I_q^{(n)}} = \frac{\sum_{k=1}^n L_{qi}^{(k)} \left( I_q^{(k)} - I_q^{(k-1)} \right)}{I_q^{(n)}}
$$
(8)

where  $L_d^{(n)}$  $\binom{n}{d}$ ,  $L_q^{(n)}$  are the *d*- and *q*- axes apparent inductances, respectively;  $\Phi_d^{(n)}$  $\mathbf{q}^{(n)}$ ,  $\Phi_q^{(n)}$  are the *d*- and *q*- axes total

<span id="page-2-0"></span>



<span id="page-2-5"></span><span id="page-2-1"></span>

<span id="page-2-2"></span>**FIGURE 1.** Experimental setup.

fluxes, respectively;  $L_{di}^{(k)}$ ,  $L_{qi}^{(k)}$  are the *d*- and *q*- incremental inductances calculated from  $(7)$ , respectively;  $I_d^{(k)}$  $d^{(k)}$ ,  $I_q^{(k)}$  is the *d-* and *q-* current, respectively; *n* is the number of current values from zero to the operating level. The accepted resolution of the discrete integration in [\(8\)](#page-2-4) is determined by *n*. For this study, each integration step is 0.1A.

<span id="page-2-3"></span>It is noted that the update of quantity  $g$  in Table  $2$ determines how fast the estimated inductances are updated. By measuring the current derivatives two active- and onezero voltage vectors during each PWM cycle, quantity *g* and the estimated inductances can be updated at the switching frequency [\[21\].](#page-7-20)

#### <span id="page-2-8"></span>**III. EXPERIMENTAL SETUP AND RESULTS**

#### A. EXPERIMENTAL SETUP

<span id="page-2-4"></span>As shown in Fig. [1,](#page-2-5) the experimental setup includes one tested IPMSM, of which the parameters are shown in Table [3.](#page-3-1) This machine is loaded by the DC motor and the H-bridge. The dSPACE1103 is used to implement the Direct Torque and Flux Control (DTFC) scheme, estimate the rotor speed and position, and the machine inductances. The Anisotropic

#### <span id="page-3-0"></span>**TABLE 2.** Calculation of g.



Magneto-Resistive (AMR) current sensor CMS3005 is used to sense the phase currents. Three Analog to Digital Converter (ADC) 12bits and Field Programable Gate Array (FPGA) ML605 are used to sample the currents from current sensors, estimate the current slopes during every modulated voltage vector and also generate the PWM signals. The block diagram of the sensorless control and inductance estimation is presented in Fig. [2.](#page-4-0)

#### B. CURRENT SLOPE MEASUREMENT

The current slopes are measured by using the least square algorithm:

$$
\frac{di}{dt} = \frac{n \sum_{i=1}^{n} x_i y_i - \sum_{i=1}^{n} x_i \sum_{i=1}^{n} y_i}{n \sum_{i=1}^{n} x_i^2 - (\sum_{i=1}^{n} x_i)^2}
$$
(9)

where  $x_i$  and  $y_i$  represents time and the current sample respectively; *n* is the number of total samplings.

In order to handle the effect of common-mode noise, the high bandwidth current sensors (AMR sensor with the bandwidth of about 2 MHz), high-speed ADCs (50 MSPS) and the RC filter have been utilized. Moreover, the sampling of the current waveforms is delayed until the oscillations in current die out after the switching transition. The duration of high frequency oscillation of the phase current after switching transition for the tested IPMSM (about 20  $\mu$ s under full load) is far longer than that of the PMSM (about  $8\mu s$ ). Therefore, the sampling of the phase current is delayed by 20  $\mu$ s after switching transition. A minimum of pulse width ( $p s min$ ) of 24  $\mu s$  was implemented in order to obtain at least 200 current samples for di/dt calculation, which

#### <span id="page-3-1"></span>**TABLE 3.** Parameters of IPMSMs tested and control system.



can guarantee the satisfactory accuracy of current derivative measurement.

# C. EXPERIMENTAL RESULTS OF THE PROPOSED SENSORLESS CONTROL METHOD

The proposed sensorless control method is compared with the conventional FPE method  $[13]$  in terms of estimation accuracy and the total harmonic distortion of the phase currents.

Fig. [3](#page-4-1) shows the experimental results of the proposed method and the conventional FPE method when the machine operates at 50 rpm under 5.5 Nm (90% of rated torque). Fig. [3](#page-4-1) shows the operation load torque (Machine torque), reference speed (Speed ref), the actual speed (Speed enc), the estimated speed by the proposed method (Speed est), the current slopes of phase A at the first and second active voltage vector (di/dt at V1 and di/dt at V2), and the position estimation error in electrical degree from top to bottom, respectively.

It is obvious that the proposed sensorless method results in the position error within 5 electrical degrees, which is 4 times smaller than the position error (within 20 electrical degrees) resulted by the conventional FPE method. The better accuracy of the proposed method at low speeds can be explained that the more accurate current slopes at the first active voltage vector than at the second active voltage vector are used to estimate the rotor speed and position. In contrast, the conventional FPE method utilizes the current slopes at both first and second active voltage vector during the first haft of a PWM cycle.

The performance of the proposed sensorless method at zero speed under 83% of rated load (5Nm) reversal is presented in Fig. [4.](#page-4-2) The first plot shows the machine torque in Nm; the second plot shows the actual position (Position enc) and the estimated position (Position est); the third plot presents the position estimation error between the actual position and the estimated position; the fourth plot shows speed reference (Speed ref), actual speed (Speed enc) and estimated speed (Speed est); The last plot shows the speed estimation error between the actual speed and the estimated speed.

<span id="page-4-0"></span>

**FIGURE 2.** The block diagram of the proposed sensorless and inductance estimation system.

<span id="page-4-1"></span>

**FIGURE 3.** Experimental results of two sensorless methods at 50 rpm under 90% of rated load (experiment).

It is noted that during the transient, the speed increases to the peak of about 400 rpm; the estimated speed error is within 15 rpm; and the position estimation error is within 25 electrical degrees. During the steady state at zero speed, the position estimation error is within 8 electrical degrees, while the speed estimation error is within 1 rpm.

The performance of the proposed sensorless method with rated speed reversal under no load condition is presented in Fig. [5.](#page-5-0) It is obvious that the position estimation errors during the transient and steady state are within 30 electrical degrees and 5 electrical degrees, respectively.

Fig. [6](#page-5-1) compares the total harmonic distortion (THD) of the phase currents between the proposed sensorless method and the conventional FPE method over the full speed range from zero to rated speed under half load. In general, the total harmonic distortion caused by the proposed method is lower

<span id="page-4-2"></span>

**FIGURE 4.** Performance of the proposed sensorless method at zero speed under 83% of rated load reversal (experiment).

than the total harmonic distortion caused by the conventional FPE method. Especially, at high speed operation the THD of the conventional FPE method is much higher than the proposed method. As an example, at 1500 rpm the THD of the proposed method (2.2%) is about a half of the THD of the conventional FPE method (4.5%). This is explained by the extension of more voltage vectors of the conventional FPE method compared to the proposed methods.

# D. SIMULATION AND EXPERIMENTAL RESULTS OF THE PROPOSED ON-LINE METHOD FOR ESTIMATING MACHINE INDUCTANCES

The proposed inductance estimation method has been verified by simulation and experimental study. Fig. [7](#page-5-2) and Fig. [8](#page-5-3) present the performance of the proposed inductance estima-

<span id="page-5-0"></span>

**FIGURE 5.** Performance of the proposed sensorless method with speed reversal at 1500 rpm under no load condition (experiment).

<span id="page-5-1"></span>

**FIGURE 6.** Total Harmonic Distortion under 50% of rated torque (experiment).

<span id="page-5-2"></span>

**FIGURE 7.** Current derivatives for inductance estimation at 30 rpm under full load (simulation).

tion method when the machine operates at 30 rpm under full load condition. In this loading condition the machine torque is 6 Nm and the RMS phase current is 2.5 A. The off-line measured *L<sup>d</sup>* and *L<sup>q</sup>* are 0.045H and 0.1027H respectively.

Fig. [7](#page-5-2) shows the current slopes at the zero-voltage vector, the first active-voltage vector and the second active-voltage vector of phase A during each PWM cycle. These current slopes are used to calculate the positional vector and g in Table [2](#page-3-0) and [3.](#page-3-1)

Fig. [8](#page-5-3) demonstrates the positional scalars,  $p_{\alpha}$ ,  $p_{\beta}$  and *g* which are used to estimate machine inductances as shown in [\(7\)](#page-2-3). Fig. [8](#page-5-3) also compares the estimated inductances (Ld est, Lq est) with the off-line measured ones (Ld offline, Lq offline), which are set to be the inductances of

<span id="page-5-3"></span>

**FIGURE 8.** Inductance estimation at 30 rpm under full load (simulation).

<span id="page-5-4"></span>

**FIGURE 9.** Inductances estimation with speed acceleration from zero to 1200 rpm under full load (simulation).

the IPMSM model. It is obvious that the errors between estimated inductances and the corresponding inductances of the IPMSM model are smaller than 0.1 mH.

Fig. [9](#page-5-4) shows the performance of the proposed method when the IPMSM accelerates from zero speed to 1200 rpm under full load condition. The off-line measured inductances at full load condition are set in the IPMSM model  $(L_d =$ 0.045 H and  $L_q = 0.1027H$ ). It is obvious that during the steady state and transient state, the estimated inductances follow closely to the reference inductances. The error between the estimated and the references  $L_d$  is smaller than 0.4 mH, while the error between the estimated and the references  $L_q$  is smaller than 0.7 mH.

<span id="page-6-0"></span>

**FIGURE 10.** Inductances estimation of the proposed- and RLS basedmethods (simulation).

<span id="page-6-1"></span>

**FIGURE 11.** On-line estimation of inductances at 300 rpm (experiment).

Fig. [10](#page-6-0) compares the updating time of the proposed method and the recursive least square based method shown 22 by simulation. When running the machine at 500 rpm, the machine inductances  $L_d$  and  $L_q$  suddenly change from 45 mH to 47 mH, and from 102.7 mH to 132.7 mH, respectively. It is obvious that the proposed method results in an instant tracking of the inductance variation, while the method based of RLS algorithm takes about 0.5s to tracks the variation of the inductances.

The estimation accucy of the proposed method was experimentally compared with the off-line method [\[23\] a](#page-7-21)s shown in Fig. [11.](#page-6-1) For the whole range of the operating current from no load (0.25A) to 120% of rated load (3A) the results of two methods are closely matched. The root mean square error (RMSE) of the two methods for the direct axis inductance and quadrature axis inductance are 2.2 mH and 3.8 mH, respectively.

<span id="page-6-2"></span>

**FIGURE 12.** Inductances estimation during the speed acceleration from zero to 900 rpm (experiment).

The machine inductances are estimated by experiment when the machine accelerates from zero to 900 rpm as shown in Fig. [12.](#page-6-2) The estimated  $L_q$  is suddenly dropped from about 133mH to about 110 mH at the start of the acceleration (at time 1.05s), corresponding to the sudden increase of the RMS phase current from 0.9A to 2.8A. When the RMS phase current reduces to about 1.1A after the transient period, the estimated  $L_q$  increases to about 130mH. It is noted that during the transient the variation of the *L<sup>d</sup>* is negligible. The comparison of the online estimated and the offline measured *L<sup>d</sup>* and *L<sup>q</sup>* during steady state and the transient state are also shown in Fig. [12.](#page-6-2) It is obvious that the online estimated inductances track very closely with the offline measured ones.

The results shown in Fig. [12](#page-6-2) demonstrate the very fast inductances estimation (at PWM cycle as presented in section  $\mathbf{II}$ ) and zero speed operation capability of the proposed method.

## **IV. CONCLUSION**

<span id="page-6-3"></span>The paper has presented a sensorless control and online inductance estimation method for IPMSM based on current slopes during the excitation of one active and one zero voltage vector every PWM cycle. With the proposed sensorless method, the estimation accuracy is improved at low speeds and total harmonic distortion of the phase current is reduced over a full speed range, compared to the conventional FPE sensorless method, which utilizes two active and two zero volage vectors for sensorless performance. The measured current slopes at one active and one zero voltage vector are also utilized to estimate machine incremental and apparent direct and quadrature inductances. The high accuracy of the proposed online inductances estimation method during steady and fast transient states was verified by comparing

the estimated inductances with the values measured offline and RLS based online methods. The experimental results also verify the capability of proposed methods in estimating machine inductances during zero speed operation.

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