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# PAACDA: Comprehensive Data Corruption Detection Algorithm

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**ABSTRACT** With the advent of technology, data and its analysis are no longer just values and attributes strewn across spreadsheets, they are now seen as a stepping stone to bring about revolution in any significant field. Data corruption can be brought about by a variety of unethical and illegal sources, making it crucial to develop a method that is highly effective to identify and appropriately highlight the various corrupted data existing in the dataset. Detection of corrupted data, as well as recovering data from a corrupted dataset, is a challenging problem. This requires utmost importance and if not addressed at earlier stages may pose problems in later stages of data processing with machine or deep learning algorithms. In the following work we begin by introducing the PAACDA: Proximity based Adamic Adar Corruption Detection Algorithm and consolidating the results whilst particularly accentuating the detection of corrupted data rather than outliers. Current state of the art models, such as Isolation forest, DBSCAN also called ''Density-Based Spatial Clustering of Applications with Noise'' and others, are reliant on fine-tuning parameters to provide high accuracy and recall, but they also have a significant level of uncertainty when factoring the corrupted data. In the present work, the authors look into the most niche performance issues of several unsupervised learning algorithms for linear and clustered corrupted datasets. Also, a novel PAACDA algorithm is proposed which outperforms other unsupervised learning benchmarks on 15 popular baselines including K-means clustering, Isolation forest and LOF (Local Outlier Factor) with an accuracy of 96.35% for clustered data and 99.04% for linear data. This article also conducts a thorough exploration of the relevant literature from the previously stated perspectives. In this research work, we pinpoint all the shortcomings of the present techniques and draw direction for future work in this field.

**INDEX TERMS** Adamic Adar algorithm, corrupted datasets, outlier detection, probabilistic models, statistical models, unsupervised learning.

#### **I. INTRODUCTION**

Ever since technological evolution dawned upon humankind there has been massive progress in about every domain that the human mind can perceive. The major credit for driving the ongoing technological advancement lies in intensive amounts of data, without which the majority of this industry might come to a standstill [\[1\]. Da](#page-22-0)ta seems to have reached such a

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significant level of importance that, it is often deemed that the companies possessing larger amounts of data seem to have a monopoly in that sector. Data often lays the foundation for the development, growth and maturity of an algorithm or technology. In today's world data is significant to all organizations and thereby it becomes all the more crucial to protect this critical entity from being manipulated by malicious means [\[1\].](#page-22-0)

A dataset can undergo a snowball effect with just a few changes, which could ultimately be detrimental. Even though

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<span id="page-1-2"></span><span id="page-1-1"></span>there are multiple unethical ways to corrupt data, persistent research has been conducted throughout time to identify efficient ways to learn about data corruption, to name a few commendable works in detecting data corruption including [\[2\],](#page-22-1) [\[3\], \[](#page-22-2)[4\], an](#page-22-3)d [\[5\]. B](#page-22-4)efore figuring out a unique approach for identifying data corruption we delved deep into other pre-existing methods available for the detection of data corruption primarily concerning outliers. The deep study of various approaches provided us with insightful knowledge of various algorithms having varying levels of accuracy when tested against the dataset containing corrupted data rather than outliers.

K-means clustering uses clusters and their centroids as part of an unsupervised technique to address issues with categories and their classification [\[6\], \[](#page-22-5)[7\]. D](#page-22-6)BSCAN is another clustering-based technique however it tends to perform well with data containing clusters with similar density, as it finds core samples of high density and expands upon them. When applied to identify outliers in the supplied dataset, both of these methods provided a satisfactory level of accuracy  $[8]$ ,  $[9]$ .

<span id="page-1-4"></span>Moving along the research we started exploring methodologies such as Isolation forest, Elliptic envelope outlier detection and histogram-based outlier detection. Isolation forest provides us with an algorithm through which we can partition the dataset features in order to identify the outliers which exceed the defined range [\[10\], \[](#page-22-9)[11\]. T](#page-22-10)he Elliptic envelope model tends to create an ellipse around the scatter plot for the dataset and all points lying outside its boundaries signify the outliers present in the dataset [\[12\], \[](#page-22-11)[13\]. A](#page-23-0)nother approach involving plotting and analyzing histograms is the Histogram based algorithm for outlier detection (HBOD) method which is also an effective unsupervised method to detect anomalies. These algorithms also have a fairly decent level of accuracy in terms of identifying anomalies in the dataset [\[14\], \[](#page-23-1)[15\].](#page-23-2)

<span id="page-1-10"></span><span id="page-1-7"></span>Algorithms such as 'Principal Component Analysis' (PCA),'DeepSVDD' and 'Rotation based Outlier Detection'(ROD) were also looked at to tabulate the level of accuracy in predicting the outliers for the synthetically generated dataset. To name a few PCA [\[16\], \[](#page-23-3)[17\], R](#page-23-4)OD [\[18\], \[](#page-23-5)[19\], L](#page-23-6)ocal Outlier Factor [\[20\], \[](#page-23-7)[21\], D](#page-23-8)eepSVDD [\[22\], \[](#page-23-9)[23\] a](#page-23-10)nd more were used. In spite of the distinct strategies given out by various models, the unique methods proposed as a part of this research stood out in the following metrics Accuracy, Recall, Precision, Sensitivity and F1 score.

Adamic Adar is a promising algorithm for data correlation in graph networks and hence has increasing amount of potential in data corruption detection. The study mentioned above led to the realization that it is feasible to avoid the current work's inefficiencies. The motivation behind this work would be to consolidate the current work in this field of study and enhance the accuracy of the present corruption detection algorithm by leveraging the Adamic Adar algorithm's prominance in data correlation. The novel method proposed as a part of the research largely revolves around a graph-based algorithm <span id="page-1-13"></span><span id="page-1-12"></span>is Adamic Adar. Adamic Adar gives us access to the Adamic Adar index, which aids in anticipating links, particularly in areas like social networks [\[24\]. B](#page-23-11)y taking into account how many common links there are between two nodes, the Adamic Adar index is determined [\[25\]. T](#page-23-12)he research puts forth a modified approach of Adamic Adar called PAACDA (Proximity based Adamic Adar Corruption Detection Algorithm) which when put into use detect the data corruption provides us with the best accuracy compared to the above-mentioned algorithms.

<span id="page-1-3"></span>After a deep study involving the existing methods for the detection of corruption and the novel method presented as a part of this research work, attention was diverted towards figuring out feasible methods to revert back to the original data for the ones deemed as corrupt. However, this is beyond the scope of this study. The linear regression approach works considerably well for two attributes datasets for data regneration however most datasets deal with humongous amounts of data consisting of multiple features. GANs (Generative Adversarial Networks ) can be a plausible approach to regenerating corrupted data using the generator and discriminator model [\[26\], \[](#page-23-13)[27\]. H](#page-23-14)owever, utilizing the various evolved forms of GAN, mainly tabular GANs in order to address the problems of regeneration of contaminated still remains unexplored.

<span id="page-1-14"></span><span id="page-1-6"></span><span id="page-1-5"></span>The remainder of this article is divided into the following sections. After highlighting some related work about the approaches taken into consideration for this study in Section [II,](#page-1-0) we go on to illustrate the data and methods used in Section [III,](#page-2-0) as well as the proposed methodology to tackle the issue in Section [IV.](#page-12-0) In Section [V,](#page-13-0) we put forth the results that indicate the cogency of our strategies, and in Section [VI,](#page-20-0) we present the conclusions and future scope of this research.

#### <span id="page-1-0"></span>**II. RELATED WORK**

<span id="page-1-11"></span><span id="page-1-9"></span><span id="page-1-8"></span>A key area of research that has numerous practical applications is anomaly identification in a given dataset. As a result, this topic has frequently been the focus of research. Multiple approaches utilizing various aspects of the dataset have been proposed to detect anomalies however only few methodologies lay emphasis on the detection of corrupted data which would further provide the most efficient results with respect to varying dataset sizes, higher dimensionality or varying degrees of corruption present. A study by Chandola et al. in their publication [\[2\] com](#page-22-1)pares numerous anomaly detection methods for diverse applications. By contrasting the benefits and drawbacks of various techniques, Hodge and Austin [\[28\] c](#page-23-15)onducted a review of outlier detection methods. An overview of cutting-edge methods for spotting suspicious behaviour is presented by Patcha and Park [\[29\]](#page-23-16) Jiang et al. [\[30\] to](#page-23-17)gether with detection scenarios for several real-world settings.

<span id="page-1-18"></span><span id="page-1-17"></span><span id="page-1-16"></span><span id="page-1-15"></span>Dimensionality reduction approaches and the underlying mathematical understandings are categorized by Sorzano et al. [\[31\]. T](#page-23-18)he issues with anomaly detection are further laid out by a number of other reports, including papers

<span id="page-2-5"></span><span id="page-2-2"></span>by Gama et al. [\[32\], G](#page-23-19)upta et al. [\[33\], H](#page-23-20)eydari et al. [\[34\],](#page-23-21) Jindal and Liu  $[35]$ , and many more.

<span id="page-2-7"></span>Outliers make up the majority of anomalies that can exist in a dataset. The first method based on distance for detection of outliers was put forth by Knorr et al. [\[36\], a](#page-23-23)nd Ramaswamy et al. [\[37\] e](#page-23-24)xpanded on it by suggesting that the greatest n locations with highest Pk be supposed outliers (Pk(p) signifies the kth nearest neighbour corresponding to p). They used a clustering technique to separate a dataset into several categories. To improve the success of outlier detection for these groups, batch processing and pruning may be beneficial [\[38\]. D](#page-23-25)eviation-based outlier detection was another method that was suggested for effectively detecting outliers. Objects or data points that vary significantly from the bulk of data points constitute outliers. Therefore, outliers are frequently called deviations [\[39\] a](#page-23-26)s given by the name deviation-based outlier detection.

<span id="page-2-11"></span><span id="page-2-10"></span><span id="page-2-8"></span>Several other methods have been invented over the years to detect anomalies, to name Breunig et al. [\[21\] d](#page-23-8)eveloped a method based on density. Cluster-based anomaly identification methods pinpointed anomalies by eliminating clusters from the actual dataset  $[40]$  or by classifying small clusters as outliers [\[41\]. A](#page-23-28)dditionally, Aggarwal and Yu [\[42\] p](#page-23-29)roposed a novel strategy for catching outliers that is remarkably effective for extremely elevated dimensional datasets. Their methodology focuses on finding locally sparse lower dimensional projections which are otherwise difficult to differentiate using brute force methods due to the vast amount of possible combinations. However, the study is inclined towards detection of outliers and does not focus on the detection of corrupted or modified datasets.

<span id="page-2-13"></span>Li et al. [\[43\] i](#page-23-30)n their paper proposed a unique outlier detection approach called 'Empirical Cumulative distribution-based Outlier Detection' (ECOD). This method uses the empirical cumulative distribution to measure outlier values present in the dataset. They extensively applied it to 30 datasets which showed that ECOD outperformed the existing state of the model as it is fast and scalable. However, the method doesn't deal with an outlier that might not be in either the left or right tails and demands readers to come up with another promising route that is, to find a mechanism to expand ECOD to such environments while keeping it quick and scalable.

The bulk of them, meanwhile, are primarily focused on outlier identification without paying much attention to data that contains corrupted values. Many cutting edge poisoning and outlier identification practices have been developed and they may generally belong to one of the following categories: distribution based [\[43\],](#page-23-30) [\[44\],](#page-23-31) [\[45\], d](#page-23-32)epth based [\[46\], d](#page-23-33)istance based [\[47\], \[](#page-23-34)[48\], \[](#page-23-35)[49\], d](#page-23-36)ensity based [\[50\], \[](#page-23-37)[51\], c](#page-23-38)lusterbased [\[52\], \[](#page-23-39)[53\], \[](#page-23-40)[54\] an](#page-23-41)d generative models [\[55\].](#page-23-42)

Thus in this work the following research objectives have been addressed:

<span id="page-2-18"></span><span id="page-2-16"></span>• To explore the efficacy of various unsupervised models to detect the corrupted data in an efficient manner and provide a comprehensive and detailed review.

<span id="page-2-4"></span>• To propose a novel method PAACDA, an unsupervised model to detect corrupted data in a more accurate manner.

<span id="page-2-6"></span><span id="page-2-3"></span>Despite the many different approaches that have been suggested, each of which has its own set of benefits and downsides, the search for the ideal, all-encompassing algorithm never seems to stop. However, here we present a novel practice that, when thoroughly compared to prior current edge approaches and evaluated against various sets of data sizes, yields satisfactory to superior results.

# <span id="page-2-0"></span>**III. MATERIALS AND METHODS**

In the section [III](#page-2-0) we put forward our proposed approach to pursue the data corruption detection problem. We elucidate the process in detail in the subdivisions below. An overview of our approach is illustrated in FIGURE [1.](#page-2-1)

<span id="page-2-12"></span><span id="page-2-9"></span><span id="page-2-1"></span>

**FIGURE 1.** llustration of proposed methodology.

# A. EXPERIMENTAL ENVIRONMENT

<span id="page-2-21"></span><span id="page-2-20"></span>All the tests were implemented on GoogleColab, Python 3.7.13 [\[62\] ve](#page-24-0)rsion was used for implementing all the algorithms. We used Keras [\[63\] ba](#page-24-1)ckend as the deep learning framework. We plan to make the research and dataset fully reproducible on GitHub to the research community.

# B. DATASETS AND CORRUPTION TECHNIQUE

The scikit-learn library for Python was used to create the synthetic datasets utilised in the following study. The datasets are linear and clustering in nature. Testing must be done on a wide variety of data and corruption rates in order to detect corrupted data in datasets that have been tainted. We use univariate data produced especially for this research paper. The authors would like to mention that this research work focuses solely on corrupted data and not just outliers and anomalies unlike the work mentioned above. However, the corrupted data may contain outliers and anomalies as part of the corruption. In light of this, we will now provide a description of our curated dataset and a discussion of the curation methods.

<span id="page-2-19"></span><span id="page-2-17"></span><span id="page-2-15"></span><span id="page-2-14"></span>The linear dataset has the following parameters:

- Number of features  $=1$
- Noise  $= 10$
- The graph for the same is shown in FIGURE [2.](#page-5-0)

The clustering dataset has the following parameters:

• Number of features  $= 2$ 

<span id="page-3-0"></span>





# **TABLE 1.** (Continued.) A review of prominent data corruption detection techniques based on different algorithms.

<span id="page-5-0"></span>

<span id="page-5-1"></span>**FIGURE 2.** Representing linear generated data for small dataset.



**FIGURE 3.** Representing clustering data generated for small dataset.

- Number of centres  $= 5$
- The graph for the same is shown in FIGURE [3.](#page-5-1)

The datasets are of 3 different sizes:

- 10,000 samples (Small)
- 40,000 samples (Medium)
- 75,000 samples (Medium-Large)

The datasets are further categorised on the basis of the percentage of corruption:

- 20 % corrupted values
- 40  $%$  corrupted values
- 60 % corrupted values

<span id="page-5-5"></span>



Thus in the present work, a total of 18 datasets of varying sizes and corruptions were used to demonstrate the impact on the 16 underlying models and our proposed Proximity based Adamic Adar Corruption Detection Algorithm (PAACDA). The data points in these provenant datasets are corrupted at random in every conceivable way, including by substituting fake values for actual ones, outliers, and missing data (0 or NaN). The most fundamental form of data corruption includes deleting the data from the datasets, which is similar to how lost system data is frequently experienced. This is extended to more complex situations, including replacing the original value with exaggerated and incorrect ones. To explore in more detail, a piece of code is used to randomly select cells with random rows and columns and replace them with a completely random value. The final contaminated dataset is then retrieved, and different techniques are applied to precisely predict and address the corrupted values.

# 1) Realistic Data

The authors also conducted the data corruption detection analysis on a Realistic dataset to improve the practicality of the proposed methodology. The dataset used here is a standard corruption detection dataset - ''The Complete Pokemon dataset'', with 802 instances and a 3% corruption rate. The dataset was not additionally or synthetically corrupted. The various corruption detection models along with PAACDA were applied to preceisely predict the corrupted values.

#### C. METHODS

# <span id="page-5-7"></span><span id="page-5-6"></span>1) LOCAL OUTLIER FACTOR

<span id="page-5-8"></span>LOF is a type of density-based system [\[64\]. O](#page-24-2)utliers are segregated in density-based [\[65\], \[](#page-24-3)[66\] sy](#page-24-4)stems because anomalies emerge in low-density areas [\[67\]. L](#page-24-5)OF compares a location's local density to that of k of its neighbours, indicating points with considerably lower density than their neighbours.

As Breunig et al. [\[21\] in](#page-23-8) their work emphasised LOF as quite promising as it can detect relevant local outliers that earlier techniques could not find. They demonstrated that their strategy of discovering local outliers is effective for the datasets with closest neighbour searches. For other objects, they provide strict upper and lower constraints on the value of LOF, irrespective of if the MinPts nearest neighbours are from single or several clusters. In addition, they investigated the effect of MinPts parameter e on the value of LOF. The experimental findings show that their heuristic is effective. Eq. [\(1\)](#page-5-2) calculates Average RD(Reachability Density) and

Eq. [\(2\)](#page-5-3) calculates Local RD which is reciprocal of RD.

$$
A(u, v) = \frac{1}{k} \sum \max( kth\_distance of \_A's\_neighbor, \\ distance(A, kth\_neighbor))
$$
 (1)

$$
LRD = \frac{1}{RD} \tag{2}
$$

Furthermore, we obtain LOF as in Eq. [\(3\)](#page-5-4), using which the points are classed as an outlier(-1) or not  $(1)$  [\[68\].](#page-24-6)

<span id="page-5-11"></span><span id="page-5-10"></span><span id="page-5-9"></span><span id="page-5-4"></span><span id="page-5-3"></span><span id="page-5-2"></span>
$$
LOF = \frac{1}{k} \frac{\sum_{i=0 \text{ to } k} LRD(i)}{LRD(A)} \tag{3}
$$

Typically, We usually recognise A as an anomaly when its LOF is lower than that of its k neighbours [\[69\], \[](#page-24-7)[70\], i.](#page-24-8)e. when LOF>1.1, albeit this depends on the context.

Lee and Tukhvatov [\[71\] fu](#page-24-9)rther proposed three augmentation schemes which are the LOF', LOF'', and GridLOF which optimised known state of the art model, LOF. By offering a new computation technique to find neighbours, the LOF''

<span id="page-6-0"></span>

**FIGURE 4.** Representing corrupted data detected using various methods.

addresses scenarios that the LOF cannot effectively handle. By trimming inliers, the GridLOF enhances the efficacy of outlier identification. Because of its intricacy, this approach has several drawbacks, including a lengthy run time.

In the present work and on experimentation, the improved LOF resulted in a performance of 59.47% on the clustering dataset and 58.79% for linear data with a corruption rate of 20%, decreasing as the corruption percentage grew and imperceptible change in accuracy as the dataset size increased.

FIGURE [4\(a\)](#page-6-0) Shows the resulting corrupt data detected using the model.

# 2) ONE-CLASS SVM

<span id="page-6-2"></span><span id="page-6-1"></span>For the past decade, SVM has been one of the most effective machine learning approaches. To discriminate between distinct classes of data, SVMs [\[72\] u](#page-24-10)se hyperplanes in multidimensional space. Naturally, SVM is utilised to handle multi-class classification challenges [\[73\]. S](#page-24-11)emi-supervised variant of SVM, i.e One-Class SVM exists for the anomaly

detection. In this case, the algorithm has been trained to comprehend ''normal,'' so that whenever new data is provided, it will determine if or not it must be included. Otherwise, the new data is labelled as anomalous or out of the norm.It employs the One-vs-All Anomaly Detection concept. It effectively optimises the distance from this hyperplane to  $(0,0)$  while keeping all data points away from the  $(0,0)$ (in feature space F). As a result, a binary function is generated that may detect input points where the density of the data is discovered. As a result, in a small region, it returns  $+1$ , and  $-1$ for others  $[74]$ ,  $[75]$ ,  $[76]$ . FIGURE  $4(b)$  depicts the model's detection of fraudulent data. Kernels can also be used to scale data to a higher dimensional for improved performance.

<span id="page-7-3"></span>However, it has been found that a one-class SVM is prone to data outliers. Amer et al. [\[75\] in](#page-24-13) their paper, apply two changes to one-class SVMs to make them more suited for unsupervised anomaly identification: robust and eta one-class SVMs. The main notion behind these changes is that outliers should influence less than regular cases. According to the research on UCI machine learning collections, their alterations are quite promising: The upgraded one-class SVMs outperform other standard unsupervised anomaly detection techniques on 2 of 4 datasets. The suggested eta one-class SVM in particular has yielded encouraging results. In the present work and on experimentation, the One-Class SVM achieved 76.82% on the clustering dataset and 72.28% for linear data with a corruption rate of 20%, dropping as the corruption percentage rose and showing no discernible change in accuracy as the dataset size increased. FIGURE  $4(b)$  Shows the resulting corrupt data detected using the model.

#### 3) K-MEANS CLUSTERING

<span id="page-7-4"></span>Another well-known state of the art model wherein the data are divided into k groups in the K-means-based outlier identification [\[77\] a](#page-24-15)pproach by allocating them to the closest cluster centres. Once assigned, we can calculate how far each item is from the cluster's centre and select those with the largest gaps as outliers. It determines the distance and its associated centroids. After determining the distance, the threshold ratio is chosen as a percentile. The data is deemed poisoned if the threshold ratio is exceeded.

The Elbow procedure is an empirical method to get the best value of k. Here, a metric known as ''Within Cluster Sum of Squares" (WCSS)  $[78]$  as shown in Eq. [\(4\)](#page-7-0) is determined with respect to its cluster centroid and recorded.

<span id="page-7-5"></span>
$$
WCSS(m) = argomin \sum_{j=1}^{n} \sum_{y_i \in cluster} ||y_i - \bar{y}_j||^2
$$
\n(4)

where o is the collection of observations, m is the total set of predictors,  $y_i$  is the observational data point in cluster i and  $\bar{y_i}$ is the sample mean in the cluster i [\[79\].](#page-24-17)

The K-means algorithm should be manually supplied or must employ additional procedures with the number of clusters. Instead of finding global optimum solutions for nonconvex problems, the K-means method becomes trapped on local optimum solutions. As Xiong et al. [\[80\] in](#page-24-18) their paper

<span id="page-7-1"></span>

**FIGURE 5.** The corrupted data detected using K-means Clustering.

for optimisation of initial clusters centers of text classification came up with an algorithm wherein the density parameter of the data items was used to calculate the first cluster centres, ensuring the logic of the initial cluster centres. Their new approach, to a considerable part, decreased the susceptibility of the K-means algorithm to the original cluster centres and produced improved text clustering results.

<span id="page-7-8"></span>When there are anomalies in the data, they do have a crucial impact on all cluster centroids as it focuses on the mean of the values for its centre  $[80]$ ,  $[81]$ . Hence, the groups that would be made in the presence and absence of these outliers would vary greatly. The distances of the values from the centres would also vary and a new set of corrupted outliers would be produced every time. In the present work and on experimentation, the K-Means obtained 86.06% on the clustering dataset and 86.70% for linear data with a corruption rate of 20%, declining as the corruption percentage grew and demonstrating no discernable change in accuracy as the dataset size increased. FIGURE [5](#page-7-1) depicts the model-detected faulty data.

#### 4) ISOLATION FOREST

<span id="page-7-9"></span>An Isolation Tree is a Random Forest variant that may be utilised for anomaly identification. They extract one random characteristic at a time and divide it into homogenous partitions. However, the goal of Isolation Forest [\[82\], \[](#page-24-20)[83\],](#page-24-21) [\[84\] is](#page-24-22) not to create homogeneous partitions, but rather to create partitions in which each datapoint is isolated (That particular isolation contains only the datapoint). The rationale underlying Isolation Trees is that a regular point is more difficult to isolate than an aberrant one.

<span id="page-7-0"></span>During the training phase of this approach, we take a sample of the data and generate an itree till each point is visited. Choose a feature at random and split it along at random. The forecast is then completed by calculating the Anomaly Scores as given in Eq.  $(5)$  for the new points  $[85]$ .

<span id="page-7-10"></span><span id="page-7-2"></span>
$$
S(x1, n1) = 2^{\frac{E(p(x1))}{c(n1)}}
$$
 (5)

- <span id="page-7-6"></span>• x1: data point
- n1: sample size
- $PS(x1,n1)$ : Prediction Score
- E( $p(x1)$ ): iTrees average search heights for x
- <span id="page-7-7"></span>•  $c(n1)$ : Average value of  $p(x)$

The samples that travelled farther into the tree are less likely to be abnormal since it requires more cuttings to separate them. Shorter branches are likely to include anomalies since the tree finds it easier to identify them from other data [\[86\].](#page-24-24)

<span id="page-8-1"></span>If 
$$
E(p(x1) \ll c(n1)) = > PS(x1, n1) = 1 \implies
$$
 Anomaly  
If  $E(p(x1)) = c(n1) = > PS(x1, n1) = 0.5 \implies$  Regular

As a result, Isolation Forest produces a score bound in the range of 0 to 1, where values close to 1 are regarded Anomalous and values less than 0.5 are considered Regular. However, the values produced by sklearn [\[86\] h](#page-24-24)ave an inverted interpretation, i.e. numbers less than −0.5 are more regular while values more than −0.5 are more likely to be anomalous. In the present work and on experimentation, the Isolation Forest achieved 82.37% on the clustering dataset and 82.2% with a corruption rate of 20%, with accuracy decreasing as the corruption percentage rose and showing no discernible change as the dataset size increased. The model-detected erroneous data is depicted in FIGURE [4\(c\).](#page-6-0)

# 5) DENSITY-BASED SPATIAL CLUSTERING OF APPLICATIONS WITH NOISE(DBSCAN)

The abbreviation DBSCAN refers to Density-Based Spatial Clustering of Applications with Noise [\[87\]. I](#page-24-25)t is an unsupervised technique that divides a set of points into sets with comparable qualities. It uses density-based clustering to find outliers that do not fit into any of the clusters or sets  $[88]$ ,  $[89]$ . FIGURE [4\(d\)](#page-6-0) Shows the resulting corrupt data detected using the model.

<span id="page-8-3"></span>DBSCAN takes in 2 input parameters-

- ε
- <span id="page-8-4"></span>• minpts $()$  [\[90\], \[](#page-24-28)[91\]](#page-24-29)

where  $\varepsilon$  represents the radius of the circle formed with data object as centre and minpts() represents the number of points inside the circle.

As a result, three types of datapoints are obtained

(i) Core point - Satisfies the input requirements.

(ii) Boundary point - the core point's neighbour.

(iii) Noise point - Neither centre nor border.

The DBSCAN starts by determining the surroundings starting from an unexplored, random starting point. If the point has enough the neighbours the clustering begins and is labelled as visited or else the point is labelled as noise. This procedure is repeated until all points in a cluster have been realised and all points have been marked visited.

In the present work and on experimentation, the DBSCAN obtained 39.60% accuracy on the clustering dataset and 43.20% with a 20% corruption rate, with accuracy falling as the corruption percentage grew and displaying no noticeable change as the dataset size increased. FIGURE [4\(d\)](#page-6-0) depicts the model-detected incorrect data.

# 6) ELLIPTICAL ENVELOPE

<span id="page-8-5"></span>The basis of the Elliptical Envelope algorithm is to create a hypothetical oval shape similar to an ellipse around the given dataset values [\[92\]. T](#page-24-30)he points which fall inside the elliptical shape are regarded as normal data and the values in the dataset outside the elliptical shapes are considered outliers or anomalies. This unsupervised algorithm is mostly used on a gaussian distributed dataset. To find out the data points which are at a further distance from the boundary of the shape minimum-covariance matrix is found. FIGURE  $4(e)$  Shows the resulting corrupt data detected using the model.

In essence, the Elliptical Envelope algorithm fits a Gaussian onto the data and then tries to find the outliers which are the data points which do not fit adequately. Since this is primarily intended to be used for the outlier detection job, our aim is to fetch a reliable estimation of the mean and covariance matrix that will allow us to accept certain outliers in the training dataset while still attempting to recover the true covariance matrix. The Mahobalies distance *dMH* is used to obtain the distance measure between an instance 'P' and a given allocation denoted by 'D'. It is computed with respect to all the multidimensional data vector x, and the resultant distances $(d_{MH})$  are sorted in ascending order. The *dMH* calculated is then used to define a threshold in order to define a boundary which would classify the data points as normal or anomalous. Mahalanobis defined ''Mahalanobis distance" [\[93\], \[](#page-24-31)[94\] as](#page-24-32) shown in Eq.  $(6)$ .

<span id="page-8-8"></span><span id="page-8-7"></span><span id="page-8-6"></span><span id="page-8-0"></span>
$$
d_{MH} = \sqrt{(y - \mu)^{T} (C)^{-1} (y - \mu)}
$$
(6)

<span id="page-8-2"></span>where C denotes the covariance matrix. When the covariance is equal to the identity matrix, *dMH* simplifies to Euclidean distance [\[95\] an](#page-24-33)d if a covariance matrix is a diagonal matrix, to the normalized Euclidean distance [\[96\].](#page-24-34)

In the present work and on experimentation, the Elliptic Envelope outlier detection algorithm has performed significantly well for datasets of varying sizes and levels of corruption. It delivered an accuracy of about 86% for datasets of smaller size but 60% corruption rate. It kept up its consistency in the identification of corruption for medium and big datasets as well, maintaining an accuracy of about 80% and 85%, respectively, for the datasets injected with 60% corruption rate.

#### 7) ROTATION-BASED OUTLIER DETECTION

<span id="page-8-11"></span><span id="page-8-10"></span><span id="page-8-9"></span>'Rotation Based Outlier Detection' or ROD is an approach that can be used for anomalies and outliers' detection in multivariate data. ROD was first designed to deal with scenarios such as complicated outliers concealed in subspaces [\[97\], \[](#page-24-35)[98\], t](#page-24-36)aking into account data generated by disparate means [\[99\], a](#page-24-37)nd smoothing the detection of outliers in higher dimensions that would otherwise go unnoticed [\[100\].](#page-24-38) The robust approach known as ''rotation-based outlier detection'' rotates the three-dimensional (3D) vectors that represent the data points twice counterclockwise around the geometric median. This rotation is done in accordance with

the Rodrigues rotation formula [\[101\].](#page-24-39) The rotation produces parallelepipeds, the volumes of which are investigated using mathematical means such as cost functions and utilized to determine the median absolute deviations and generate the outlier score. When the original data space is divided into 3D subspaces, the total score is determined by averaging the 3D-subspace scores for high dimensions. FIGURE [4\(f\)](#page-6-0) Shows the resulting corrupt data detected using the model. The algorithm performed fairly well for datasets of varying sizes having lower level of corruption. As per the tests run by the authors ROD provided an accuracy around 62.71% in detecting corruption for clustering data and 62.83% for linear data with 20% corruption, however the accuracy drastically declined as the level of corruption was increased keeping the dataset size fixed.

# 8) PRINCIPAL COMPONENT ANALYSIS

Principal component analysis or PCA is a traditional mathematical approach where the data matrix is split into principal components. The principal components' poor interpretability and the trade-off between losing crucial information/data and reducing dimensionality, which has a powerful impact on the accuracy, are the main reasons why the method is significantly less effective than other approaches when applied to the synthetic datasets used in this study. The disadvantages of this technique are exacerbated by the requirement to provide the dataset's contamination rate in order to identify outliers. The key elements can be used in multiple situations. As demonstrated in this work, ''Principal Component Analysis'' (PCA), which is frequently utilized for exploratory analysis and dimension reduction, can also be used to detect corrupted data. FIGURE  $4(g)$  Displays the model's detection of corrupt data.

Principal Component Analysis is primarily used to decrease the dimensionality for the dataset which consists of numerous variables that are correlated, whilst simultaneously retaining the variation and essence of the original dataset. This feat is reached by converting into a new set of variables that are principal components which are not much correlated as well as ordered such that the first few hold the majority of the variation with respect to original variables [\[102\].](#page-24-40) FIGURE [6](#page-9-0) adequate puts forth the basic steps in order to

<span id="page-9-0"></span>

**FIGURE 6.** The steps involved in PCA.

<span id="page-9-5"></span><span id="page-9-3"></span>use PCA for dimension reduction [\[103\],](#page-24-41) [\[104\],](#page-25-0) [\[105\],](#page-25-1) [\[106\].](#page-25-2) Anomaly detection using PCA is based on the decomposition of data metrics, However, anomaly detection using this technique is mostly restricted to numerical data which is also one of the drawbacks of this methodology. The various tests conducted as a part of this research to measure the effectiveness of PCA for detection of data corruption revealed some astonishing results. As the level of corruption was increased from 20% to 60% for small, medium and large data sized a significant drop in detecting corruption was observed.The accuracy dropped from around 70% for 20% corruption to around 15-20% for 60% corruption across datasets of all sizes. Thus highlighting the algorithms effectiveness in situations where there are highly corrupted datasets.

# 9) DEEP SUPPORT VECTOR DATA DESCRIPTION

Deep support vector data description(DeepSVDD) approach proposes a modification of support vector data description model which is another traditional paradigm for anomalies detection. DeepSVDD employs a specific type of neural network to learn appropriate data representations. To distinguish between regular and anomalous data, DeepSVDD [\[107\]](#page-25-3) employs the hyper-sphere rather than the hyper-plane. DeepSVDD extracts discriminative features from the initial data using a neural network.

$$
\min \frac{1}{n} \sum_{i=1}^{n} ||\phi(x_i; W) - a||^2 + \frac{\lambda}{2} \sum_{b=1}^{L} (||W^b||_F)^2
$$
\n(7)

In Eq.  $(7)$ , "a" represents the center of the sphere, x represents features extracted and W being the weights of the hidden layers and subscript F represents Frobenius norm which cycles through all the entries, adds their squares and then takes the square root as represented in Eq.  $(8)$ .

<span id="page-9-8"></span><span id="page-9-7"></span><span id="page-9-6"></span><span id="page-9-2"></span><span id="page-9-1"></span>
$$
||A||_F = \sqrt{\sum_{i=1}^n \sum_{j=1}^m |aij|^2}
$$
 (8)

<span id="page-9-4"></span>The first part of Eq.  $(8)$  [\[108\]](#page-25-4) reflects the loss which varies with the distance to the sphere's centre. The next term denotes a W decay regularizer with  $> 0$  inserted as a hyperparameter. The Python PyOD library's Deep SVDD, which was employed to test this model, calls for the specification of the contamination or corruption rate. The default hyper-parameters offered by the PyOD module serve as the foundation for the results that the deepSVDD generates on the aforementioned datasets which are trained for 100 epochs.

DeepSVDD is used to train a neural network [\[109\],](#page-25-5) [\[110\],](#page-25-6) which reduces the size of the hypersphere that surrounds the data network representations, driving the network to identify recurring sources of variation. DeepSVDD, like PCA, may be used to discover outlier items in data by calculating their distance from the center. FIGURE  $4(h)$  depicts the model-detected faulty data. DeepSVDD when tested on detection of corruption did not show much deviation in the accuracies for different size and rate of corruption for

the dataset. In the present work and on experimentation, it gave an accuracy of 70-75% for 20% corruption of small, medium and large datasets which only dropped slightly to around 50-55% for 40% and 60% corruption for small and medium sized datasets. Whereas it maintained a consistent accuracy of around 70% for large datasets with varying corruption rates.

# 10) LUNAR

<span id="page-10-7"></span>LUNAR stands for Learnable Unified Neighbourhood-based Anomaly Ranking [\[60\], i](#page-24-42)t develops a trainable method for using data from each node's closest neighbours to detect anomalies. Along with the PAACDA algorithm, LUNAR is another graph-based outlier detection technique that offers comparable comparison points.

The LUNAR is unified using K-NN, DBSCAN, LOF and GNNs to provide a faster computing speed and better performance. The outlier score for the KNN is given by Eq. [\(9\)](#page-10-0). Where y is the data sample and n is the number of neighbours.

$$
KNN(y_i) = dist(y_i, y_i^2)
$$
\n(9)

The outlier score for the LOF factor is given by the Eq. [\(10\)](#page-10-1) where lrd is ''local reachability density''.

$$
LOF(y_k) = \frac{\sum_{i \in D} l r d_j(y_i)}{|D_k| l r d_j(y_i)}
$$
(10)

The edges in the graph component are computed using the Eq. [\(11\)](#page-10-2) which is the Euclidean distance of the 2 points, where  $y_i$  and  $y_j$  are the two data samples and N is the number of neighbours.

$$
e_{i,j} = dist(y_i, y_j \text{ if } j \in N_j), 0 \quad otherwise \tag{11}
$$

The K closest neighbours of a sequence of data points are produced as input to the neural network. Finding the k nearest neighbours is one of LUNAR's limitations, as it is with all local outlier approaches. This is mostly a problem in extremely high-dimensional spaces, but because the aforementioned datasets have smaller dimensions, the LUNAR model outperforms conventional probabilistic models in these situations. Other outlier detectors like the local outlier factor (LOF) and DBSCAN have been compared to LUNAR. However, we will focus on the detection of damaged data in tainted datasets in this paper rather than just outliers. In the present work and on experimentation, LUNAR models seems to have performed fairly well in small, medium and large datasets for 20% corruption rate and thereby provided an accuracy of around 85-87%. However the accuracy dropped to about 70% for 40% corruption rate and subsequently to around 50% when the level of corruption was increased to 60% in the datasets. FIGURE  $4(i)$  Shows the resulting corrupt data detected using the model.

#### 11) EMPIRICAL CUMULATIVE OUTLIER DETECTION

It is important to note that for outlier detection with the Empirical Cumulative distribution function, there is a class <span id="page-10-8"></span>called ECOD (Empirical Cumulative Outlier Detection) [\[43\].](#page-23-30) ECOD is a highly interpretable approach for outlier detection and requires no parameters. The synthetically generated datasets have a rather high sensitivity metric when this method is applied to them. Here the investigators formulated that one of the algorithm's important characteristics is that there are no hyper-parameters, which makes it simpler to implement [\[111\].](#page-25-7) However, the function in the Python PyOD package also requires the definition of the corruption percentage, just like other statistical approaches. The authors proposed that ECOD [\[43\] w](#page-23-30)as easily interpretable by looking at the left or right tailed probability which was highly optimised as both of them contributed to the total outlier score. Thus the importance of the tailed probabilities was illustrated in the work we drew inspiration from and thus gained crucial results. In the present work and on experimentation, the optimized ECOD led to a performance of 82.71% on the clustering dataset and 82.30% for linear data with a corruption rate of 20%, decreasing with increase in corruption percentage and indistinguishable change in accuracy when size of the dataset increased.

<span id="page-10-9"></span><span id="page-10-1"></span><span id="page-10-0"></span>An overview of the methodology, where data is less likely (low-density) and hence more likely to be corrupted, the ECOD employs information about the distribution of the data. For each variable in the data, ECOD individually estimates an Empirical Cumulative Distribution Function (ECDF) [\[112\],](#page-25-8) [\[113\].](#page-25-9) ECOD uses a univariate ECDF to determine tail probabilities for each variable and then combines them together to produce a score for an observation. The computation takes into account both the left and right tails of each dimension and is performed in log space. Although this method is designed to find outliers, we'll use it to find instances of faulty data in a dataset  $[114]$ . FIGURE  $4(j)$  Shows the resulting corrupt data detected using the model. The outlier score for the ECOD algorithm is calculated using the below-mentioned formulae. The Outlier scores are calculated for the left tail, right tail and another measure called auto as shown in Eq.  $(12)$ , Eq.  $(13)$ , Eq. [\(14\)](#page-10-5).

<span id="page-10-10"></span><span id="page-10-3"></span><span id="page-10-2"></span>
$$
O_{\text{left-only}}(Y_k) := -\log \widehat{D_{\text{left}}(y_k)} = -\sum_{i=1}^a \log(\widehat{D_{\text{left}}}^{(i)}(Y_k^{(i)}))
$$
\n(12)

<span id="page-10-4"></span>
$$
O_{right-only}(Y_k) := -\log \widehat{D_{right}(y_k)} = -\sum_{i=1}^a \log(\widehat{D_{right}}^{(i)}(Y_k^{(i)}))
$$
\n(13)

<span id="page-10-5"></span>
$$
O_{auto}(Y_k) = -\sum_{i=1}^{a} [\gamma_i < 0 \log(\hat{D_{left}}^{(i)}(Y_k^{(i)})) + \gamma_i < 0 \log(\hat{D_{right}}^{(i)}(Y_k^{(i)}))]
$$
\n(14)

where O is the outlier scores, Y is the input data, D is the corresponding ECDF. The final outlier score is derived by aggregating the above-mentioned outlier scores using the formula mentioned in Eq. [\(15\)](#page-10-6).

<span id="page-10-6"></span>
$$
O_i = \max (O_{left-only}(Y_i), O_{right-only}(Y_i), O_{auto}(Y_i))
$$
\n(15)

# 12) GAUSSIAN MIXTURE MODELS

GMMs or Gaussian mixture models use sets of parameterised probabilistic functions as the weighted components of

<span id="page-11-2"></span>the pre-trained model using expectation maximisation technique [\[115\].](#page-25-11) Previous work on outlier detection has shown that gaussian mixture models have proved effective in detecting outliers providing optimised performance at  $k=2$  gaussians and other parameters being randomly initialised [\[116\].](#page-25-12) In the present work and on experimentation, the optimized ECOD led to a performance of 82.71% on the clustering dataset and 82.83% on linear data with a corruption rate of 20%, decreasing with increase in corruption percentage and indistinguishable change in accuracy when size of the dataset increased.

GMMs when used on the aforementioned datasets, it has a very high recall but a very low accuracy. In terms of outlier detection it performs better than other similar clustering techniques like K-Means clustering and DBSCAN clustering. It necessitates the specification of the contamination rate, just like other probabilistic models. This unsupervised clustering method is the Gaussian Mixture Model and can be described using Eq.  $(16)$ . As a sum of component densities for a particular point. In contrast to K-Means, we fit 'k' Gaussians in the data in this technique. The parameters such as the mean and the variance for each of the cluster as well as the weight of the cluster also called the distribution parameters are then determined [\[116\].](#page-25-12) We then determine the odds that each data point will belong to each of the clusters. FIGURE  $4(k)$ Shows the resulting corrupt data detected using the model. The unsupervised method is applied on univariate data and produces an outlier score which then becomes the threshold and the primary criteria to filter the outliers and anomalies from the data [\[117\].](#page-25-13) The outlier score for a particular data instance is calculated by the Eq.  $(17)$ , where  $p(y)$  is the PDF or the probability density function and f would be any constant to scale the outlier score and u is the mean  $[118]$ . Further the outlier score is normalised to an interval of 0 to 10 in order to ease the comparison.

<span id="page-11-4"></span>
$$
p(y|\lambda) = \sum_{k=1}^{N} v_k g(y|\mu_k, \sum_k)
$$
 (16)

$$
OS_{y} = (\log(p(y)))^{2f} \tag{17}
$$

GMMs can also be used to identify potential anomalies in multidimensional datasets. It can also be aggregated with an LSTM (long short term memory) to examine the correlation between the multivariate parameterised data in order to obtain improved outcome in detecting potential outliers [\[119\].](#page-25-15)

#### 13) MEDIAN ABSOLUTE DEVIATIONS

The MAD or ''median absolute deviation'' for a set of attributes is the median of that dataset's absolute deviation. This concept is the crux of the Median Absolute Deviation also called MAD algorithm [\[120\].](#page-25-16) The absolute deviation of an instant is the pairwise displacement between such a tuple and the distribution's mean. In previous works the MAD is a reliable indicator of the variability in a sample of numeric data, is used in statistics. Because it is so successful and efficient, the Median Absolute Deviation model is frequently <span id="page-11-9"></span><span id="page-11-8"></span><span id="page-11-3"></span>employed for this kind of anomaly identification [\[121\].](#page-25-17) Instead of pure outliers and anomalies, we will concentrate on corrupt data and provide optimised results [\[121\].](#page-25-17) The primary reason this algorithm does well on the aforementioned datasets is that MAD is primarily used for evaluating the distance between data instance and its median in the terms of the median distance and is strictly for univariate data  $[122]$ . The time required to compute the MAD score is fairly less and the MAD algorithm is aimed towards symmetric distributions [\[123\].](#page-25-19) Unlike the other probabilistic models, the Median Absolute Deviation does not require the corruption rate to be specified which adds to its credibility and provides optimised results [\[123\].](#page-25-19) FIGURE [4\(l\)](#page-6-0) Shows the resulting corrupt data detected using the model.

<span id="page-11-10"></span>The MAD is an alternative to the earlier used threshold equal to the sum of the mean of a distribution and three standard deviations which causes problems as the mean value and the standard deviations are extremely sensitive to outliers. This model is another threshold based outlier detection technique to identify outliers based on the statistical formulae like mean, median, mode. Unfortunately though this algorithm like many other statistical algorithms adds a bias to multiple statistical measures used in outlier detection algorithms which lead to inaccurate results [\[124\].](#page-25-20)

<span id="page-11-11"></span>In the present work and on experimentation, the optimised MAD successfully accomplished an effectiveness of 94.46% on the clustering dataset and 94.77% on linear data with a corruption rate of 20%, decreasing with increasing corruption percentage and indistinguishable change in accuracy as dataset size increased.

#### 14) COPULA-BASED OUTLIER DETECTION

<span id="page-11-5"></span><span id="page-11-1"></span><span id="page-11-0"></span>The Python PyOD module contains a set of probabilistic algorithms one of them named COPOD [\[57\], o](#page-23-43)ne of which is the Copula-Based Outlier Detector. COPOD is an empirical copula model-based, parameter-free, and highly interpretable outlier detection algorithm. It is important to note that achieving top optimised performance on anomaly detection datasets, interpretable and straightforward corruption visualisation, speed and computational efficiency and scaling to high-dimensional datasets are some of its key distinguishing characteristics [\[125\].](#page-25-21) The corruption rate is the only known parameter we use in this investigation. FIGURE  $4(m)$  Shows the resulting corrupt data detected using the model. In previous work the authors have highlighted that the optimised COPOD is highly correlated with the ECOD algorithm [\[57\]](#page-23-43) and that it outperforms all its variants by being deterministic without any hyper parameters and highly effective for high dimensional datasets.

<span id="page-11-14"></span><span id="page-11-13"></span><span id="page-11-12"></span><span id="page-11-7"></span><span id="page-11-6"></span>In statistics and probability, copula is a CDF and a multivariate function where the marginal probability distributions of the variables is uniform in the range [0,1]. Copulas are also used for representing or modeling the dependence of random variables [\[126\].](#page-25-22) This is the main motivation behind using copulas to detect anomalies in various application [\[127\].](#page-25-23)

The COPOD algorithm has three main steps to detect outliers [\[57\]:](#page-23-43)

- Calculate the cumulative distributive function based on the dataset.
- Calculate the empirical copula.
- Find the tail-probabilities [\[128\]](#page-25-24) using the above mentioned empirical copula.
- The outlier score is found using the max of the tail probabilities calculated for each data instance.

COPOD (Copula-Based Outlier Detector) does not require pairwise distance measurement, in contrast to other proximity-based algorithms. It mainly applies to multivariate data. To determine and identify the anomalies contained in the dataset, the COPOD generates an empirical copula before calculating the tail-based probability for each data occurrence [\[129\].](#page-25-25)

<span id="page-12-5"></span>In the present work and on experimentation, the optimised COPOD achieved a clustering dataset effectiveness of 92.43% with a corruption rate of 20%, decreasing to 88% with increasing corruption percentage and indistinguishable change in accuracy as dataset size increased. The proposed linear data algorithm had a 92.67% accuracy for a dataset with 20% corrupted data, with comparable trends when the corruption percentage and dataset size were varied.

#### 15) HISTOGRAM-BASED OUTLIER DETECTION

A potent method is called unsupervised histogram-based outlier identification also called HBOS. It establishes the level of corruption while assuming feature independence by producing histograms. The focus of the authors' work will be on the application of histogram-based outlier detection (HBOS), a statistical model that is primarily for outliers, to identify corrupted data in datasets that have been tainted. The histogram algorithm assesses the level of anomalies while assuming feature independence by producing histograms [\[14\]. A](#page-23-1)fter multivariate anomaly detection, a histogram for each feature can be generated, graded separately, and aggregated [\[130\].](#page-25-26) It is mostly relevant to multivariate data, although outperforming many other probabilistic models when applied with the aforementioned bespoke dataset. Similar to other probabilistic and statistical models, the corruption rate must be given for this histogram based algorithm for outlier detection. FIGURE  $4(n)$  Shows the resulting corrupt data detected using the model.

The histogram algorithm for numerical data is essentially based on two approaches: the first uses the renowned histogram bins with static bin-width that do not vary, and the second uses the bin-width that changes approach (dynamic bin-width). These bins with a wider interval of values or range have lesser density and less height. As a result, the density of each bin is represented by its height, which is then normalised to guarantee that the anomaly is given the same weight and score. The following step involves applying the Eq.  $(18)$  to

calculate the HBOS value [\[131\].](#page-25-27)

<span id="page-12-9"></span><span id="page-12-8"></span><span id="page-12-7"></span><span id="page-12-1"></span>
$$
HBOS(q) = \sum_{j=0}^{a} \log \frac{1}{hist_j(q)}
$$
(18)

<span id="page-12-4"></span>where HBOS for instance q with dimension a is calculated by use of height of the bins where q is located. HBOS works well on tasks involving global anomaly identification, but it is unable to identify local outliers since it is unable to model or depict histograms with local anomaly density. The algorithm works well on univariate data [\[132\].](#page-25-28) A similar anomaly detection approach can be used there, even though histograms for multidimensional data are computationally intensive and need a large number of operations [\[133\],](#page-25-29) [\[134\].](#page-25-30)

In the present work and on experimentation, the optimised HBOS achieved a clustering dataset effectiveness of 95.05% with a corruption rate of 20%, decreasing to 88% with increasing corruption percentage and indistinguishable change in accuracy as dataset size increased. For a dataset with 20% corrupted data, the proposed linear data algorithm had an accuracy of 95%, with comparable trends when the corruption percentage and dataset size were varied.

#### <span id="page-12-0"></span>**IV. PROPOSED METHODOLOGY**

PAACDA (Proximity based Adamic Adar Corruption Detection Algorithm): Adamic Adar [\[135\],](#page-25-31) [\[136\]](#page-25-32) is a graph algorithm used to link nodes in a social network. In this study, we utilise the concept behind this algorithm to detect outliers and missing and modified values while leveraging its prominence in data correlation in graph networks by applying PAACDA to a numerical, tabular dataset. This algorithm is used to compute the accuracy of a particular data instance within a dataset as a whole. The Adamic Adar Index [\[65\] is](#page-24-3) calculated using Eq. [\(19\)](#page-12-2).

<span id="page-12-10"></span><span id="page-12-2"></span>
$$
A(x, y) = \sum_{n \in D(x) \cap D(y)} \frac{1}{\log |Deg(n)|} \tag{19}
$$

<span id="page-12-6"></span>The formula in Eq. [\(19\)](#page-12-2) presented determines the Adamic Adar index for each node in a network where  $D(x)$  represents the neighbors of  $x$  and  $D(y)$  represents the neighbors of  $y$  and Deg(n) is the degree of the common neighbours. Typically, the Adamic Adar Algorithm is utilized to evaluate the closeness of two nodes in a graph. It is based on the notion that values with greater discrepancies between them and values with less in are less likely to be regarded as important than common. The parameter of a value's network closeness is oppositely related [\[71\] to](#page-24-9) the Adamic-Adar index. Since we are dealing with numerical data, we use the data's mean as a metric to verify the link with each data point and spot the altered or distorted values. The proposed Eq. [\(20\)](#page-12-3) is used in the PAACDA Algorithms for data corruption detection.

$$
PAACDA Index = \sum_{x=1}^{N} \frac{1}{\log |(Number of values in x*range)|}
$$
\n(20)

<span id="page-12-3"></span>The steps listed below illustrate the method followed:

• The mean is calculated for the column being analysed.

- The range is set as mean/4.
- Each data instance is iterated and Eq. [\(20\)](#page-12-3) is applied, where x is each data instance.
- If the instance is missing then the PAACDA Index value is set to infinity.
- The PAACDA Index is compared amongst each other and the set of corrupted values is determined.
- The accuracy metric is obtained and confusion matrix is determined.

The reason why defining the range as mean/4 explains intuitively is that the mean accounts for all the components of the provided data and contains information from each observation in a dataset. The mean serves as a link between the actual values and the corrupted data in this manner. Using probe and analysis, we come to the conclusion that mean/4 is the appropriate range for the following method. Again, the algorithm's iteration count is determined experimentally and we utilise 3 iterations for this algorithm and dataset as shown in Algorithm [1.](#page-13-1) The proposed algorithm loops through twice. The outer loop iterates through each datapoint and the inner loop further iterates and compares each cell data with the one held by outer loop. The time complexity is quadratic. Thus this algorithm runs in  $\Theta(n^*n)$  time, where n is number of data entries in a column.

The PAACDA algorithm is based on the notion that values with fewer similarities [\[71\] a](#page-24-9)re more likely to be viewed as significant than values with greater differences. The performance of this algorithm might vary from dataset to dataset depending on the data distribution as well as the percentage and level of corruption it is subjected to. The PAACDA algorithm uses mean to compute the index which acts as an advantage because each time the data is corrupted the mean varies accordingly. The PAACDA has proven to be more effective than the other clustering and statistical techniques at locating outliers, missing values and corrupted data where accuracy is the primary concern. This makes PAACDA the most suitable for data corruption detection for numerical datasets.

# <span id="page-13-0"></span>**V. RESULTS AND DISCUSSION**

On the various sizes and corruption variations of the synthetically created dataset, several experiments were attempted and put to use. The study primarily focuses on 2 types of datasets: Clustered and Linear

Each of the aforementioned datasets was subsequently examined in various sizes, including,

- Small Dataset 10000 values
- Medium Dataset 40000 values
- Medium-Large Dataset 75000 values

Again, different corruption levels were explored each category of various dataset sizes:

- 20%
- $40%$
- $60\%$

<span id="page-13-1"></span>**Algorithm 1** Proximity Based Adamic Adar Corruption Detection Algorithm(PAACDA)

```
indices \leftarrow []
for each i ∈Corrupted Column do
    first \leftarrow 1second \leftarrow 1third \leftarrow 1
    for each j ∈Corrupted Column do
         if abs(j - i) \leq range then
             first \leftarrow first + 1end if
         if abs(j - i) \leq 2 * range then
              second \leftarrow second + 1end if
         if abs(i - i) \leq 3 * range then
              third \leftarrow third + 1end if
    end for
    index \leftarrow 0
    if first \neq 1 then
         index \leftarrow \frac{1}{log(first)}end if
    if second \neq 1 then
         index \leftarrow index + \frac{1}{log(second)}end if
    if third \neq 1 then
         index \leftarrow index + \frac{1}{log(third)}end if
    indices.append(index)
end for
```
After extensive experiments, the following conclusions were drawn. Table [3](#page-14-0) shows the accuracy values of the top performing models. The rest of the results can be found in the appendix.

# A. RESULTS FOR CLUSTERED DATA

PAACDA, HBOS, MAD perform best in this situation, with accuracy values of 99.74%, 95.05%, and 94.46%, respectively. The middling performers include COPOD, GMM, LUNAR, Elliptic Envelop, K-Means clustering, ECOD and Isolation Forest with accuracy values of 92.43%, 91.95%, 87.01%, 72.17%,86.06%, 82.71% and 82.37% respectively. The One-Class SVM, DeepSVDD, PCA, ROD, LOF and DBSCAN with accuracies of 76.82%, 72.25%, 72.53%, 62.71%, 59.47% and 39.60% respectively generally performed the worst, while the results varied depending on the degree of corruption and the size of the sample.

There were several noticeable variations as the corruption rate went from 20 to 60, including some models that did well in smaller sizes but did poorly as the size expanded. But PAACDA consistently demonstrated its superiority over the competition with unwavering accuracy.

# <span id="page-14-0"></span>**TABLE 3.** Accuracy values of the top performing algorithms.



<span id="page-14-1"></span>

(d) Sensitivity

(e) F1-Score

**FIGURE 7.** Depicts results for the clustering data for small dataset and corruption rates 20%, 40% and 60%.

<span id="page-14-2"></span>

**FIGURE 8.** Depicts results for the clustering data for medium dataset and corruption rates 20%, 40% and 60%.

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<span id="page-15-0"></span>

<span id="page-15-1"></span>**FIGURE 9.** Depicts results for the clustering data for medium-large dataset and for corruption rates 20%, 40% and 60%.





<span id="page-15-2"></span>

**FIGURE 11.** Depicts results for the linear data for medium dataset and corruption rates 20%, 40% and 60%.

<span id="page-16-0"></span>

<span id="page-16-1"></span>**FIGURE 12.** Depicts results for the linear data for medium-large dataset and for corruption rates 20%, 40% and 60%.

**TABLE 4.** Results of realistic dataset.



Furthermore, the observed pattern shows unequivocally that the PAACDA model's performance declined as the extent of corruption rose as shown in FIGURE [7,](#page-14-1) [8,](#page-14-2) [9.](#page-15-0) Although, in general, the hierarchy of the model's performance was not greatly impacted by the amount of corruption since the same models performed best and worse, the accuracy statistics substantially reduced as the level of corruption rose.

# B. RESULTS FOR LINEAR DATA

The same findings as in the previous instance were reached. PAACDA fared better in this instance as well with an accuracy of 99.94%. Most of the higher-performing models from the past including HBOS, MAD, COPOD and GMM did better in this instance with accuracies 95.00%, 94.77%, 92,27% and 92.15% respectively. K-Means clustering, LUNAR, Isolation forest, ECOD and DeepSVDD fared with accuracies of 86.70%, 86.87%, 82.22%, 82.83% and 76.25% respectively. Results were better for models that were more geared toward linear data. Once again, the PCA, One Class SVM, ROD, LOF and DBSCAN Clustering were the worst performers with accuracies of 73.01%, 72.28%, 62.83%, 58.79% and 43.20% respectively. As the dataset size changed, there were no appreciable changes in accuracy.

# <span id="page-17-0"></span>**TABLE 5.** Accuracy values for clustering data.



#### <span id="page-17-1"></span>**TABLE 6.** Accuracy values for linear data.



However, just like in the previous instance, performance suffered as the amount of corruption rose.

Slightly different trends were observed in the case of the other metrics like Precision, Recall, Sensitivity, and F1 score in the case of both Clustered and Linear Datasets. Several models that had previously had moderate and semi-moderate accuracy now had either high precision, recall, or F1 score, despite the ordering hierarchy being relatively constant as these models were geared towards linear data when compared to clustering data as shown in FIGURE [10,](#page-15-1) [11,](#page-15-2) [12.](#page-16-0)

# <span id="page-18-0"></span>**TABLE 7.** Recall values for clustering data.



# <span id="page-18-1"></span>**TABLE 8.** Recall values for linear data.



# C. RESULTS FOR REALISTIC DATA

The same set of experiments with 16 different models were carried out on Realistic existing dataset with outliers. PAACDA performed the best with 99.75% accuracy. Unlike the synthetic data, the close competitors for our proposed model was not HBOS and MAD, but instead COPOD and

Elliptical Envelope with accuracy of 99.12% and 98.50% respectively. Every model performed decently well except K means which has accuracy of 7.74% as it is not suitable for all kinds of dataset. Further, for each of the above models other metrics such as precision, recall, sensitivity and F1 score are tabulated in the Table [4.](#page-16-1)

# <span id="page-19-0"></span>**TABLE 9.** Precision values for clustering data.



# <span id="page-19-1"></span>**TABLE 10.** Precision values for linear data.



# D. LIMITATIONS AND CONSTRAINTS

The proposed methodology however has some limitations. The PAACDA requires the specification of the corruption percentage as one of the parameters which further

will require parameter tuning. In addition to this PAACDA works well with uni-variate data unlike ROD, GMM and HBOD which can handle multi-variate data at the a time.

# **TABLE 11.** Sensitivity values for clustering data.



#### **TABLE 12.** Sensitivity values for linear data.



# <span id="page-20-0"></span>**VI. CONCLUSION AND FUTURE SCOPE**

Data that is reliable and accurate is essential for conducting effective research. This is because faulty and untrustworthy data produces erroneous or false results. Inadvertently entering incorrect data into a computer will produce an output,

which could be fatal in fields such as healthcare and defence. While being written, edited, or transferred to another drive, data might become corrupted. Additionally, a virus can damage files. Usually, this is done on purpose to harm crucial system files. Finding outliers that are silently existing in a



#### **TABLE 13.** F1-Score values for clustering data.

dataset is only half the issue; data with high rates of corruption can seriously impair model accuracy and the outcomes of data analytics. In this case, accuracy is a necessary requirement to verify the information from the sources. Research accuracy ensures that the information gathered is accurate or inaccurate. Therefore, it is crucial to check the accuracy of any survey.

In this article, firstly we introduce the primary concepts of outlier detection and how these models and techniques can be used to detect corrupted data. Then, we encapsulate the quality improvement approaches of data corruption detection and split the data to two categories based on their behavior: linearly distributed data and clustered data on 3 high structured synthetic datasets- small, medium, medium-large. The results showed That the PAACDA outperformed the other algorithms with an accuracy of 96.35% for clustered data and 99.04% for linear data. Lastly, we lay-out an experiment-based comparison of multiple cutting edge quality improvement approaches using a plethora of quality evaluation metrics, the authors have combined the findings of various other probabilistic and statistical models and explained how they used the innovative PAACDA algorithm to get desired results on the data. With accuracy values of 95.05% and 94.46%, respectively, HBOS and MAD are among the other top performers for the clustering dataset. COPOD, GMM, LUNAR, Elliptic Envelop, K-Means clustering, ECOD, and Isolation Forest are among the middle performers, with accuracy values of 92.43%, 91.95%, 87.01%, 72.17%, 86.06%, 82.71, and 82.37%, respectively. The One-Class SVM, DeepSVDD, PCA, ROD, LOF, and DBSCAN performed the worst, with accuracies of 76.82%, 72.25%, 72.53%, 62.71%, 59.47%, and 39.60%, respectively. Most previous higher-performing models, including HBOS, MAD, COPOD, and GMM, performed better on the linear dataset, with accuracies of 95.00%, 94.77%, 92.27%, and 92.15%, respectively. Accuracy rates for K-Means clustering, LUNAR, Isolation forest, ECOD, and DeepSVDD were 86.70%, 86.87%, 82.22%, 82.83%, and 76.25%, respectively. Models that were more geared toward linear data produced better results. PCA, One Class SVM, ROD, LOF, and DBSCAN Clustering performed the worst, with accuracies of 73.01%, 72.28%, 62.83%, 58.79%, and 43.20%, respectively. There were no discernible changes in accuracy as the dataset size increased. However, as in the previous case, performance suffered as the level of corruption increased.

To the authors knowledge, the paper is the first one that systematically addressed the detection of corrupted data from different aspects such as data distribution, dataset size and also variations of corruption rates. We reviewed most of the published papers in well reputed libraries. With an accuracy of 96.35% for clustered data and 99.04% for linear data, the PAACDA algorithm exceeds the other models. In this work an exhaustive review of many unsupervised and probabilistic models was conducted. The other top performing algorithms are the Histogram based outlier detection model, K-Means Clustering, Elliptical Envelope outlier detection and Isolation forest.

This study correctly identified the PAACDA algorithm as one of the better methods and provided a comprehensive compilation of numerous alternative approaches for solving

#### **TABLE 14.** F1-Score values for linear data.



the problem of correctly differentiating corrupted data in the dataset. The future work in this field must focus on the following aspects: 1. To find tainted values that stray just a little from the original values, more algorithmic research could be explored. 2. The current effort leans towards outliers and focuses mostly on the detection of tainted data. 3. It is possible to conduct additional studies on the topic of recovering the original data using tools like backpropagation and GANs (Generative Adversarial Networks). When the output feature is known, backpropagation can be used to create the input features. 4. The missing values can be filled in using GANs. Furthermore, traditional restoration models are comparitively complex, which limits our propensity to expand pragmatic studies and applications. The potential of these strategies is genuinely tremendous, and listing them only scratches the surface. This study can be expanded further to include categorical and even picture datasets in addition to numerical data. 5. In the realm of picture collections, GANs have a wide range of uses, particularly for identifying false images and producing Deep fakes.

# **APPENDIX**

The entire tables under the results and discussion section have been included in the Appendix [A](#page-22-12) below.

# <span id="page-22-12"></span>APPENDIX A TABLES

Additional tables that support the experiment can be found here. All the experimental results including the results for small, medium and large datasets for all corruption rates (20%, 40%, 60%) are included in this document. Table [1](#page-3-0)[,2](#page-5-5)[,3](#page-14-0)[,4](#page-16-1)[,5](#page-17-0)[,6,](#page-17-1)[7,](#page-18-0)[8,](#page-18-1)[9,](#page-19-0)[10](#page-19-1) represent the accuracy, recall,

precision, sensitivity and F1-score of both linear and clustering data.

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