

## RESEARCH ARTICLE

# Mobile Sensor Nodes Traversal Schemes to Attend Events at Random Locations With Minimal Energy Depletion

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**ABSTRACT** A group of homogeneous mobile sensor nodes (MSNs) with fixed amount of energy are deployed randomly over the region of interest (ROI). Events might happen at a random location within the ROI. MSNs must travel a certain distance to reach the random location for information collection. The modified Min-Heap approach helps to identify a suitable MSN from the group of MSNs. The selected MSN will reach the random location by traveling a shorter distance than its counterparts. The proposed mathematical models are helpful in uniformly distributing the workload among the MSNs, to ensure that all the MSNs have an approximately equal amount of residual energy.

**INDEX TERMS** Mobility, random deployment, energy-efficient, traversal schemes, network lifetime.

## I. INTRODUCTION

Rapid development in microelectronics, wireless communications, and sensor technology cause the design and development of micro-structured sensor devices, that can sense the environmental information and transmit the sensed data to the base stations for further processing [1].

Sensor nodes with locomotive capabilities give wireless networks extra abilities, making them more robust for habitat and environmental monitoring, traffic observation, battlefield surveillance, smart homes, and smart cities [2]. Although millibots appear small, they collectively contain integrated capabilities, including sensing, computation, communication, localization, and mobility [3].

Placement of sensor nodes at the predetermined locations is not feasible in a disastrous and hazardous environment. MSNs are the most suitable for the information collection from such an environment where human intervention is not possible. In many cases, space, terrain, and narrow entrance hinder the movement of big-sized robots. Sensor nodes with locomotive capabilities enable them to move throughout the sensing region.

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Coverage can be maximized in controlled mobility by more precise deployment patterns. Specific phenomena or locations in the sensing region can be easily targeted and followed [4], [5].

Robomote, a robotic solution developed to explore problems in large-scale distributed robotics and sensor networks, appeared in [6]. The low-cost mobile sensor devices make it possible to have the applications of mobile sensor nodes in a wide range of domains [7].

The relocation capabilities of mobile sensor nodes in sensor networks enhance the application's output. A few applications of mobile sensor nodes are to heal the coverage holes, perform network resource optimization, or provide fault tolerance support [8]. In some cases, the mobile sensor nodes will get scattered and are expected to do the information collection in fields of kilometers in size [9].

In some applications, a reasonable number of moving nodes are included along with static nodes. Through the moving nodes, an improvement in the coverage of the monitoring area is observed [10]. Mobile entities can have a predefined set of stop locations for data collection [11]. Intrusion detection in wireless sensor networks with efficient power usage is discussed in [12] and [13].

The organization of this paper is as follows. Section II details with related work. The description of the problem is in Section III. Section IV is devoted to objectives. Section V narrates the solution to the problem. Section VI carries the Results and Discussions. Section VII concludes the paper.

**II. RELATED WORK**

The role of MSNs appeared in a diverse range of applications. Specifications, architecture, working model and implementation of MSNs are specific to the application. Consider a scenario in which MSNs are designed to work with underwater applications such design may not fit for applications on the battlefield. Similarly, MSNs intended for military applications may not be suitable for industrial applications.

As an example of applications, MSNs are utilized for sweep coverage [14] and air quality monitoring in [15]. In [16], the area coverage with mobile sensor nodes in 3D wireless sensor networks is described.

The specifications, architecture, working model, and implementation are specific to the application. Hence designing a typical prototype that will fit for all the applications is very complex.

A minimal amount of research is available on the coverage-based pattern movement of MSNs. ROI is covered using three MSNs in a triangulation method. The initial equilateral triangle is formed randomly on the ROI, and the remaining area is covered in a snake-like fashion [17].

To achieve the complete coverage of the ROI, MSNs are deployed at the predetermined locations on the ROI and moved in a predetermined traversal path from source to destination in shifted migration method [18]. MSNs are moved in a distributed manner to achieve one coverage without coverage holes. This approach shows that the MSNs deplete minimum energy during the traversal [19].

In the above-listed approaches, the MSNs are used to cover the entire sensing region without coverage holes. The MSNs are either randomly deployed or deployed at a predetermined position in the sensing region. Predetermined traversal schemes help to move the MSNs and achieve coverage.

None of the work focuses on the random deployment of MSNs and collection of information from random locations within the sensing region.

**III. PROBLEM DESCRIPTION**

Due to the random deployment and the influence of environmental factors, the MSNs may land at any location on the ROI. Random Sensing Point (RSP) is the location from where the information needs to be sensed by a MSN. Upon successful landing, the MSN has to travel a certain distance to reach the RSP. That makes it to deplete the battery. There exists a need to identify a suitable MSN to attend the RSP, and all the MSNs should get opportunities to have an approximately equal amount of residual energy.

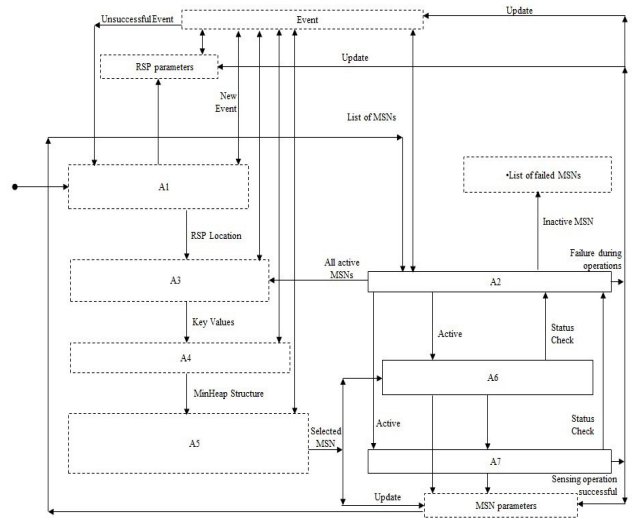


FIGURE 1. Block Diagram / Model Diagram.

**IV. OBJECTIVES**

1. Identify a single MSN from the group of MSNs that can reach the RSP with a shorter traveling distance than its counterparts.
2. Ensure that all the MSNs have approximately equal amount of residual energy to prolong the network lifetime.

**V. PROPOSED SOLUTION METHODOLOGY**

Figure 1 shows the working model of the proposed solution. The Block diagram consists of 2 types of rectangular boxes. The rectangular boxes with solid lines indicate either the operations of mechanical, electrical, communication, or sensing units of the MSNs. The rectangular boxes with dotted lines narrate the activities of the MSNs. Arrows indicate the flow of data and control. The event module is the controller module which keeps coordination with all other modules.

An event  $E_x$  is the sequence of activities needed to collect the information from an  $RSP_x$ . Resources of  $E_x$  will get released only on successful completion of  $E_x$  or if any activities fail during the operation. Only on the successful completion of  $E_x$ , another event  $E_{(x+1)}$  will get initiated.

**Algorithm 1** Sequence of Activities for a Random Event

- 1: Generation & Selection of RSP (A1)
- 2: Identification of active MSNs (A2)
- 3: Calculation of distance between the RSP and all active MSNs (A3)
- 4: Creation of modified-Min-Heap (A4)
- 5: Suitable MSN identification (A5)
- 6: Mobility of the identified MSN to the location of RSP (A6)
- 7: Sensing operations at the RSP (A7)

**TABLE 1.** Description of symbols associated with RSP.

Symbol	Description
$R_{ID}$	Unique identification number given to every RSP
$R_L$	Location of the RSP (Hexagon Number)
$R_R$	Row value of the selected RSP
$R_C$	Column value of the selected RSP
$R_S$	Status of the RSP ( Sensed / Not Sensed )
$R_{Sel}$	RSP is selected for operation or not
$R_{Count}$	Total number of RSPs
$D_R$	Array to store values for parameters of all RSPs

As shown in Algorithm 1, it has a set of activities which are named A1, A2 upto A7. All the activities are serially ordered. Output of an activity is forwarded as input to the next activity. The definitions for the parameters associated with RSP are in Table 1. The RSP location, which is the row number  $R_R$  and  $R_C$  is the position on that row are calculated from the value of  $R_L$ .  $R_L$  is the sensing point/hexagon number which will vary from 1 to  $R_{Max} \times C_{Max}$ , where  $R_{Max}$  is the maximum value for  $R_R$  and  $C_{Max}$  is the maximum value for  $R_C$ .

A linear data structure  $D_R$  is defined to store the values of all the parameters of a RSP as specified in Table 1. Array  $D_R$  keeps the information of all the RSPs in the ascending order of  $R_{ID}$ , where  $R_{ID}$  is a unique identification number assigned to every RSP on its generation.  $R_{Count}$  is the total number of RSPs.

Whenever an RSP gets generated, the values of  $R_L$ ,  $R_R$ ,  $R_C$  along with  $R_{ID}$  are automatically stored in  $D_R$ . The values for  $R_S$  &  $R_{Sel}$  are assigned as 0 and linked with  $R_{ID}$ . This sorted array  $D_R$  is passed as input to the Algorithm 2.

As shown in Algorithm 2, the RSP with  $R_S$  as 0 &  $R_{Sel}$  as 0 will be selected. Where  $R_{Sel}$  is binary variable used to indicate the present status of the RSP (Selected for operation / Not) and  $R_S$  is a binary variable used to identify the status of the RSP (Sensed / Not sensed).

#### Algorithm 2 Selection of RSP

```

1: I = 1
2: while I ≤ RCount do
3:   if RS = 0 && RSel = 0 then
4:     Update (RID, RSel)
5:     Calculate: (RR, RC)
6:   end if
7:   I = I + 1
8: end while

```

The value of  $R_{Sel}$  for the selected RSP will get updated as 1. This indicates that the RSP is selected for operation. However the value of  $R_S$  will be 1 only on successful completion of all the activities listed in Algorithm 1 for the selected RSP. The values of  $R_R$  and  $R_C$  get updated and passed to Algorithm 4 along with respective  $R_{ID}$  for further operations.

**TABLE 2.** Description for symbols associated with MSNs.

Symbol	Description
$M_{ID}$	Unique identification number given to every MSN
$M_S$	Status of the MSN (1 or 0)
$M_N$	Number of active MSNs
$M_L$	Current location of the MSN (Hexagon Number)
$M_R$	Row value of the MSN
$M_C$	Column value of the MSN
$M_E$	Distance between the selected RSP and MSN
$M_A$	Distance already traveled by the MSN
$M_T$	Total distance traveled by the MSN
$M_P$	Number of RSPs already attended
$D_M$	Array to store values for parameters of all MSNs
$M_{Count}$	Number of MSNs

Mobile Sensor Node architecture is almost similar to the standard sensor node. The four main components of an MSN are the mobilizer, sensing, communication, processing, and power supply. They may contain a few additional units, such as position finders and power generators. The location or position finder unit helps to identify the sensor node's position. The Power generating unit supports a partial power supply, but it is an optional unit.

#### Algorithm 3 MSN Status Check

```

1: I = 1
2: while I ≤ MCount do
3:   if (MU = 1) & (SU = 1) & (CU = 1) & (OU = 1)
4:     then
5:       Set: MS = 1
6:     else
7:       Set: MS = 0
8:     end if
9:   I ← I+1
10: end while

```

[MU = Mobilizer Unit, SU = Sensing Unit, CU = Communication Unit & OU = Other Units]

A linear data structure  $D_M$  is defined to store the values of all the parameters of a MSN as specified in Table 2. Array  $D_M$  keeps the information of all the MSNs in the ascending order of  $M_{ID}$ , where  $M_{ID}$  is a unique identification number assigned to every MSN prior to deployment.

Upon the successful landing, the values  $M_L$ ,  $M_R$ ,  $M_C$  along with  $R_{ID}$  are computed and automatically stored in  $D_M$ . The values for  $M_E$  &  $M_A$  are assigned as 0.

The failure in one or multiple components of MSNs cannot be ruled out. An MSN may fail at any location during the traversal or the sensing operations. Hence at all stages, it is essential to detect the status of the MSN. An MSN

with one or more failed components is not fit for further operations, and such MSN is updated as failed in the MSN list.  $M_S$  is a binary variable used to indicate the status of the MSN.

Algorithm 3 helps to identify the status of the available MSNs. Value of  $M_S$  is set as 1 for all the MSNs that are fit for the traversal & operations and the value of  $M_S$  is set as 0 for all the MSNs that are not fit for the traversal & operations.

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#### Algorithm 4 Distance Calculation

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1: J = 1
2: while J ≤ MN do
3:   ME = (|MR - RR|) + (|MC - RC|)
4:   MT = ME + MA
5:   Min Heap (M[ID,P,T])
6:   J ← J+1
7: end while

```

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Necessary parameters of the active MSNs and selected RSP are passed to Algorithm 4 to calculate the distance between the selected RSP with all the active MSNs. The variable  $M_A$  stores the distance already traveled by the MSN in the earlier rounds. The value  $M_E$  is the distance between the RSP in consideration and the MSN, is calculated using Equation (1). This calculation is repeated for the  $M_N$  number of times, where  $M_N$  is the total number of active MSNs.

$$M_E = (|M_R - R_R|) + (|M_C - R_C|) \quad (1)$$

In some cases, the value  $M_E$  may be the smallest value. But the corresponding MSNs' past travel, i.e.,  $M_A$ , may be more than their counterparts. In other cases, the value of  $M_A$  may be small compared to peers, but the value  $M_E$  may be more. Hence for the proper selection of MSN, both the previous travel  $M_A$  and the present distance  $M_E$  are considered.

$M_T$  is the sum of the distances already traveled in the earlier rounds and the distance between the selected RSP and the MSN. It can be written as  $M_T = M_E + M_A$ . The value of  $M_A$  will be 0 if the MSN has not traveled any distance from its initial landing.

Algorithm 4 generates a total of  $M_N$  number of tuples for an RSP. Each tuple  $M_{[ID,P,T]}$  will have three parameters  $M_{ID}$ ,  $M_P$  and  $M_T$ . All the three or some of these parameters are helpful for calculation and updation purposes.

All the generated tuples are passed to Algorithm 5 to identify a most suitable MSN to reach the RSP in consideration. Once the MSN selection process is completed, the  $M_E$  value for non-selected MSNs is updated to zero. The selected MSN's  $M_A$  value will be updated as  $M_A = M_T$ , only on successful completion of sensing operations at the RSP.

#### A. SELECTION OF SUITABLE MSN TO ATTEND RSP

A Min-Heap is created with the  $M_N$  number of tuples to identify the tuple with the smallest  $M_T$  value.  $M_T$  is considered as the key value for the Min-Heap creation, as shown in Algorithm 5.

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#### Algorithm 5 Heap Creation / Insertion

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```

1: Min Heap ( M[ID,P,T] )
2: if (Min Heap == NULL) then
3:   M[ID,P,T] = Root
4: else
5:   Add M[ID,P,T] to the bottom level of Min Heap
6:   Compare MT with its ParentT
7:   Swap the M[ID,P,T] with its ParentID,P,T
8:   [If not in order], Repeat previous step
9: end if

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The root node will always have the smallest key value in a Min-Heap. In some cases, it may be possible that more than one node may have the same value as  $M_T$ . It causes a tie between the MSNs.

If the  $M_T$  value of the root node and its left node is the same, then the value of  $M_P$ , i.e., the total number of RSPs attended by the root, gets compared with the left node. The same procedure is applied, in case of root node and its right node  $M_T$  values is same. The root node will get replaced with a left node or right node, which has attended less number of RSPs, as shown in Algorithm 6.

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#### Algorithm 6 Selection of Suitable MSN

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```

1: if RootT = RightT = LeftT then
2:   if Leftp > Rightp then
3:     Swap: Root Node with Right Node
4:   else
5:     Swap: Root Node with Left Node
6:   end if
7: end if
8: if RootT = LeftT then
9:   Check: Rootp > Leftp
10:  Swap: Root Node with Left Node
11: end if
12: if RootT = RightT then
13:  Check: Rootp > Rightp
14:  Swap: Root Node with Right Node
15: end if
16: M[ID,T] = Root
17: Delete: Min Heap

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The Min-Heap will get deleted after the successful selection of the root node. Since the value of the RSP is a random number, the Min-Heap created for a particular RSP is not helpful for other RSPs. Hence the creation and deletion of Min-Heap are done for all the RSPs. Algorithm 6 is helpful for the identification of the most suitable MSN to attend the RSP.

#### B. MOBILITY OF THE SELECTED MSN TO THE LOCATION OF RSP

The location of RSP can be calculated from  $R_L$ , where  $R_R$  stores the value of the row, and  $R_C$  holds the column value on that particular row.  $M_R$  and  $M_C$  hold the current location

of the MSN.  $M_R$  and  $M_C$  represent the values of the row and column in which the MSN is currently standing. The selected MSN has to travel from the source ( $M_R, M_C$ ) to the destination ( $R_R, R_C$ ).

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**Algorithm 7** Mobility of the Selected MSN to the Location of RSP
 

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1: Source ( $M_{[ID, R, C]}$ )
2: Destination ( $R_{[ID, R, C]}$ )
3:  $RT = M_R - R_R$ 
4:  $CT = M_C - R_C$ 
5: while ( $M_L == R_L$ ) do
6:   MSN Status Check (Algorithm 3)
7:   if  $M_S = 1$  then
8:     if  $M_R > R_R$  then
9:       Move MSN RT times in down direction
10:    else
11:      Move MSN RT times in up direction
12:    end if
13:    if  $M_C > R_C$  then
14:      Move MSN CT times in left direction
15:    else
16:      Move MSN CT times in right direction
17:    end if
18:  end if
19: end while
  
```

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If the row value of MSN and RSP are identical, then the MSN needs to move in either the left or the right direction, depending on the column value. If the MSNs row value is higher than the RSPs row value, then MSN has to travel from top to bottom. Otherwise, it has to travel in the bottom to top direction. Top to bottom means traveling from the highest to the least valued row. Lowest to highest means traveling from least valued row to highest valued row.

If the column value of MSN is greater than the column value of RSP, then the MSN needs to move in the left direction, otherwise, in the right direction. Moving left to right means traveling from the least valued column to the highest valued column, and right to the left stands the highest valued column to the least valued column, as shown in Algorithm 7.

In some cases, the current location of the selected MSN and the location of RSP may be the same, and then the MSN need not move. It can directly start sensing operations.

Due to travel, the current location of the MSN changes with every move. Once the MSN reaches the RSP, the current location of the MSN will get updated with the value of the RSP. This value remains unchanged till the next move. The same MSN may or may not get selected to attend the next RSP.

Data structure  $D_M$  holds the values of the parameters shown in Table 3 along with the parameters detailed in Table 2. Some parameters related to the battery and depletion are defined as shown in Table 3. Other than  $M_{ID}$ , other parameter

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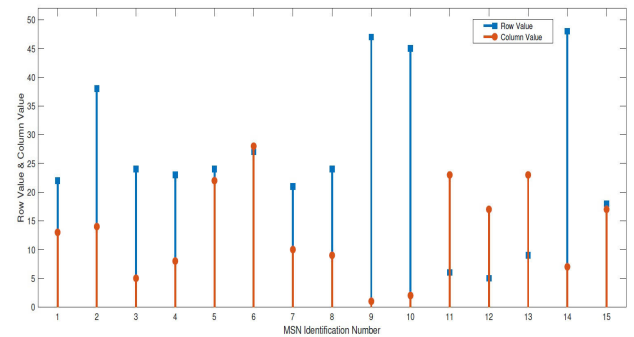
**Algorithm 8** Sensing Operations at the RSP
 

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1: if  $M_L = R_L$  then
2:   MSN Status Check (Algorithm 3)
3:   if  $M_S = 1$  then
4:     Perform sensing operations at RSP
5:   end if
6: end if
7: if Sensing operation at RSP = Successful then
8:    $M_P = M_{P+1}$ 
9:   Update:  $R_S = 1$ 
10: else
11:   Update:  $R_S = 0$ 
12: end if
  
```

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**FIGURE 2.** MSNs landed positions on the ROI.

values keep changing as the MSNs move from one location to another. These values will get updated when required at regular intervals.

### C. MSN OPERATIONS AT RSP

Once the selected MSN reaches the RSP, the communication and co-ordination activities will be performed. Sensing operations will be performed at the RSP. The kind of the sensing operations are subject to the application. Time and energy required for the sensing operations are application specific. On successful completion of sensing operations, the value of  $M_P$  will be increased by 1 for the MSN. A signal will be sent to the event handler to mark the event as completed, as shown in Algorithm 8. If an MSN fails during the traversal or the sensing operations, then Algorithm 1 will rerun from activity number A2.

## VI. RESULTS AND DISCUSSIONS

For simulation purposes, ROI of size 50 rows ( $Y$ ) and each row with 30 regular hexagons ( $X$ ) is used. The word sensing point and regular hexagons are used interchangeably. Sensing points are numbered from 1 to 1500. The sensing point with identification number 1 is on row number 1 at position 1 on that row ( $X_1, Y_1$ ), and the sensing point with the number 1500 is on row number 50 at position 30 on that row ( $X_{50}, Y_{30}$ ).

A group of 15 MSNs are deployed randomly over the ROI. These MSNs are expected to land successfully on the ROI

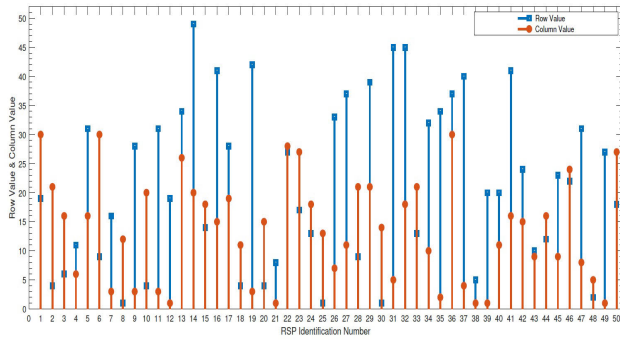


FIGURE 3. RSPs location on the ROI.

at any sensing point. The landing locations of the MSNs are identified with sensing point numbers.

Let  $\alpha$  be the sensing point on which an MSN is landed successfully,  $\alpha$  being the hexagon number on the ROI. Using Equations (2) and (3), the row number  $M_R$  and column number  $M_C$  are calculated as follows.

$$M_R = \lfloor \frac{\alpha}{Y} \rfloor + 1 \tag{2}$$

$$M_C = \alpha - (\lfloor \frac{\alpha}{Y} \rfloor \times Y) \tag{3}$$

For the  $M_N$  number of active MSNs, a set of  $M_N$  number of random numbers ( $\alpha$ ) are generated. Since  $M_R$  and  $M_C$  are derived from random numbers, the values of  $M_R$  and  $M_C$  differ among all the  $M_N$  number of MSNs.

In some cases, a few values of the  $M_R$  may be the same, but the values of  $M_C$  will differ. In some other cases, the value of  $M_C$  may be the same, but the value of  $M_R$  will vary.

MSN with identification 1 is landed on sensing point 643, which is at the 13th column position of the 22nd row. On row number 24 at column position 22, an MSN with identification number 5 is landed. MSN with identification 10 is landed on the sensing point 1322, which is at 3 column position of the 45th row.

Similarly, MSN with identification 15 is landed on sensing point 527, at the 17th column position of 18 row. In the simulation, proper validation is set to ensure that no more than one MSN can be landed on a single sensing point. This avoids collision between the MSNs at random deployment, as shown in Figure 2.

By definition Random Sensing Point (RSP) is the sensing point from which the information needs to be collected by anyone MSN. It is assumed that all the MSNs landed safely on various sensing points before the generation of the Random Sensing Points.

Let  $\beta$  be the RSP from which the information needs to be collected by the MSN. The RSP( $\beta$ ) can be any one among the total number of hexagons. The row number  $R_R$  and column  $R_C$  are calculated using Equations (4) and (5).

$$R_R = \lfloor \frac{\beta}{Y} \rfloor + 1 \tag{4}$$

$$R_C = \beta - (\lfloor \frac{\beta}{Y} \rfloor \times Y) \tag{5}$$

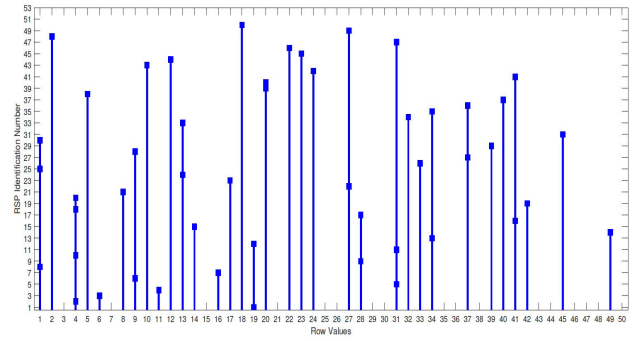


FIGURE 4. RSPs row wise occupancy on the ROI.

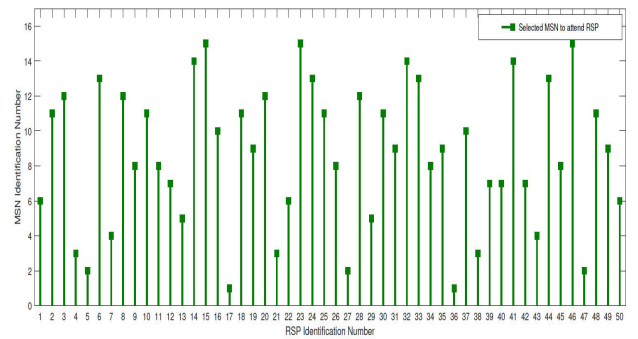


FIGURE 5. MSN got selected to attend the RSP.

In Figure 3, the row number and column values for the RSPs are shown. The row value is indicated with a blue color marker, and the column position is marked with a red color marker. RSP 1 is located at location 570, on row number 19 and column number 30. On row number 1, RSP 25 is identified at column value 13. Similarly, RSP 50 is located at the 27th position on row number 18, which is the sensing point 537.

In some cases due to the random generation of RSPs, more than one RSP is seen on the same row at different column values. RSP 8, 25, and 30 are on row number 1 at positions 12, 13, and 14. These three RSPs are adjacent to each other. A similar observation is made in rows 4 and 41. Row number 4 contains a maximum of 4 RSPs, and row number 31 contains a maximum of 3 RSPs. It is noticed that a few rows are empty, as shown in Figure 4. No random sensing points are generated for row numbers 3, 7, 15, 21, 25, 26, 29, 30, 35, 35, 43, 44, 46, 47, 48 and 50.

In Figure 5, the MSNs that got selected to attend the RSPs are shown. MSN 6 is identified as the most suitable one to attend the RSP 1. To attend RSP 25, MSN 11 is selected as the most suitable. MSN 9 is identified as the most appropriate to attend the RSP 35.

Since the total number of RSPs is more than the total number of active MSNs ( $R_N \gg M_N$ ), a few MSNs got an opportunity to attend more than one RSP.

MSN with identification number 1 has attended RSP 17 and 36. RSP 13 and 29 are served by MSN 5. RSP 16 and 37 are served by MSN 10. MSN with identification number 15 has attended RSP 15, 23 and 46. MSN 11 attended a total

TABLE 3. Description for symbols associated with energy parameters.

Symbol	Description
$E_I$	Energy at the time of deployment
$E_D$	Energy depleted due to unit traversal
$E_S$	Energy depleted due to sensing operations
$E_C$	Energy depleted due to communication & co-ordination activities
$E_T$	Total energy depleted by the MSN
$E_R$	Residual energy of the MSN

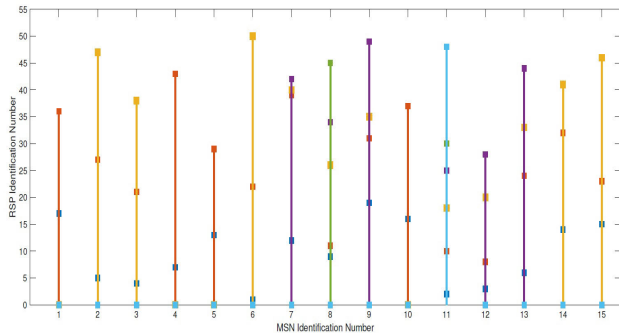


FIGURE 6. Identification numbers of RSPs that are attended.

of 6 RSPs, namely 2, 10, 18, 25, 30, and 48. MSN 8 has attended 5 RSPs, namely 9, 11, 26, 34, and 45. MSN 7, 9, 12, and 13 each has attended 3 RSPs. MSN 1, 4, 5, and 10 each has attended 2 RSPs. None of the MSN is idle; all the MSNs have participated in attending the RSPs, as shown in Figure 6. Let  $E_\delta$  represent the amount of energy that is depleted by the MSN to perform sensing operations at an RSP which includes energy depleted due to the traversal to reach the RSP, energy depleted for coordination and communication activities, and sensing operations at the RSP, as shown in Equation (6).

$$E_\delta = \sum_{i=1}^{n1} E_D + \sum_{i=1}^{n2} E_C + \sum_{i=1}^{n3} E_S \quad (6)$$

MSN depletes a certain amount of energy on every move. The energy consumed due to the traversal to reach the RSP is denoted as  $\sum_{i=1}^{n1} E_D$ , where n1 is the number of units of distance between the MSN and target location.

During the traversal and at every regular interval, MSNs need to coordinate and communicate with central systems. This activity consumes a certain amount of energy, denoted as  $\sum_{i=1}^{n2} E_C$ , where n2 is the number of times the MSN has performed coordination and communication.

Once the MSN reaches the target location, it has to perform sensing operations and pass the information to the central system for further processing; it is denoted as  $\sum_{i=1}^{n3} E_S$ , where n3 is the total units of time taken to perform sensing and other operations at the target location.

The number of times an MSN got selected to attend the RSPs may differ from other MSNs. An MSN may get fewer number chances, and some other MSNs might get more

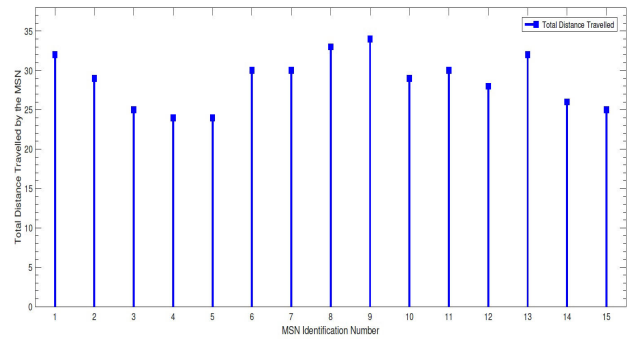


FIGURE 7. Total distance travelled by the MSN.

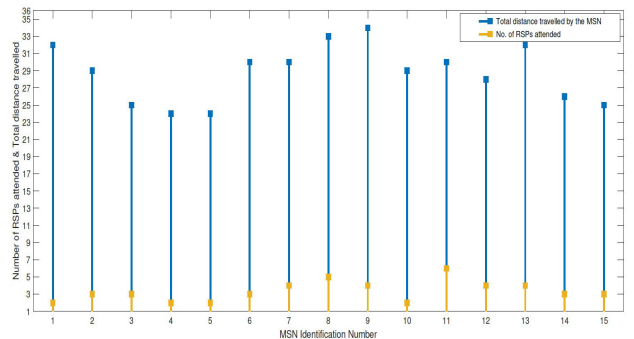


FIGURE 8. No. of RSPs attended & Total distance travelled by the MSN.

number chances compared to their counterparts. Hence the total distance traveled by the MSNs also differs.

Figure 7 shows the identification numbers of the RSPs attended by the MSN. MSN 9 has traveled the longest path of 34 units. This MSN has served 4 RSPs, namely 19, 31, 35, and 49. It has traveled 7 units of distance to attend RSP 19 and 5 units of distance to attend RSP 31, 14 units of distance to attend RSP 35 and 8 units of distance to attend RSP49.

MSN 11 got the opportunity to attend 6 RSPs. The total distance traveled by this MSN is 30 units. To attend RSP 2, it has traveled 4 units of distance; to attend RSP 10 and RSP 30, it has traveled a distance of 1 unit each. To attend RSP 25, it has traveled 5 units of distance. It has traveled the longest distance of 10 units to reach RSP 48, as shown in Figure 7.

Figure 8 shows that MSN 9 has attended 4 RSPs but has traveled 34 units of distance. MSN 11 has served 6 RSPs and the total distance traveled by the MSN is 30 units, less than the distance traveled by MSN 9. MSN 6 has traveled 30 units of distance to attend 3 RSPs. MSN 8 has traveled 33 units of distance to attend 5 RSPs. MSN 1 covers a total distance of 32 units to attend RSP12 & RSP20.

Energy depleted to attend a RSP, including sensing operations at the RSP, can be calculated using Equation 6. The total number of RSPs covered by the MSN is stored in  $M_p$ . The total amount of energy depleted to attend all the  $M_p$  number of RSPs is calculated using Equation 7, where  $E_\delta$  represents the amount of energy that is depleted by the MSN to perform sensing operations at an RSP which includes energy depleted due to the traversal to reach the RSP, energy

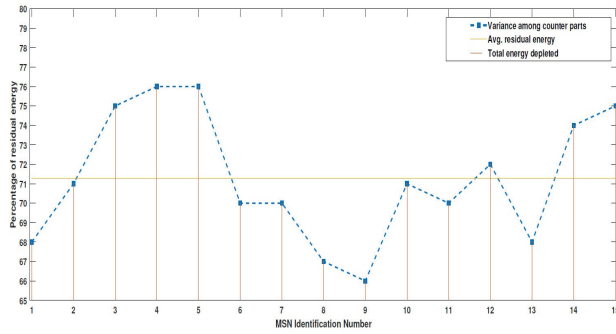


FIGURE 9. Percentage of residual energy after attending 50 RSPs.

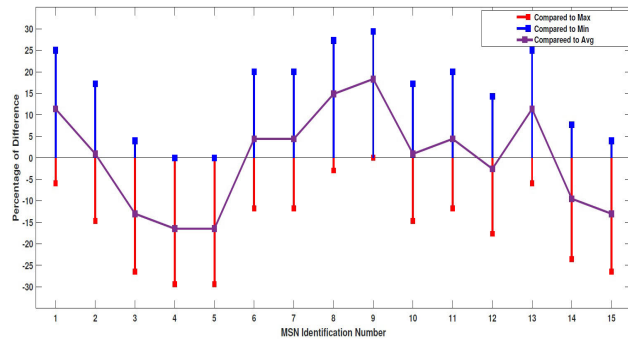


FIGURE 10. Percentage of variance from Max, Min & Average.

depleted for coordination and communication activities, and sensing operations at the RSP and  $E_T$  is the total energy depleted by the MSN. The residual energy for the MSNs can be calculated as  $(1 - E_T)$ .

$$E_T = \sum_{i=1}^{M_p} E_{\delta i} \quad (7)$$

The percentage of residual energy after attending 50 RSPs by the MSNs is shown in Figure 9. It is observed that all the MSNs have an approximately equal amount of residual energy. The average value of residual energy is 71.2267. MSN 8 has the highest residual energy of 5.98 % units above the average. MSN 5 has the lowest amount of residual energy which is 6.64 % below the average. MSN 2 and 10 are very much closer to the average residual energy.

The percentage of variance with maximum, minimum, and average distance traveled after attending altogether, 50 RSPs by the MSNs are shown in Figure 10. The average distance traveled by the MSNs is 28.73 units. The maximum and minimum distances traveled by the MSNs are 34 and 24 units respectively. The leading variance with maximum distance traveled is -29.41 percent. The minimum variance with maximum distance traveled is -5.88 percent. The maximum variance with minimum distance traveled is +29.41%. The minimum variance with the minimum distance traveled is +4 %. Compared with the average distance traveled by the MSNs, the maximum variance is +18.32 %, and the minimum variance is -16.47 %.

TABLE 4. Maximum, Minimum and Standard deviation of the MSNs.

X1	X2	X3	X4	X5	X6	X7	X8
100	78	6	56	9	931	62	6
200	145	2	119	8	1982	132	7
300	220	6	197	11	3124	208	7
400	286	5	272	12	4197	279	5
500	364	6	342	1	5263	350	6
600	425	12	403	5	6225	415	6
700	503	9	477	5	7352	490	7
800	574	12	552	10	8482	565	7
900	647	14	629	1	9543	636	5
1000	723	14	699	9	10675	711	7
1100	785	11	758	10	11587	772	7
1200	860	10	835	8	12722	848	8
1300	928	2	908	11	13749	916	6
1400	1003	6	972	8	14763	984	7
1500	1066	10	1041	7	15776	1051	7

[X1 = Number of Simulations, X2 = Max Value, X3 = Max MSN ID, X4 = Min Value, X5 = Min MSN ID, X6 = Total, X7 = Avg., X8= Std. Deviation]

Simulations are run up to 1500 RSPs from 100 RSPs at the interval of 100. This section focuses on understanding the model’s behavior in traveling distances of an individual MSN among the group of MSNs. It highlights the comparison of distances traveled and residual energy.

As shown in Table 4, a total of 1500 RSPs are generated at a difference of 100. For the first 100 RSPs, the total distance traveled by all the MSNs is 931. MSN 6 has traveled a maximum distance of 78 units. MSN 9 has traveled a minimum distance of 56 units. The average distance traveled is 62 units.

With 100 RSPs, the maximum difference in distance traveled by the MSNs is 7 units. The exact value of the difference was also observed at 500, 600, and 1300 number of simulations. A maximum of 5 units of difference in the total distance traveled among the MSNs is observed when the number of simulations is 400. The maximum value for difference among the MSNs is 7 units that is observed at 200,300, 700, 800, 1000, 1100, 1400, and 1500 simulations.

As shown in Figure 11 and Table 5, the difference between the maximum and minimum distances traveled by all the MSNs decreases gradually. It is also observed that the maximum, minimum and average distances traveled by all the MSNs are closer to each other as the number of simulations increases.

For 1500 simulations, the difference between the maximum and minimum distances traveled by all the MSNs lies in the range of 14 units to 31 units, with an average of 23 units. Figure 12 shows the distance traveled by all the MSNs for simulations from 100 to 1500 at the intervals of 100. This figure depicts the total distance traveled by the MSNs is getting closer as the number of simulations increases.

During the first 100 simulations, the values are very little apart. As the number of simulations increases, the values get



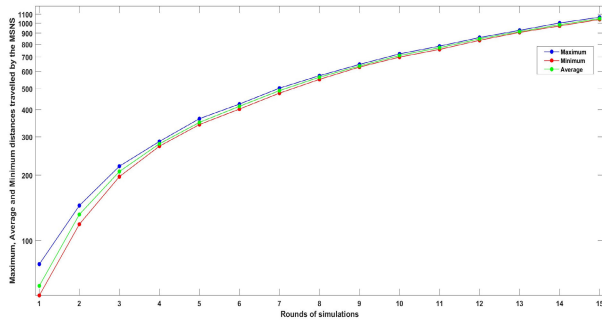


FIGURE 11. Maximum, Average & Minimum Distances travelled by all the MSNs at the interval of 100 rounds.

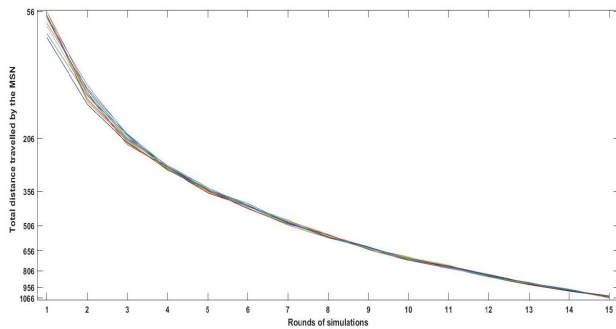


FIGURE 12. Total distance travelled by the MSN at the interval of 100 rounds.

closer to each other. This is because, during the initial round of simulations, few MSNs have the opportunity to travel and attend the RSPs. As the number of RSPs increases, the workload is shared among the MSNs. Hence after 400 runs of simulations, the total distance traveled by the MSNs is nearly equal.

The total distance traveled by the MSN to attend  $M_P$  number of RSPs can be written as Equation 8, where  $M_{Ei}$  is the number of units of travelled.

$$M_{DT} = \sum_{i=1}^{M_P} M_{Ei} \tag{8}$$

The value of  $M_{DT}$  will vary from MSN to MSN, this is due to the value of  $M_P$  and  $M_{Ei}$ . The value of  $M_{Ei}$  depends on the value obtained from Equation 1, which depends on the location of MSN and RSP. The total number of RPS generated is  $R_{Count}$ ; which is equivalent to the sum of  $M_P$  of all MSNs.

As the value of  $R_{Count}$  increase during the simulations, the value of  $M_P$  may increase for few MSNs. In some cases, the value of  $M_P$  for certain MSNs may not increase but the value of  $M_T$  may increase. The raise in the value of  $R_{Count}$  provides more and more opportunities to MSNs. Hence the total distance traveled increases gradually.

It is important to ascertain the total distance traveled by the MSNs after 1500 simulations. The average distance traveled by the MSNs is 1051 units. MSN with identification

TABLE 5. Distance travelled by the MSNs for 1500 RSPs.

	Y1	Y2	Y3	Y4	Y5	Y6	Y7	Y8
1	1052	14	11	0.267	1.33080	1.04563	0.0253	
2	1054	12	13	2.267	1.13852	1.23340	0.2150	
3	1047	19	6	-4.733	1.81471	0.57307	-0.4520	
4	1061	5	20	9.267	0.47125	1.88501	0.8734	
5	1050	16	9	-1.733	1.52381	0.85714	-0.1650	
6	1054	12	13	2.267	1.13852	1.23340	0.2150	
7	1041	25	0	-10.733	2.40154	0.00000	-1.0310	
8	1059	7	18	7.267	0.66100	1.69972	0.6862	
9	1047	19	6	-4.733	1.81471	0.57307	-0.4520	
10	1066	0	25	14.267	0.00000	2.34522	1.3383	
11	1054	12	13	2.267	1.13852	1.23340	0.2150	
12	1050	16	9	-1.733	1.52381	0.85714	-0.1650	
13	1043	23	2	-8.733	2.20518	0.19175	-0.8373	
14	1044	22	3	-7.733	2.10728	0.28736	-0.7407	
15	1054	12	13	2.267	1.13852	1.23340	0.2150	

[Y1 = MSN ID, Y2 = Total distance traveled, Y3 = Difference from Max, Y4 = Difference from Min, Y5 = Difference from Avg, Y6 = % of Y3, Y7 = % of Y4, Y8 = % of Y5]

number 10 traveled a maximum distance of 1066 units for 1500 simulations; similarly, MSN with identification number 7 traveled a minimum distance of 1041 units.

From Table 5, it can be seen that the difference in average distance traveled by the MSNs lies in the range of -1.03 % to +1.3%. MSN 7 has a variance with the average distance traveled being -1.03%. MSN 10 has a variance of +1.33% with the average distance traveled. It has to be observed that other than MSN 7 and 10, all the other MSNs have variance with an average distance traveled which is as small as 0.8 units. This shows that MSNs have traveled almost equal units of distances. For a few MSNs, the variance in average distance traveled is -0.16 and 0.02. These results confirm that the MSNs have depleted an equal amount of energy by traveling approximately equal units of distance.

MSNs deplete the maximum amount of energy during the traversal compared to sensing and other operations. Hence in the above paragraphs, the discussion is wholly devoted to energy depletion due to traversal. The energy depleted by the MSN during the communication, coordination, and sensing operations needs to be included for a detailed understanding of the proposed model. In the literature many models are available for calculating the energy usage and battery depletion. Models described in [20] and [21] are generic and hence are applied in this work.

Unit of energy depletion is defined as the amount of energy depleted due to a unit traversal and is denoted as  $C_1$ . The amount of energy consumed due to communication and sensing operations is  $C_2$  and the amount of energy consumed due to sensing operations is  $C_3$ . The relationships between  $C_1$ ,  $C_2$  and  $C_3$  can be established as  $C_1 = \gamma_1 \times C_2$  and  $C_1 = \gamma_2 \times C_3$ . During the simulation  $C_1$  is set as 1 and  $C_2 + C_3$  is

**TABLE 6.** Residual energy of MSNs after 1500 RSPs.

Z1	Z2	Z3	Z4	Z5	Z6	Z7
1	1052	101	101	0.00287907	0.026397516	0.035507845
2	1054	117	117	0.03007037	0	0.063483815
3	1047	91	91	-0.01711452	0.045807453	0.014863749
4	1061	91	91	-0.00591810	0.034937888	0.026424443
5	1050	98	98	-0.00351887	0.032608696	0.028901734
6	1054	103	103	0.00767754	0.02173913	0.040462428
7	1041	88	88	-0.02671145	0.055124224	0.004954583
8	1059	95	95	-0.00111964	0.030279503	0.031379026
9	1047	82	82	-0.03150991	0.059782609	0
10	1066	90	92	-0.00351887	0.032608696	0.028901734
11	1054	109	109	0.01727447	0.01242236	0.050371594
12	1050	118	118	0.02847088	0.001552795	0.061932287
13	1043	106	106	0.00367882	0.025621118	0.036333609
14	1044	87	87	-0.02591170	0.054347826	0.005780347
15	1054	114	114	0.02527191	0.004658385	0.058629232

[Z1 = MSN ID, Z2 = Total distance traveled, Z3 = No. of RSPs attended, Z4 = No. of Comm. & Co-ord. activities, Z5 = % of difference from Avg, Z6 = % of difference from Max, Z7 = % of difference Min]

set as 1.

$$E_{\delta} = C_1 \times E_D \sum_{i=1}^{M_p} n1 + C_2 \times E_C \sum_{i=1}^{M_p} n2 + C_3 \times E_O \sum_{i=1}^{M_p} n3 \tag{9}$$

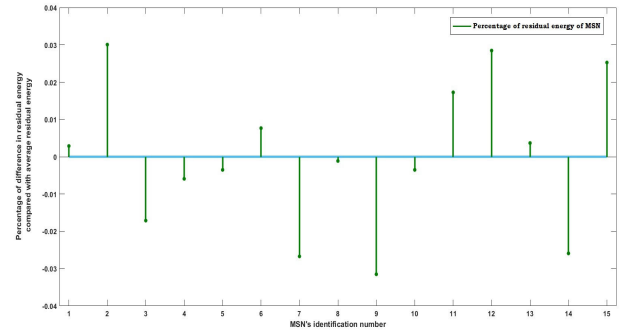
As shown in Table 6, the MSN 10 has traveled a maximum distance of 1066 units with 90 attended RSPs. Similarly, MSN 7 has traveled a minimum distance of 1041 units with 88 attended RSPs. The average value of units of distance traveled by the MSNs is 1250. The MSN 12 has participated in a total of 118 RSPs with a total traveling of 1050 units. MSN 9 has participated in a total of 82 RSPs with a total travel of 1047 units.

The total distance traveled by the MSNs has no direct connection with calculating the number of RSPs attended. In some cases, an MSN may need to travel few units of distance to reach the RSP while in other cases, an RSP may make the MSN to travel larger distances.

$$E_{R1} = E_{I1} - E_{\delta1} \tag{10}$$

The value of  $E_{I1}$  is equal for all the MSNs at the time of deployment, hence the value of  $E_{R1}$  depends on the value of  $E_{\delta1}$ . From the Equation 9, it can be ascertained that, this value depends on the value of  $M_p$  and other parameters. Equation 10, is used to calculate the residual energy.

Let  $E_N$  be the set that contains the values denoted as  $E_{R1}, E_{R2}, E_{R3} \dots E_{RM}$ , where  $E_{RN}$  is the value of value of residual energy of MSN<sub>N</sub>. Hence the set  $E_N$  contains N number of  $E_R$



**FIGURE 13.** Percentage difference in residual energy compared with average energy depletion.

values that belong to N number of MSNs

$$E_M = \{E_{R1}, E_{R2}, E_{R3} \dots E_{RN}\}$$

$$E_{Min} = \min_{a_N \in S_N} \{E_M\} \tag{11}$$

$$E_{Max} = \max_{a_N \in S_N} \{E_M\} \tag{12}$$

$$E_{Avg} = \frac{1}{N} \sum_1^N \{E_M\} \tag{13}$$

The average residual energy of all the MSNs is calculated using Equation 13. This value is compared with the residual energy of all the MSNs.

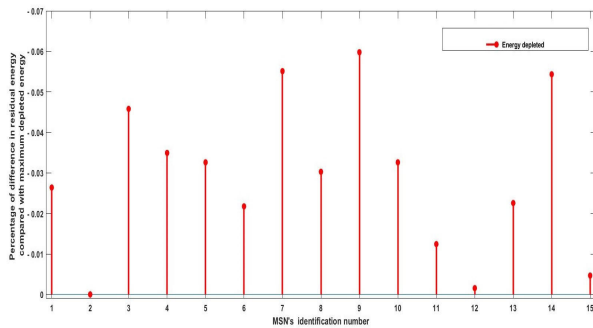
The percentage of maximum difference with average is 0.030070377 units. The rate of minimum difference with average is -0.031509917 units. The remaining values are within the range. This difference is very small. This shows that the energy consumption & energy depletion of all the MSNs are nearly equal to the average energy consumption & energy depletion, as shown in Figure 13.

The MSN which has depleted the maximum energy among all the MSNs is identified using Equation 12. That MSNs  $E_R$  value is considered as the base value and compared with all the other MSNs  $E_R$  value.

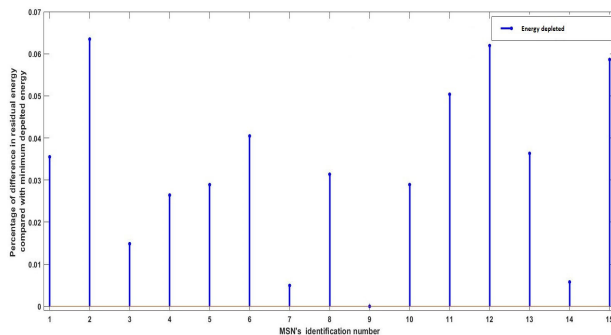
The MSN 2 has traveled a distance of 1054 units; other activities include 234 units of depletion; this MSN has 1288 units of energy depletion, which is the maximum among all the MSNs. The residual energy of this MSN is compared with other MSNs, as shown in Figure 14. The percentage of difference in residual energy compared to maximum energy depletion is 0.059782609 units.

The MSN which has depleted the minimum energy among all the MSNs is calculated using Equation 11. That MSNs  $E_R$  value is considered as the base value and compared with all the other MSN's  $E_R$  value.

MSN 9 has traveled a distance of 1047 units, and other activities consume 164 units, total energy depletion is 1211 units, which is the minimum among all the MSNs. The residual energy of this MSN is compared with other MSN. The percentage of difference in residual energy compared with minimum energy depletion is 0.063583815 units, as shown in Figure 15.



**FIGURE 14.** Percentage difference in residual energy compared with maximum energy depletion.



**FIGURE 15.** Percentage difference in residual energy compared with minimum energy depletion.

Figures 13, 14, 15, and Table 6 clearly show that the proposed approach makes the MSNs deplete approximately equal amounts of energy, hence the residual energy is also approximately equal. The values in Table 5 and Table 6 are shown in decimal values with 9 digits after the decimal. In some cases, the value of unit energy may be very large; hence more number of decimal values are used to get the precision.

## VII. CONCLUSION

Mobile Sensor Nodes are randomly deployed over the region of interest and allowed to sense the environmental information from random locations. Mobile sensor nodes energy depletion is computed by calculating the distances that needs to be traveled using the modified Min-Heap method. The simulation results show that the MSNs have traveled approximately equal distances. Hence the energy depletion and residual energy levels are nearly same for all the MSNs.

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