

Graph-based Facial Affect Analysis: A Review

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Abstract—As one of the most important affective signals, facial affect analysis (FAA) is essential for developing human-computer interaction systems. Early methods focus on extracting appearance and geometry features associated with human affects while ignoring the latent semantic information among individual facial changes, leading to limited performance and generalization. Recent work attempts to establish a graph-based representation to model these semantic relationships and develop frameworks to leverage them for various FAA tasks. This paper provides a comprehensive review of graph-based FAA, including the evolution of algorithms and their applications. First, the FAA background knowledge is introduced, especially on the role of the graph. We then discuss approaches widely used for graph-based affective representation in literature and show a trend towards graph construction. For the relational reasoning in graph-based FAA, existing studies are categorized according to their non-deep or deep learning methods, emphasizing the latest graph neural networks. Performance comparisons of the state-of-the-art graph-based FAA methods are also summarized. Finally, we discuss the challenges and potential directions. As far as we know, this is the first survey of graph-based FAA methods. Our findings can serve as a reference for future research in this field.

Index Terms—Facial Expression Recognition, Micro-expression Recognition, Action Unit Detection, Graph Representation, Graph Relational Reasoning, Graph Neural Network.

1 INTRODUCTION

FACIAL affects relate to 55% of messages when people perceive others' feelings and attitudes [1, 2] because it conveys critical information that reflects emotional states and reactions in human communications [3, 4, 5]. Many facial affect analysis (FAA) methods have been explored during the past decade, benefiting from interdisciplinary studies of affective computing, computer vision, and psychology [6, 7, 8]. Some have been extended to many applications, including medical diagnosis [9], social media [10], e-education [11], and video generation [12]. Meanwhile, competitions such as FERA [13], EmotiW [14], Aff-Wild [15], ABAW [16], EmotioNet [17], AVEC [18], and MuSe [19] are regularly held to evaluate the latest progress and propose frontier research trends.

Historically, FAA methods have undergone a series of evolutions. Initial studies usually rely on hand-crafted design or classic machine learning to obtain useful affective features without structural information [7, 20]. Psychological findings indicate that the human cognition of facial information is realized through a dual system composed of analytic processing and holistic processing [4]. The former acquires multi-dimensional cluster features by analyzing local areas, while the latter aims to generate a holistic representation to perceive the overall structure [4, 21]. Such an analytic-holistic working system is similar to a topology-like structure, so it is reasonable for machine vision researchers to model it into a graph. Accordingly, many state-of-the-art studies have been dedicated to generating a facial graph with local-to-global affective features [22, 23, 24, 25].

If the above evidence reveals the feasibility of using graph-based methods for FAA, research on how facial muscles participate in affective expression further demonstrates its possibility as a necessary condition [26, 27, 28]. There are latent relationships among different facial areas and contexts, which are vital clues [29, 30]. A few non-graph-based deep models have partly captured these relationships and improved performance [31, 32, 33]. The underlying assumption is that explicit mappings that reflect this relationship can be directly learned [34]. However, these mappings are not solid enough in the real world because they differ from subject to subject and even from one condition to another [35, 36]. Recently, graph-based methods have shown that they represent facial anatomy and simultaneously fit latent relationships in facial affects [37, 38, 39]. Some pilot studies have also suggested that the graph-based method can even move beyond to deal with challenging tasks such as analyzing occluded faces [40, 41] and ambiguous facial affects [42, 43].

By searching on Google Scholar using keywords of 'graph' and **Index Terms** in this survey, we have counted the number of relevant published papers from 2010 to the present. As presented in Fig. 1, the graph-based FAA has gained increasing attention, especially in the past five years (publications in 2021 increased by 600 year-on-year).

Based on theoretical support, outstanding performance and quantity of existing work, and potential for future development, it is necessary to review the state of graph-based FAA methods. Although many reviews have discussed FAA's historical evolutions [7, 34, 44] and recent advances [45, 46, 47], including some specific problems like occluded expression [48], multi-modal affect [49] and micro-expression [50], **this is the FIRST systematic and in-depth survey for the graph-based FAA field** as far as we know. We emphasize representative research proposed after 2010. The goal is to present a novel perspective on FAA and its latest trends.

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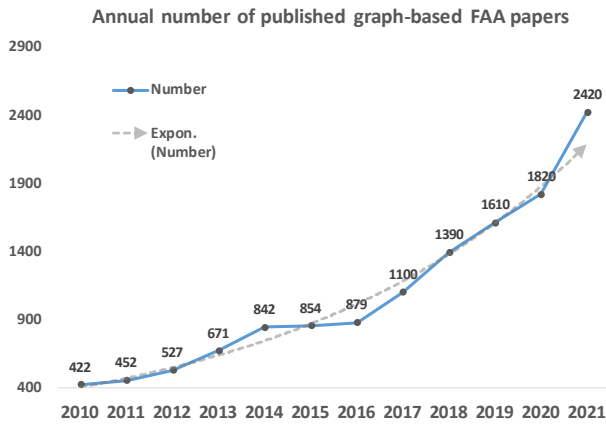


Fig. 1. The growth trend of papers related to graph-based FAA.

This review is organized as follows: Section 2 provides a brief background on FAA and discusses the unique role of graph-based methods in FAA research. Section 3 presents a taxonomy of mainstream graph-based methods for affective representation. Section 4 reviews classical and advanced approaches for graph relational reasoning and discusses their pros and cons in FAA tasks. Section 5 summarizes public databases, main FAA applications, and current challenges based on a detailed comparison of related literature. Finally, Section 6 identifies potential research directions.

2 FACIAL AFFECT ANALYSIS

2.1 Affective Description Model

As early as the 1970s, Ekman and Friesen [51] proposed the definition of six basic affects, i.e., *happiness*, *sadness*, *fear*, *anger*, *disgust*, and *surprise*, based on an assumption of the universality of human affective display [26]. In addition, compound affects [52] defined by different combinations of basic affects (e.g., *sadly surprise* and *happily surprise*) are proposed to depict more complex affective situations [53]. Another kind of famous description, called Facial Action Coding System (FACS), is designed for a broader range of affects, which consists of a set of atomic Action Units (AUs) [21, 30]. Fig. 2 shows an example of six basic affects plus *neutral* and activated AUs in each facial affect. Besides categorical models, a continuous affective model named VAD Emotional State Model [54] is also suggested [55, 56, 57]. It has three dimensions, i.e., *valence* (how positive or negative an affect is), *arousal* (the activation intensity of an affect), and *dominance* (how submissive or in-control a person is in an affective display). The continuous model describes human affects quantitatively and is appropriate to depict dynamic changes [45, 58]. Please refer to [7, 44] for a more detailed discussion about this topic.

2.2 General Pipeline

A standard FAA method can be broken down into fundamental components: face preprocessing, affective representation, and task analysis. As a new branch of FAA, the graph-based method also follows this generic pipeline (see Fig. 3). Face detection and registration are two necessary pre-steps that first locate faces and normalize facial variations, sometimes also providing facial landmarks [60, 61]. Fig. 4 presents an illustration of the preprocessing steps. Early methods like *Viola and Jones* [62], *Mixtures of Trees* [63], and *Active Appearance Model (AAM)* [64] have been widely

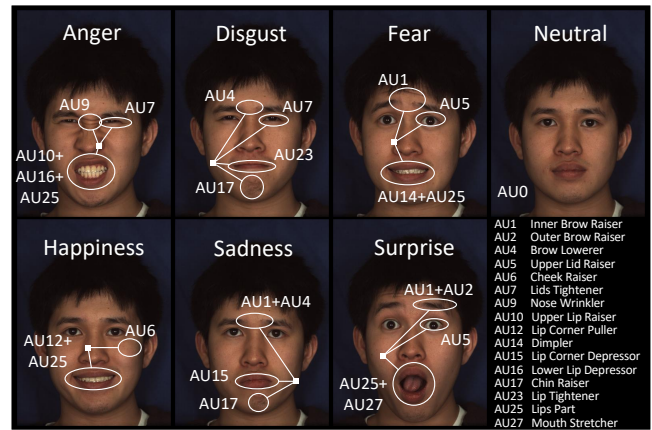


Fig. 2. An example of basic facial affects and related AU marks. AU0 denotes no activated AU. All annotations are made by FACS certificated experts. Images are from BU-4DFE [59] database.

used for this purpose. Recently, cascaded deep approaches with real-time performance are popular, such as *Multi-Task Cascaded Convolutional Network* [65], *Hyperface* [66], and *Supervision by Registration and Triangulation* [67]. Please refer to [68, 69, 70] for more specific information.

Compared to other existing methods, the graph-based FAA pays more attention to representing facial affects with graphs and obtaining affective features from such representation by graph reasoning. The two components can perform separately or arranged as an end-to-end framework. They are expected to exhibit better performance and generalization capability by manually or automatically providing richer information through prior knowledge.

In mathematical terms, a graph can be denoted as $G = (V, E)$. The node set V contains all the representations of the entities in the graph, and the edge set E contains all the structure information between two entities. Thus, when E is empty, G becomes an unstructured collection of entities (e.g., independent local facial areas [31]). Meanwhile, we could also define some initial graph structure, usually denoted in the form of an adjacency matrix A , ahead of the relational model, which is a general practice in many affective graph representations [25, 40, 72].

Given this unstructured collection, performing relational reasoning requires the model to infer the structure of these entities before predicting the property or category of an object. Naturally, generic approaches need to be adjusted depending on affective graph representations or propose new graph-based approaches to infer the latent relationship and extract the final affective feature.

In the rest of this survey, different graph generation methods and their relational reasoning approaches will be systematically elaborated in Sec. 3 and Sec. 4, respectively, while the relevant preprocessing parts will be involved in both Sec. 3 and Sec. 5.1. All the analysis tasks will be discussed in Sec. 5.

3 GRAPH-BASED AFFECTIVE REPRESENTATIONS

Affective representation is a crucial procedure for most graph-based FAA methods. Depending on the domain that an affective graph models, we categorize the strategy as Spatial graphs, Spatio-temporal graphs, AU-level graphs, and Sample-level graphs. Fig. 5 illustrates a detailed summary of the literature using different graph representations.

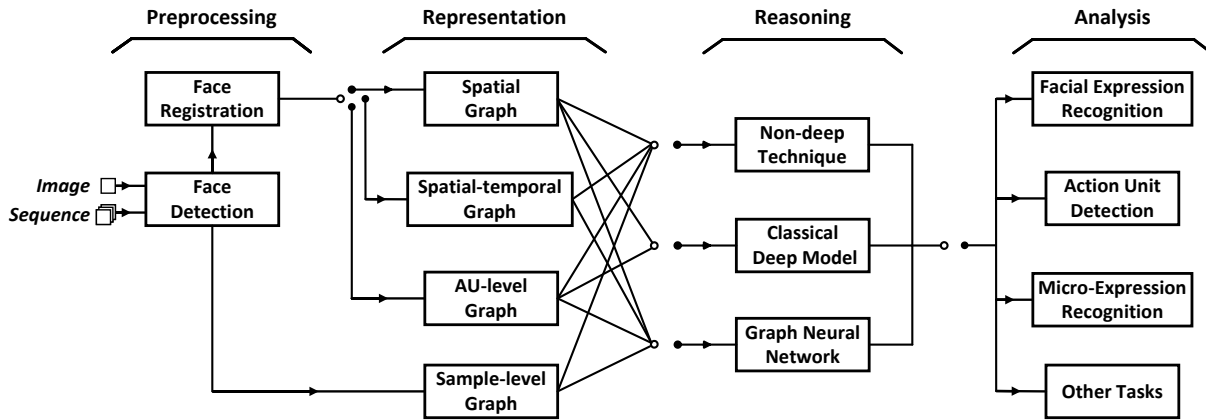


Fig. 3. The pipeline of graph-based facial affect analysis methods.

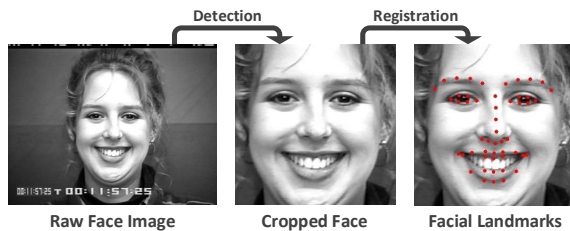


Fig. 4. An illustration of face detection and face registration. The *happy* image is from CK+ database [71].

Note that many graph-based representations contain pre-extracted geometric or/and appearance features. Whether hand-crafted or learned, these feature descriptors are not essentially different from those used in non-graph-based affective representations. Interested readers can refer to [7, 44, 46] for a systematic understanding of this topic.

3.1 Spatial Graph Representations

Non-graph-based spatial methods usually treat a facial affect as a whole representation or pay attention to variations among main face components or crucial facial parts [31, 107, 108]. For spatial affective graphs, facial changes are considered while their co-occurring relationships and affective semantics are represented as essential cues [22, 75, 83]. These approaches can be divided into landmark-level graphs and region-level graphs. Fig. 6 illustrates frameworks of different spatial graph representations.

3.1.1 Landmark-level graphs

Facial landmarks are one of the most critical geometries that reflects the shape of face components and the structure of facial anatomy [109]. Thus, it is natural to use facial landmarks as base nodes to generate a graph representation.

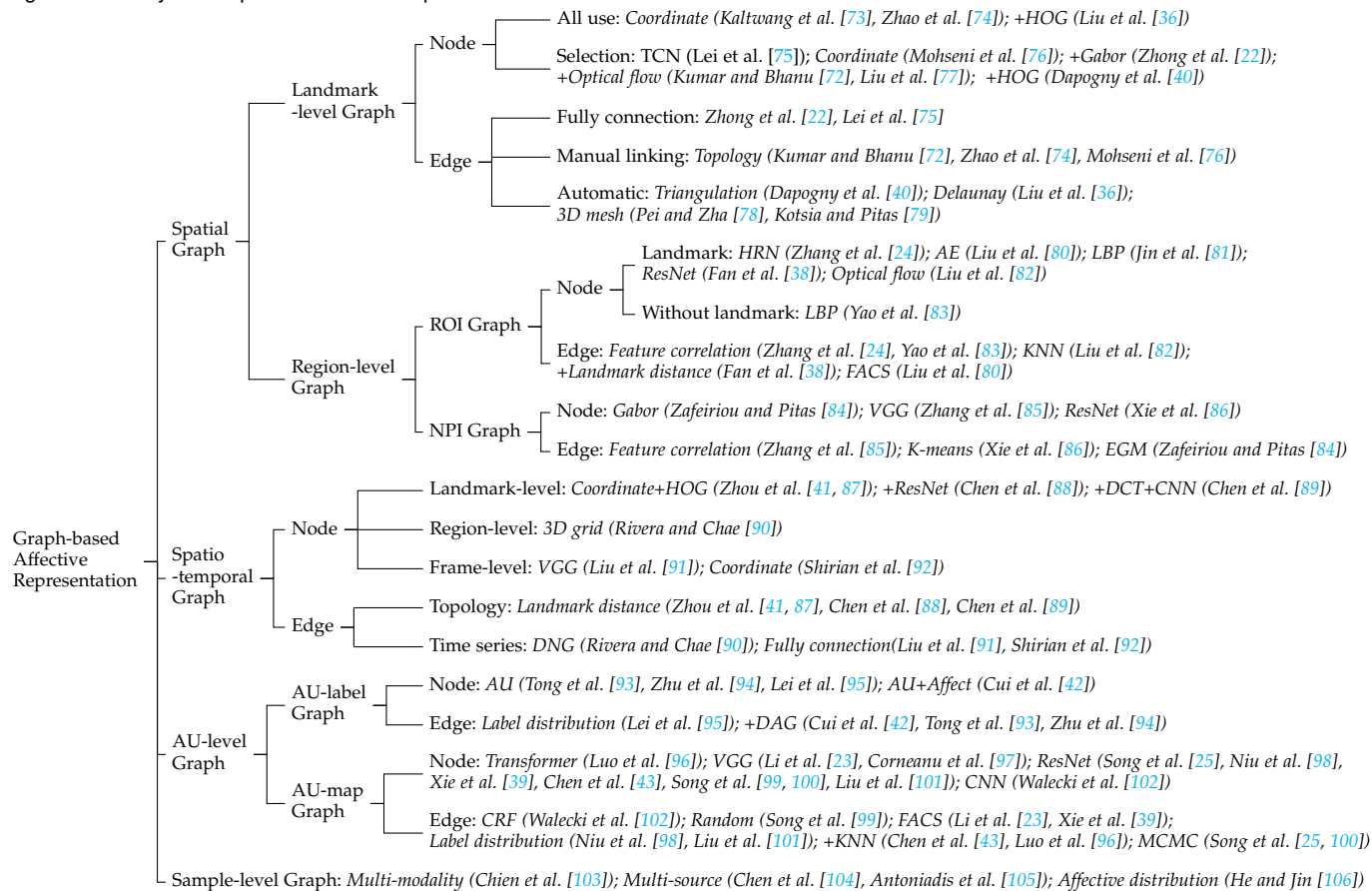
Limited by the detection performance, only a few landmarks that locate basic face components were applied in early graph representations [110]. Recently, graphs using more facial landmarks (e.g., 68 landmarks [111]) are proposed to depict fine-grained facial shapes. For example, in [36] and [74], the authors associated 68 landmarks with the AUs in FACS and made graph-based representations. The difference is that the former additionally employed local appearance features extracted by *Histograms of Oriented Gradients (HOG)* [112] as node attributes; the latter proposed three landmark knowledge encoding strategies for enhanced geometric representations. Alternatively, [73] formulated a *Latent Tree (LT)* where 66 landmarks were set as parts of leaf nodes accompanied by several other leaf

nodes of AU targets and hidden variables, which reflected the joint distribution of targets and features.

Furthermore, some current methods select landmarks with significant contributions to avoid redundant information [75, 113]. Landmarks locating external contour and nose are frequently discarded [40, 76] (see Figs. 6a, b) because they are considered irrelevant to facial affects. [22] chose to remove the landmarks of the facial outline and applied a small window around each remaining landmark as one graph node, while the local features were extracted by *Gabor filter* [114]. Since these local areas were segmented to introduce facial appearance into the graph representation rather than as independent nodes, similar to [36], these methods are still classified in landmark-level graphs. On the other hand, adding extra reasonable landmarks was designed to generate comprehensive graph representations [72, 115], which could keep an appropriate dimension and represent sufficient affective information.

A fully connected graph is the most intuitive way to form edges [22, 75]. However, the number of edges is $n(n-1)/2$ for a complete graph with n nodes, which means the complexity of the spatial relationship will increase as the number of nodes increases. This positive correlation is not helpful because landmarks in a facial component mostly move in concert rather than arbitrarily when conveying facial affects [116]. Studies of point-light displays in emotion perception also show that more complex representations seem to be redundant [117]. To this end, work like [72, 74, 76, 115] manually reduced edges based on muscle anatomy and FACS. Another type of approach is exploiting triangulation algorithms [40], such as the *Delaunay* triangulation [36], to generate graph edges consistent with true facial muscle distribution and uniform for different subjects. Similarly, the landmark-level graph with triangulation is also utilized in generating a sparse or dense facial mesh for 3D FAA [78, 79]. The Euclidean distance is the simplest and most dominant metric for edge attributes of the above facial graphs, even with multiple normalization methods like inner-eyes distance [36, 74]. The *Hop* distance has also been explored as edge attributes to model spatial relationships [41, 87]. Besides, several learning-based edge generation methods (e.g., *LT* [73], *Conditional Random Field (CRF)* [102]) have been proposed to extract semantic information from facial graphs automatically. This part is discussed in detail in Sec. 4.1 and 4.4.

Fig. 5. Taxonomy for Graph-based Facial Representation.



3.1.2 Region-level graphs

Like geometric information, appearance information, especially in local facial regions, can also contribute to FAA [118, 119]. Using graph structures is an excellent choice to encode spatial relationships while representing texture changes in facial components [83, 84]. There are two categories of region-level affective graphs: region of interest (ROI) graphs and non-prior information (NPI) graphs.

ROI graphs partition a set of facial areas as graph nodes related to affective display. Coordinates of facial landmarks are commonly applied to locate and segment ROIs. Unlike a few landmark-level graphs that only use texture near all landmarks as supplementary information, ROI graphs explicitly select meaningful areas as graph nodes, and edges do not entirely depend on established landmark relationships. [24] employed a *High-Resolution Network (HRN)* [120] to regress ROI maps spotted by representative landmarks. Each spatial location in the extracted feature map was considered one graph node, while edges were induced among node pairs according to mappings between ROIs and AUs. Another example in [38] utilized feature maps of landmark-based ROIs outputted by the *ResNet50* [121] as nodes to construct a *K-Nearest-Neighbor (KNN)* graph. For each node, its pair-wise semantic similarities were calculated, and the nodes with the closest *Euclidean* distance were connected as initial edges. Similarly, [82] also employed landmark-based ROIs, but the *KNN* graph was generated in *optical-flow* space to encode the local manifold structure for a sparse representation [77]. Due to chained reactions among multiple AUs and the symmetrical structure of the human

face, [81] proposed a parts-based graph that had manually linked edges by taking FACS and landmarks as references. The nodes were ROIs with *Local Binary Pattern (LBP)* [20] or deep features as attributes. In addition, the method of obtaining ROIs without relying on facial landmarks has also been studied [83] (see Fig. 6c).

NPI graphs usually define a graph structure without introducing external prior knowledge such as landmarks and FACS. Nodes in NPI graphs are generally facial regions uniformly distributed over the raw image or generated in a fully automatic manner. For example, [84] created a reference bunch graph by evenly overlaying a rectangular graph on object images (see Fig. 6d). Alternatively, [86] built two NPI graphs for cross-domain FAA, where local-to-global, global-to-local, and local-to-local edges were computed according to statistical feature distribution acquired by the *K-means* algorithm. Recent studies have also tried to introduce regions beyond facial parts or single-face images as context nodes. [85] exploited the *Region Proposal Network (RPN)* [122] with *VGG16* [123] to extract regions-level nodes, including the target face and its contexts, while edges were affective relationships calculated based on feature vectors.

3.2 Spatio-Temporal Graph Representations

Spatio-temporal representations deal with a sequence of frames within a temporal window and describe the dynamic evolution of facial variations [124]. In particular, introducing temporal information allows nodes to interact with each other at different times and generates a more complex affective graph. Fig. 7 presents frameworks of various spatio-temporal graph representations.

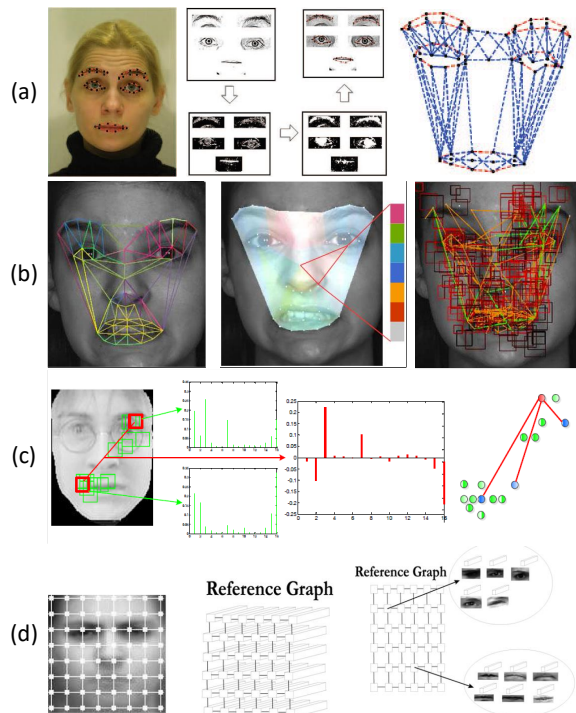


Fig. 6. Spatial graphs. (a) Landmark-level graph with FACS-based edges [76]; (b) Landmark-level graph with automatic triangle edges [40]; (c) ROI graph based on correlation without landmarks [83]; (d) NPI graph with individual nodes [84]. Zoom in for better view.

Extend spatial graphs to the spatio-temporal domain is currently the main route. [90] exploited weighted compass masks to obtain 2D directional number responses and 3D space-time directional edge responses corresponding to each of the symmetry planes of a cube. The two masks of given local neighborhoods were nodes in a spatio-temporal *Directional Number Transitional Graph (DNG)*, which could represent salient facial changes and statistic frequency of affective behaviors over time (see Fig. 7a).

Several representations have been proposed to define temporal connections between landmarks, which can be seen as landmark-level spatio-temporal graphs. [89] developed a context-aware facial multi-graph where intra-face edges were initialized based on morphological and muscular relationships, and inter-frame edges were created by linking the same node between consecutive frames. Similar landmark-based edge initialization in the temporal domain was also utilized in [87, 88]. In [41], the authors introduced a connectivity inference block that could automatically generate dynamic edges for a spatio-temporal situational graph of part-occluded affective faces (see Fig. 7b).

Unlike landmark-level graphs, [91] first extracted a holistic feature of each frame and set them as individual nodes to establish a fully connected graph (see Fig. 7c), which could be seen as a frame-level spatio-temporal graph. Similar work includes [92] that took *Discrete Cosine Transform (DCT)* features as node attributes. Edge connections of these methods would be established by learning the long-term dependency of nodes in time series (discussed in Sec. 4).

3.3 AU-level Graph Representations

Apart from using knowledge of AUs and FACS in the above two types of affective graphs, many graph-based representations have been proposed to model affective information

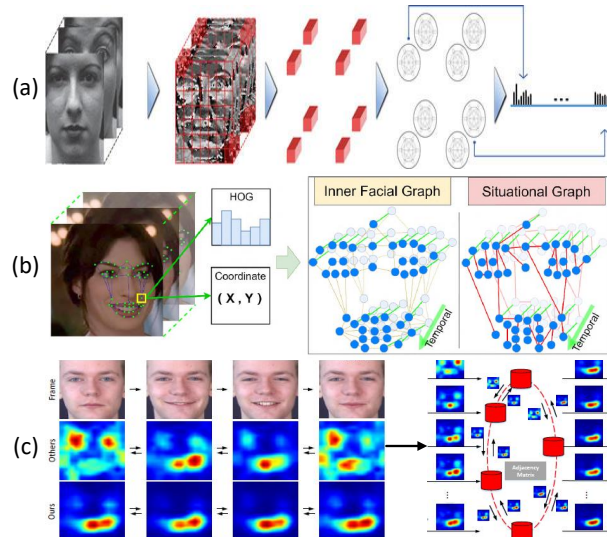


Fig. 7. Spatio-temporal graphs. (a) Region-level graph with edges based on transitional masks [90]; (b) Landmark-level graph with adaptive edges [41]; (c) Frame-level graph [91]. Zoom in for better view.

from the perspective of AUs themselves. We divide these approaches into two categories: AU-label graph and AU-map graph. Fig. 8 shows frameworks of different AU-level graph representations.

3.3.1 AU-label graphs

Unlike spatial and spatio-temporal graphs, AU-label graphs were built from the label distribution of training data [37, 94]. [93] computed the co-occurrence and co-absence dependency between every AU pair from the existing database (see Fig. 8a). Since the dependency is not always symmetric, these AU label relationships were used as edges to construct a *Directed Acyclic Graph (DAG)*. In [95], an AU-label graph was built with a data-driven asymmetrical adjacency matrix that denoted the conditional probability of co-occurring AU pairs. AU labels were transformed into high-dimensional node vectors as node attributes [125]. On the other hand, [42] established a *DAG* where object-level labels (affect categories) and property-level labels (AUs) were regarded as parent nodes and child nodes, respectively. The conditional probability distribution of each node to its parents was measured to obtain graph edges for correcting existing labels and generating unknown labels. A similar idea was achieved in [43] to boost affective feature learning in large-scale FAA databases (see Fig. 8b).

3.3.2 AU-map graphs

AU-map graphs are intuitively close to region-level spatial graphs, especially ROI graphs, because they both employ local feature maps as graph nodes. [23] is an example in between. Twelve AUs features were learned through landmark-based ROI features cropped from a multi-scale global appearance feature [123]. These AU features and the AU relationships gathered from training data and manually pre-defined edge connections [126] were combined to construct a knowledge graph (see Fig. 8c). However, the significant difference is that AUs define a set of facial muscle actions, which means there might be multiple AUs in the same ROI. Like in Fig. 2, AU12 and AU15 co-occur at lip corners but refer to 'puller' and 'depressor', respectively. Therefore, for many AU graphs, their definition of nodes

is independent of those in ROI graphs, even though they are similar in feature map extraction. For instance, graph nodes in [39] were AU features directly obtained by *ResNet* without defining ROIs. The homologous protocol was also conducted in [100].

Some special AU-map graphs have been proposed to introduce structure learning for more complex FAA tasks. For AU intensity estimation, [102] trained a *Convolutional Neural Network (CNN)* to learn deep AU features from multiple databases jointly. The *copula functions* [127] were applied to model pair-wise AU dependencies in a *CRF* graph. In addition, *Bayesian networks (BNs)* are also used to capture the AU inherent dependencies for this task [25, 100]. To account for indistinguishable affective faces, [97] designed a *VGG-like patch prediction module* plus a fusion module to predict the probability of each AU. A prior knowledge taken from the given databases and a mutual gating strategy were used simultaneously to generate initial edge connections. To model uncertainty samples in real-world databases, [99] established an uncertain graph, in which a weighted probabilistic mask that followed *Gaussian* distribution was imposed on each AU feature map. By doing this, the importance of edges and the underlying uncertain information could be encoded in the graph representation. Another attempt in [98] boosted semi-supervised AU recognition for labeled and unlabeled face images. The parameters of two AU classifiers were used as graph nodes to share the latent relationships among AUs.

3.4 Sample-level Graph Representations

Recently, several graph representations beyond a single sample have been proposed, which indicates that this is still an open research field. In [106], a correlation graph with word-embedded affective labels as nodes was built for distribution learning. Its edges could be generated either by psychologically normalized *Gaussian* function or conditional probabilities. To combine signals from multiple corpora, [103] proposed a dual-branch framework, in which the visual semantic features were extracted in source and target sets. These features were then retrieved with correlation coefficients to generate positive edge connections for a learnable visual semantic graph (see Fig. 8d). Besides, [104] constructed a *KNN* graph with edges of binary weights to preserve the intrinsic geometrical structure of source and target data, which can seek more latent common information to reduce the distribution difference and make representations more discriminative.

3.5 Discussion

As a significant part of the graph-based FAA method, different affective graph representations have their merits, drawbacks, requirements, and time burdens. (see Table 1).

Spatial graph representations: Conceptually, landmark-level graphs model the facial shape variations of fiducial points and easily generate the internal structural relationships of different affective displays. However, most methods are sensitive to facial landmarks' detection errors, thereby failing in uncontrolled conditions. On the other hand, the selection of landmarks and the connection of edges have not yet formed a standard rule. Their effects on the graph representation are rarely reported, even though some FACS-based strategies have been designed. Region-level graphs

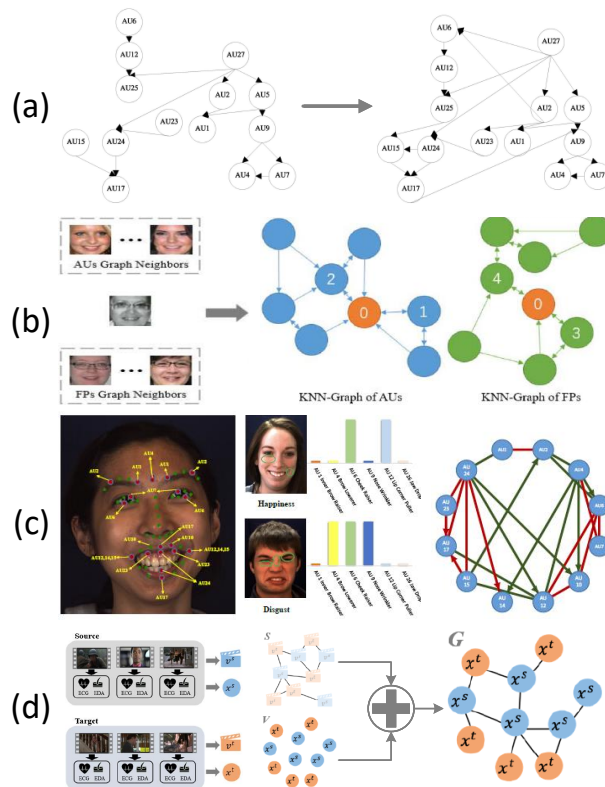


Fig. 8. AU-level and Sample-level graph representations. (a) AU-label graph with edges generated from training data [93]; (b) Auxiliary graphs of AUs and landmarks [43]; (c) AU-map graph with FACS based edges [23]; (d) Sample-level multi-modal graph of visual and physiological signals [103]. Zoom in for better view.

explicitly regard an affective face as multiple local crucial facial areas compared with landmark-level graphs. The spatial relationships among selected regions are measured through feature similarity instead of manual initialization based on facial geometry. The circumstance resulting from inaccurate or unreasonable landmarks will also impact related ROI graphs. Since most NPI graphs utilize a region searching strategy, the problem is how to avoid the loss of target face and how to exclude invalid regions.

Spatio-temporal graph representations: With extra dynamic affective information, spatio-temporal graphs can help aggregate evolution features in continuous time. For landmark-level methods, the current initialization strategy of edges is to link the facial landmark with the same index frame by frame. Unfortunately, no research has been reported to learn the interaction of landmarks with different indexes in the temporal dimension. Besides, in addition to *Euclidean* distance and *Hop* distance, other edge attributes measurement methods should also be explored to model the semantic context both spatially and temporally. For the frame-level methods, embedding domain knowledge related to affective behaviours like the muscular activity by graph structure is not explicitly considered in recent work. Therefore, building a hybrid spatio-temporal graph is a practical way to simultaneously encode the two levels of affective information.

AU-level graph representations: As a distinctive type, AU-level graphs provide certain semantics of facial affects by representing each AU and its co-occurrence dependency. The measurement criteria of AU correlations are versatile

TABLE 1
An Overview of Affective Graph Representations

Category	Branch	Strength	Limitation	Demand	Time
Spatial	Landmark-level	Effective facial geometry embedding; Flexible structural relationships	Sensitive to the landmark detection accuracy	High-quality face registration	Low-Mid
	Region-level	Versatile local texture extraction; Underlying correlation beyond locations	Landmark sensitive for related ROI graphs; Redundant or missing regions for NPI graphs	Suitable for various situations	Mid-High
Spatio-Temporal		Extra dynamic evolution information	Relatively fixed edges in the time domain	Video/Sequence input	Low-High
AU-level	AU-label	Meaningful semantic dependencies;	Cannot be an end-to-end framework	Reliable & sufficient AU annotations	Low
	AU-map	Explicit prior knowledge introduction	Unstable co-occurring distributions		Mid-High
Sample-level		Modular to existing architectures; Cross-corpus information	Lack of in-face modelling	Large-scale/Multiple databases	Low-High

but not general. Most AU-label graphs rely on the label distributions of one or multiple given databases. Nevertheless, AU labelling requires annotators with professional certificates and is a time-consuming task that causes existing databases with AU annotations to be usually small-scale. Therefore, the distribution from limited samples may not reflect the true dependencies of individual AUs, and its impact on FAA still needs to be assessed.

Sample-level graph representations: Sample-level graphs are an appealing field that introduces latent relationships in data distributions. Such characteristic makes it convenient to integrate with existing FAA methods. However, it also puts forward higher requirements for the diversity and balance of samples. On the other hand, to the best of our knowledge, there is no work combining sample-level and other in-face graphs to construct a joint representation, which we think is a good topic.

Computational complexity: The time complexity of building a graph representation depends on its node attributes and edge initialization. Landmark-level graphs require less computation, no matter for spatial or spatio-temporal graphs. Graphs involving pre-extracted features like region-level and AU-map graphs need additional computation, the degree of increase varies from manual to deep methods. AU-label graphs are the most efficient branch because they prefer a unified view of the distribution. Since sample-level graphs usually consider multiple data sources, extra burdens might be added according to specific situations.

4 AFFECTIVE GRAPH RELATIONAL REASONING

Generally, graph relational reasoning can be considered a two-step process, i.e., understanding the structure from a certain group of entities and making inferences of the system as a whole or the property within [128]. However, things are slightly different in the case of graph-based FAA. Depending on what kind of affective graph representation is exploited, the contribution of graph relational reasoning can be either merged before the decision level with other affective features or reflected in a collaborative way in the level of feature learning.

In this Section, we review relational reasoning methods designed for affective graph representations in four categories: *Dynamic BNs (DBNs)*, classical deep models, *Graph Neural Networks (GNNs)* and non-deep machine learning techniques.

4.1 Dynamic Bayesian Networks

DBNs are often used to reason about relationships among facial displays like AUs [129] and, of course, for AU-label

graph representations. The *BN* is a *DAG* that reflects a joint probability distribution among a set of variables. In the work of [37, 93], a *DAG* was manually initialized according to prior knowledge, and then large databases were used to perform structure learning to find the optimal probability graph structure. After that, the probabilities of different AUs were inferred by learning the *DBN*. Following this idea, [94] additionally integrated *DBN* to a multi-task feature learning framework and made the AU inference by calculating the joint probability of each category node. Sometimes *DBN* is also combined with some statistical methods to explore different graph structures [25, 100], such as *Hidden Markov Models* [130]. Another advanced research of *DBN* is [42] that modeled the inherent relationships between category labels and property labels. Its parameters were utilized to denote the conditional probability distribution of each AU given the facial affect. The wrong labels could be corrected by leveraging the dependencies after the structure optimization.

4.2 Adjustments of Classical Deep Models

Before *GNNs* are widely employed, many studies have adopted conventional *Deep Neural Networks (DNNs)* to process affective representations with the graph structure. These deep models are not explicitly designed but can conduct standard operations on structural graph data by adjusting the internal architecture or applying an additional transformation to the input graph representation. Fig. 9 shows examples of classical deep models for graph relational reasoning.

4.2.1 Recurrent neural networks

The *Recurrent Neural Networks (RNNs)* variant is one of the successfully extended model types for handling graph structural inputs. Similar to random walk, [22] applied a *Bidirectional RNN* to deal with its landmark-level spatial graph representation in a rigid order. The Gabor features of each graph node were updated by multiplying with the average of the connected edges to incorporate the structural information. Subsequently, the nodes were iterated by the *RNN* with learnable parameters in forwarding and the backward direction (see Fig. 9a). In [97], the authors built a structure inference module to capture AU relationships from an AU-map graph representation. Based on a collection of interconnected recurrent structure inference units and a parameter sharing *RNN*, the mutual relationship between two nodes could be updated by replicating an iterative message passing mechanism with the control of a gating strategy. Following the sequential idea of *RNNs*, [23] exploited a *Gated Graph Neural Network (GGNN)* [131] that calculated

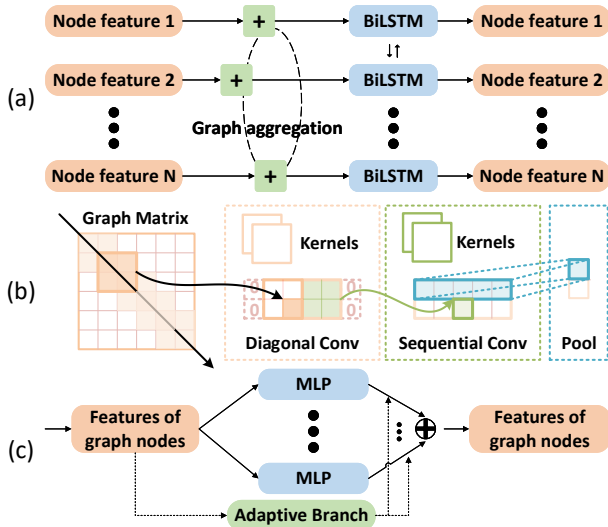


Fig. 9. Classical deep models for graph relational reasoning. (a) RNN [22]; (b) CNN [36]; (c) MLP [100]. Zoom in for better view.

the hidden state of the next time step by jointly considering the current hidden state of each node and adjacent nodes. The relational reasoning could be done through the iterative update of GGNN over its AU-map graph.

4.2.2 Convolutional neural networks

Unlike the sequential networks, [36] utilized a variant CNN to process the landmark-level spatial affective graph. Compared to standard convolution architectures, the convolution layer in this study convolved over the diagonal of a particular adjacency matrix to aggregate the information from multiple nodes. Then a list of the diagonal convolution outputs was further processed by three 1D sequential convolution layers. The corresponding pooling processes were performed behind convolution operations to integrate feature sets (see Fig. 9b). Another attempt for landmark-level spatial graph representations is the *Graph Temporal Convolutional Networks (Graph-TCN)* [75]. It followed the idea of TCNs that consisted of residual convolution, dilated causal convolution, and weight normalization [132]. By using different dilation factors, TCNs were applied to convolve the elements inside one node sequence and from multiple node sequences. Thus, the TCN for a node and TCN for an edge could be trained respectively to extract node features and edge features simultaneously. Besides, [38] exploited a Semantic Correspondence Convolution module to model the correlation among its region-level spatial graph. Based on the assumption that the channels of co-occurring AUs might be activated simultaneously, the *Dynamic Graph CNN (DG-CNN)* [133] was applied on the edges of the constructed KNN graph to connect feature maps sharing similar visual patterns. After the aggregation function, affective features were obtained to estimate AU intensities.

4.2.3 Multilayer perceptron networks

As a vanilla architecture, *Multilayer Perceptrons (MLPs)* have also been explored. [40] employed a hierarchical *Auto-Encoder (AE)* based on MLPs to capture relationships from a landmark-level spatial graph. It accumulated HOG features of multiple nodes whose appearance changes were closely related and computed the confidence scores as the triangle-wise weights over edges. After that, a *Random Forest (RF)*

was used for facial affect classification and AU detection simultaneously. In [100], a hybrid graph network composed of dynamic MLPs performed multiple types of message passing, which provided more complementary information for reasoning the positive and negative dependencies among AU nodes. An adaptive branch was used to generate weights for different graph structures (see Fig. 9c).

4.3 Graph Neural Networks

GNNs are proposed to extend the 'depth' from 2D image to graph structure and establish an end-to-end learning framework instead of additional architecture adjustment or data transformation [134]. Unlike conventional deep models that are stacked by layers of $H^{l+1} = f(H^l)$, where H^l denotes the hidden state of the l -th layer, f is the nonlinear function, GNNs formulate layers as $H^{l+1} = f(H^l, A)$, where the adjacency matrices A (records all the edges in a graph) is explicitly fed for the relational reasoning. Therefore, GNNs can infer comprehensive graph structures through A for better feature extraction, including effective node updates and flexible edge connections. Fig. 10 illustrates several GNN architectures for affective graph relational reasoning.

4.3.1 Graph convolutional networks

Graph Convolutional Networks (GCNs), especially the spatial GCN [135], are the most popular GNN in graph-based FAA research. Practically, GCNs can be set as an auxiliary module [74, 95, 105] or part of the collaborative feature learning framework [25, 96, 101].

For the auxiliary module, GCNs are applied immediately after the graph representation. However, the outputs of relational reasoning are not directly used for facial affect classification or AU detection but are later combined with other deep features as a weighting factor (see Fig. 10a). [98] employed a two-layer GCN for message passing among different nodes in its AU-level graph. Both the dependency of positive and negative samples were considered and used to infer a link condition between any two nodes. The output of GCN was formulated as a weight matrix of the pre-trained AU classifiers. Besides, GCNs can also be utilized following the above manner to execute relational reasoning on atypical graph representations, such as multi-target graph [85], distribution graph [106], and cross-domain graph [86].

For the collaborative framework, GCNs usually inherit the previous node feature learning model progressively (see Fig. 10b). Like in [80], a GCN-based multi-label encoder was proposed to update features of each node over a region-level spatial graph representation. The reasoning process was the same as that in the auxiliary framework. Similar studies also include [24] and [103]. In addition, to incorporate the dynamic in spatio-temporal graphs, [91] set GCNs as an imitation of attention mechanism or weighting mechanism to share the most contributing features to explore the dependencies among frames. After training, the structure helped nodes update features based on messages from the peak frame and emphasize the concerned facial region. A more feasible way is to apply *Spatial Temporal GCN (STGCN)* [136] on spatio-temporal graphs [41, 87, 88, 89] (see Fig. 10c). In their relational reasoning, features of each node were generated with its neighbor nodes in the current frame and consecutive frames by using spatial graph convolution and temporal convolution, respectively.

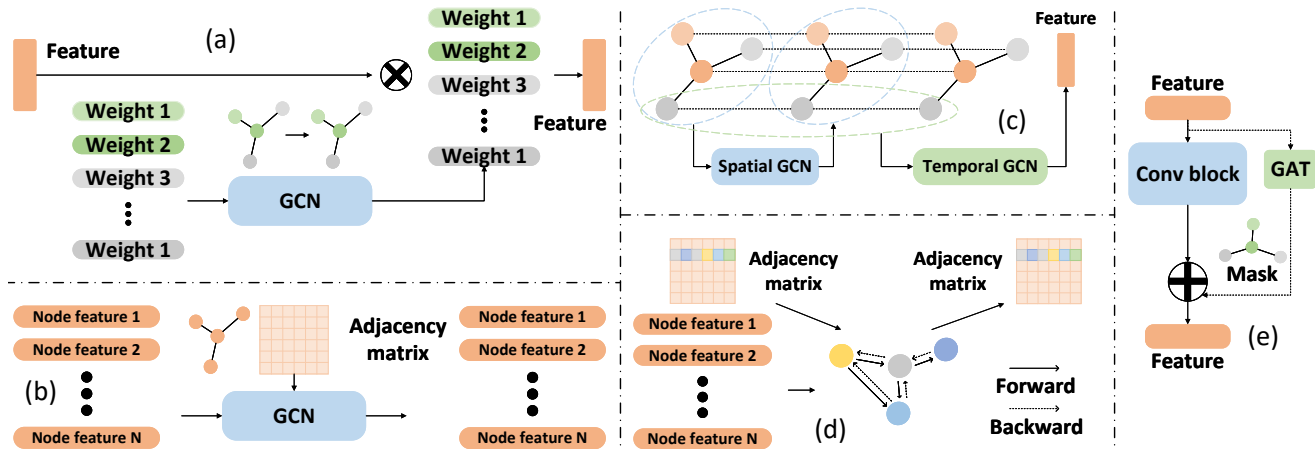


Fig. 10. GNNs for graph relational reasoning. (a) GCN as an auxiliary module [98]; (b) GCN as a collaborative framework [25]; (c) STGCN [89] (d) Spectral GCN [81]; (e) GAT [89]. Zoom in for better view.

Alternatively, the approach of spectral GCN [137] has also been studied [113]. [81] devised a lightweight GCN following the *Message Passing Neural Network* [138]. A learnable adjacency matrix was adapted to infer the spatial dependencies of ROI nodes in different facial affects. [92] extended in *Inception* idea from standard CNNs to spectral GCNs that captured emotion dynamics at multiple temporal scales. The yielded embeddings of different dimensions were jointly learned over a classification loss and a graph learning loss for the optimal graph structure.

4.3.2 Graph attention networks

Graph Attention Networks (GATs) aim to strengthen the node connections with high contribution and offer a more flexible way to process the graph structure [139]. [99] introduced an uncertain GNN with GAT as the backbone. The goal is to select valuable edges, depress noisy edges, and learn AU dependencies on its AU-map graph. In addition, the underlying uncertainties were considered in a probabilistic way, close to the idea of *Bayesian* methods in GNN [140], to alleviate the data imbalance by weighting the loss function. On the other hand, GAT collaboratively worked with GCN in [72] to deal with two-stream graph inputs. Compared to applying GAT directly, [39] proposed a GNN that added a self-attention graph pooling layer after three sequential GCN layers. A similar block was done in [115] which revised the GCN block with channel and node attention. It improved the reasoning process on graph representations because only important nodes would be aggregated, including affective information and facial topology. To make nodes interact more dynamically instead of using a constant graph structure, [89] applied a set of learnable edge attention masks to the STGCN for subtle adjustments of the defined spatio-temporal graph representation (see Fig. 10e).

4.4 Non-deep Machine Learning Methods

Although refining deep features extracted by parameterized neural networks and gradient-based methods is the mainstream, they require numerous training samples for effective learning. Due to the insufficient data in the early years or the purpose of efficient computation, many non-deep machine learning techniques have been applied for affective graph relational reasoning. Graph structure learning is one of the widely used approaches. In [73], the reasoning of its spatial

graph representation was conducted by *LT* learning. Parameters update and graph-edit of *LT* structure were performed iteratively to maximize the marginal *log*-likelihood of a set of training data. [102] employed *CRF* to infer AU dependencies in an AU-map graph. The use of *copula* functions allowed it to model non-linear dependencies among nodes easily. At the same time, an iterative balanced batch learning strategy was introduced to optimize the most representative graph structure by updating each set of parameters with batches. Approaches of graph feature selection are also exploited in this part, such as *Graph Sparse Coding (GSC)* [82, 104] and *Elastic Graph Matching (EGM)* [84]. These methods have provided a more diverse concept for graph relational reasoning.

4.5 Discussion

Although all the methods above can achieve affective graph relational reasoning, the choice has a causal relationship with the type of graph representation (see Table 2).

TABLE 2
Causal Relationships between Graphs and Reasoning methods

Category	Spatial	Spatio-Temporal	AU-level	Sample-level
DBNs			✓	
DNNs	✓	✓	✓	
GNNs	✓	✓	✓	
Non-deep	✓	✓	✓	✓

Dynamic Bayesian network: Nearly half of AU-label graph representations employ *DBNs* as their relational reasoning model. However, the representation quality highly relies on the available training data that need balanced label distribution in positive-negative samples and categories. This strong assumption will limit the effectiveness of node dependencies learned by *DBNs*. Another problem is that *DBNs* can only be combined with facial features as a relatively independent module and are hard to integrate into an end-to-end learning framework.

Classical deep model: Standard deep models, including *CNNs*, *RNNs*, and *MLPs*, have been explored to conduct graph relational reasoning before the emergence of *GNNs*. Even if they are suitable for more graph representations than *DBNs*, these grid models focus more on local features. The additional adjustments in input format or/and network architecture cause losses of node information or let node messages only pass and update in a specific sequence,

which suppresses the global property represented by the graph. Thus, we think the specifically designed networks like *GNNs* will become dominant in this part.

Graph neural network: *GNNs* are developing techniques that make full advantage of graphs. Architectures with different focuses have been proposed but have their flaws as well. For instance, *GCNs* cannot handle directed edges well (e.g., AU-level graphs), while *GATs* only use the node links without considering edge attributes (e.g., spatial graphs). Besides, due to the low dimension of the nodes in affective graphs, too deep *GNNs* may be counterproductive. In addition, being an auxiliary block or part of the whole framework will influence the construction of *GNNs*. Therefore, managing graph representation and relational reasoning using *GNNs* still need to be explored.

Non-deep methods: Non-deep machine learning has a place in early studies and is even applied in recent work because no training is required. They partly inspire advanced techniques like *DBNs* and *GNNs*. Nevertheless, one of the reasons they have been replaced is that these approaches need to be designed separately to cope with different graph representations, similar to hand-crafted feature extraction. Hence, it is not easy to form a general framework. On the other hand, more training data and richer computing resources allow deep models to perform more effective and higher-level relational reasoning on affective graphs.

Computational complexity: Obviously, classical deep models like *CNNs*, *RNNs*, and *MLPs* are more time-consuming than the non-deep methods such as *GSC* and *EGM*. For *GNNs* including *GCNs* and *GATs*, existing methods typically add a limited number of layers due to relatively small graph dimensions and potential overfitting issues. Thus, their computational burden is not significant compared to the overall framework, as has been confirmed by experiments in a few related studies [81, 100].

5 APPLICATIONS AND PERFORMANCE

According to different description models of facial affects, the FAA can be subdivided into multiple applications. The typical output of FAA systems is the label of a basic facial affect or AUs. Recent research also extends the goal to predict micro-expression or affective intensity labels or continuous affects. This section compares and discusses graph-based FAA methods from four main application categories: facial expression recognition, AU detection, micro-expression recognition, and a few special applications. Due to page limitation, we select the most relevant and representative papers following these standards: published in more well-known forums in the past five years; or belonging to distinct branches of graph representation and reasoning for diversity consideration.

5.1 Databases

Most FAA studies apply public databases of facial affect as validation material. A comprehensive overview is presented in Table 3. The characteristics of these databases are listed from four aspects: samples, attributes, graph-related properties, and certain contents. Fig. 11 exhibits several examples of facial affects under different conditions. In addition, for better interpreting the graph-based FAA, we summarize corresponding elements (e.g., landmark coordinates, AU

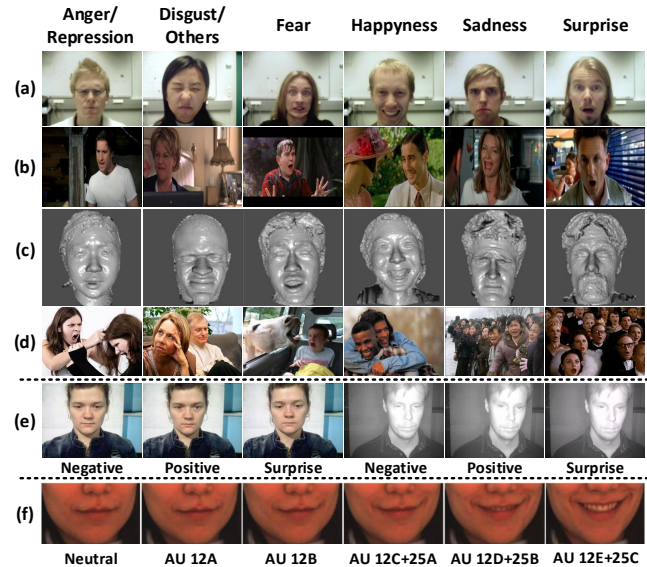


Fig. 11. Facial affect databases. (a) Oulu-CASIA contains posed facial affects; (b) SFEW 2.0 has facial affects under in-the-wild scenarios; (c) BP4D provides 3D affective face images; (d) EMOTIC, multiple faces appear per image with VAD annotations; (e) The SMIC collects images of spontaneous micro facial affects in visual light and near infrared light; (f) DISFA offers frame-level AU intensity labels.

labels) self-carried by databases, which are rarely considered in previous related surveys.

Databases containing posed facial affects, including Extended Cohn-Kanade Dataset (CK+) [71, 141], M&M Initiative Facial Expression Database (MMI) [142], and Oulu-CASIA NIR&VIS Facial Expression Database (Oulu-CASIA) [143], are chosen by early FAA methods. More challenging databases, such as FER-2013 [144], Static Facial Expression in the Wild (SFEW) 2.0 [145], and Acted Facial Expression in the Wild (AFEW) 7.0 [146], tend to acquire spontaneous affective data from complex and wild environments.

Some databases also contain intensity labels of facial affects and even AUs, e.g., Denver Intensity of Spontaneous Facial Action Database (DISFA) [147], Binghamton University 3D/4D Facial Expression Database (BU-3DFE/4DFE) [148, 149] and Binghamton-Pittsburgh 3D Dynamic Spontaneous Facial Expression Database (BP4D) [150].

Another type of database is for micro-expressions. Participants are required to keep a neutral face while watching videos associated with induction of specific affects [151]. Following this setting, Spontaneous Micro Facial Expression Database (SMIC) [152], Improved Chinese Academy of Sciences Micro-Expression Database (CASME II) [153], Spontaneous Micro-Facial Movement Database (SAMM) [154], Chinese Academy of Sciences Macro-Expression and Micro-Expression Database (CAS(ME)²) [155] have been released. However, it is hard to collect and annotate large-scale micro-expression data with uncontrolled scenarios due to its subtle, rapid, and involuntary nature.

Recently, large-scale databases have been developed to provide massive data with spontaneous facial affects and in-the-wild conditions, such as Real-World Affective Face Database (RAF-DB) [156], Large-Scale Face Expression in-the-Wild dataset (ExpW) [10], EMOTIC [157], AffectNet [158], and EmotioNet [159]. Besides, Aff-Wild2 [160] is the largest database with continuous and AU labels.

Concerning graph-based FAA, it is available to find and

TABLE 3
An Overview of Facial Affect Databases

Database 'year	Samples			Attributes			Graph-based Properties ³			Special Contents ⁴
	Data Type	Subjects	Number	Eli. & Sou. ¹	Affects ²	B.B. ¹	LM	AU	Dynamic	
CK(+) '10	Sequences	97(123)	486(593)	P & Lab	6B+N(+C)	●	●	● + I	●	-
MMI '10	Images/Videos	75	740/2900	P & Lab	6B+N	○	○	●	● + D	Head pose
Oulu-CASIA '11	Sequences	80	2880	P & Lab	6B	●	○	○	●	NIR
DISFA '13	Sequences	27	130,000	S & Lab	6B+N	●	●	● + I	● + F	-
FER-2013 '13	Images	-	35887	S & Web	6B+N	●	○	○	○	Wild
SFEW 2.0 '15	Images	-	1766	S & Movie	6B+N	●	●	○	○	Wild
AFEW 7.0 '17	Videos	-	1809	S & Movie	6B+N	●	●	○	●	Audio, Wild
BU-3DFE '06	Images	100	2500	P & Lab	6B+N	●	●	○	○	3D, Multi-view, I
BU-4DFE '08	Videos	101	606	P & Lab	6B+N	●	●	● + I	●	3D, Multi-view
BP4D '14	Videos	41	328	S & Lab	6B+E+P	●	●	● + I	● + F	3D, Head pose
SMIC '13	Sequences	16	164	S & Lab	3B [‡] +N	●	○	○	●	Micro., NIR
CASME II '14	Sequences	35	247	S & Lab	3B [‡] +R+O	●	○	●	● + D	Micro.
SAMM '18	Sequences	32	159	S & Lab	6B+C	●	○	●	● + D	Micro.
CAS(ME) ² '18	Sequences	22	300+57	S & Lab	3B [‡] +O	●	○	●	● + D	Macro. & Micro.
EmotioNet '16	Images	-	950,000	S & Web	6B+17Comp.	●	●	● + I	○	Wild
ExpW '18	Images	-	91,793	S & Web	6B+N	●	○	○	○	Multi-sub., Wild
RAF-DB '19	Images	-	29672	S & Web	6B+N+11Comp.	●	●	○	○	Wild
AffectNet '19	Images	-	420,299	S & Web	6B+N+C+O	●	●	○	○	V&A, Wild
EMOTIC '19	Images	-	23,571	S & Web	6B+N+19Comp.	●	○	○	○	V&A, Multi-sub., Wild
Aff-Wild2 '19	Images/Videos	-	564/2,800,000	S & Web	6B+N+O	●	○	●	●	Audio, V&A, Wild

¹ Eli.: elicitation; Sou.: source; P: posed; S: spontaneous; B.B.: bounding boxes; LM: landmarks; ● = Yes, ○ = No.

² 6B: six basic affects; N: neutral; C: contempt; E: embarrassment; P: pain; O: others; R: repression; 3B[‡]: three basic affects (positive, negative, surprise); 3B[‡]: three basic affects (happiness, disgust, surprise); Comp.: compound affects.

³ I: intensity annotation; D: onset-apex-offset annotation; F: frame-level annotation.

⁴ NIR: near-infrared; Multi-sub.: multiple subjects per image; Micro.: micro-expression; Macro.: macro-expression; Wild: in-the-wild; V&A: valence and arousal.

select suitable databases with corresponding metadata, such as landmarks, AU labels, and dynamics, for different graph representation purposes. However, existing databases also have some shortcomings. On the one hand, not enough AU intensity annotations are provided by in-the-wild databases, decreasing AUs' role in FAA. On the other hand, there is few large-scale dynamic affective database so that limits temporal information in generating affective graph representations. Finally, databases about natural and spontaneous facial affects in a continuous domain need more attention instead of discrete categories.

5.2 Facial Expression Recognition

Facial expression recognition (FER), or macro-expression recognition, has been working on basic facial affects classification. An inevitable trend of FER is that the research focus has shifted from the early posed facial affects in controlled conditions to the recent spontaneous facial affects in real scenarios. In other words, existing methods, including graph-based FER, can achieve excellent FER under lab-controlled scenarios, which can be corroborated from the results in Table 4. For example, the performance on the CK+ database is very close to 100% [79, 90, 91, 115].

From the view of the representation, spatial graphs and spatio-temporal graphs are dominant. Specifically, hand-crafted features (e.g., *LBP* [81, 83], *Gabor* [22, 115], *HOG* [36, 87, 104]) or deep-based features (e.g., *CNN* [74, 115], *VGG* [91], *ResNet* [39]) are employed to enhance the node representation similar to many non-graph FER methods [20, 31]. For reasoning approaches, early studies prefer to capture the relations of an individual node from predefined graph structures using tracking strategies (e.g., displacement projection [76] and *DNG* [90]) or general machine learning models (e.g., *RF* [40], *RNN* [22], *CNN* [36]). In the latest work, *GCNs* become one of the mainstream choices in the latest work and show state-of-the-art performances on posed and in-the-wild databases [39, 74, 81, 101, 105, 113, 115]. Another

observation is that the framework of combining the spatio-temporal graph representation and *GNNs* is getting more attention in FER studies [41, 87, 91, 92].

Although many graph-based studies have shown improvements in predicting facial affects, FER still has some potential topics. One thing is that the goal of existing methods stays on classifying basic facial affects. No study of graph-based methods to recognize compound affects (or mixture affects), whose labels are provided by recent databases like RAF-DB and EmotioNet, is reported. One possible solution is introducing AU-level graph representations that can describe fine-grained macro-expressions with closer inter-class distances. The other topic is practical graph-based representations due to the big gap between the performance of current methods and the acceptable result in practice when analyzing in-the-wild facial affects. In addition, since existing databases lack sufficient dynamic annotated samples, the evaluation of spatio-temporal graphs in large-scale conditions remains to be explored.

5.3 Action Unit Detection

The AU detection (AUD) facilitates a comprehensive analysis of the facial affect and is typically formulated as a multi-task problem that learns a two-class classification model for each AU. It can expand the recognition categories of macro-expressions through the AU combination [73] and can be used as a pre-step to enhance the recognition of micro-expressions [95]. Compared with graph-based FER, the wide usage of graph structures has a long history in AUD [34] and has played a more dominant role. Table 5 summarizes graph-based AUD methods including the performance comparison.

Specifically, spatial graphs and AU-level graphs are equally popular in the representation part of AUD. Interestingly, no matter landmark-level or region-level, all the spatial graphs constructed in the listed AUD methods employed facial landmarks [24, 36, 38, 40, 73, 80], even

TABLE 4
Performance summary of representative graph-based FER methods

References	Prep. ¹		Representation ²		Reasoning		Posed Database ³	Wild Database	Validation ⁴	
	B.B.	LM	Category	Node	Edge	Model				Classifier
Mohseni et al. [76]	o	50	$S : \mathcal{L}$	\mathbb{C}	M+E	Tracking	Adaboost	MMI ar: 0.877	-	10F CV
Rivera and Chae [90]	•	-	$ST : \mathcal{R}$	Histograms	DNG	Tracking	SVM	CK+ ar: 1; MMI ar: 0.976; Oulu ar: 0.984	-	10F CV
Yao et al. [83]	•	-	$S : \mathcal{R}$	LBP	L	-	SVM /CNN	-	SFEW ar: 0.5538; AFEW ar: 0.5380;	HO
Dapogny et al. [40]	•	49	$S : \mathcal{L}$	$\mathbb{C}+HOG$	Δ	AE	RF	CK+ ar: 0.934 (w/o 0.915); BU-4DFE ar: 0.750 (w/o 0.730)	SFEW ar: 0.371 (w/o 0.357)	10F-SI CV /HO
Zhong et al. [22]	•	46	$S : \mathcal{L}$	Gabor	F+E	RNN	Softmax	CK+ ar: 0.9827; MMI ar: 0.9444; Oulu ar: 0.9368 (w/o 0.8263)	-	10F-SI CV
Chen et al. [43]	•	-	$AU : \mathcal{B}$	Φ	KNN	-	Softmax	CK+ ar: 0.9308 (w/o 0.8899); MMI ar: 0.7049 (w/o 0.6779); Oulu ar: 0.6385 (w/o 0.5935)	SFEW ar: 0.5650 (w/o 0.5219); RAF ar: 0.8553 (w/o 0.8181); AffNet ar: 0.5935 (w/o 0.5797)	CD (AffNet+RAF)
Liu et al. [36]	•	68	$S : \mathcal{L}$	$\mathbb{C}+HOG$	Δ	CNN	Softmax	CK+ ar: 0.9767; MMI ar: 0.8011	SFEW ar: 0.5536	10F-SI CV /HO
Xie et al. [86]	•	-	$S : \mathcal{R}$	ResNet	K-means	GCN	Softmax	CK+ ar: 0.8527; JAFEE [161] ar: 0.6150	SFEW ar: 0.5643; FER2013 ar: 0.5895 ExpW ar: 68.50%	CD (RAF)
Zhou et al. [87]	•	34	$ST : \mathcal{L}$	$\mathbb{C}+HOG$	M+H	GCN	Softmax	CK+ ar: 0.9863; Oulu ar: 0.8723	-	10F-SI CV
Liu et al. [91]	•	-	$ST : \mathcal{F}$	VGG	F	GCN	LSTM	CK+ ar: 0.9954; MMI ar: 0.8589; Oulu ar: 0.9104	-	10F-SI CV
Zhou et al. [41]	•	44	$ST : \mathcal{L}$	$\mathbb{C}+HOG$	L+H	GCN	Softmax	CK+ ar: 0.9892 (w/o 0.8726); Oulu ar: 0.8750 (w/o 0.8405)	AFEW ar: 0.4512 (w/o 0.2721)	10F-SI CV /HO
Cui et al. [37]	o	-	$AU : \mathcal{B}$	CNN	Φ	DBN	Softmax	CK+ ar: 0.9759 (w/o 0.9429); BP4D ar: 0.8382 (w/o 0.6168); MMI ar: 0.8490 (w/o 0.6735)	EmoNet ar: 0.9555 (w/o 0.8085)	5F-SI CV
Liu et al. [115]	•	40	$S : \mathcal{L}$	$\mathbb{C}+HOG+Gabor$ /C+CNN	L+H /E	GCN	Softmax	CK+ ar: 0.9923; MMI ar: 0.8575; Oulu ar: 0.9088	SFEW ar: 0.5742 RAF ar: 0.8713	10F-SI CV /HO
Chen et al. [104]	o	-	\mathcal{X}	HOG	KNN	GSC	SVM	CK+ (JAFEE) ar: 0.7171; JAFEE (CK+) ar: 0.5667; Oulu (CK+) ar: 0.4834; CK+ (Oulu) ar: 0.7756	-	CD
Shirian et al. [92]	o	68	$ST : \mathcal{F}$	\mathbb{C}	F	GCN	Softmax	RML [162] ar: 0.9411; eINTERFACE [163] ar: 0.8749; RAVDESS [164] ar: 0.8565	-	10F CV
Jin et al. [81]	•	68	$S : \mathcal{R}$	LBP/AE	F/M	GCN	Softmax	CK+ ar: 0.9432 (w/o 0.9286); Oulu ar: 0.7328 (w/o 0.6764)	RAF ar: 0.5825 (w/o 0.5663)	10F-SI CV /HO
Zhao et al. [74]	•	68	$S : \mathcal{L}$	$\mathbb{C}+CNN$	M	GCN	Softmax	CK+ (RAF) ar: 0.9320 (w/o 0.7864); MMI (RAF) ar: 0.7439 (w/o 0.5707); Oulu (RAF) ar: 0.6302 (w/o 0.4875)	SFEW ar: 0.5711 RAF ar: 0.8752	10F-SI CV /HO
Rao et al. [113]	•	68	$S : \mathcal{L}$	\mathbb{C}	M	GCN	Softmax	CK+ ar: 0.9868; JAFEE ar: 0.9664	FER2013 ar: 0.7806 RAF ar: 0.8695	10F/LO CV /HO
Liu et al. [101]	•	-	$AU : \mathcal{M}$	CNN	M	GCN	Softmax	-	RAF ar: 0.8931 (w/o 0.8582) AffNet ar: 0.6157 (w/o 0.5794)	HO
Antoniadis et al. [105]	•	-	\mathcal{X}	Φ	L	GCN	Softmax	-	AffNet ar: 0.6646 (w/o 0.6437), val_ccc: 0.767 (w/o 0.761), aro_ccc: 0.649 (w/o 0.628); Aff-Wild2 ar: 0.4892 (w/o 0.4506), val_ccc: 0.457 (w/o 0.416), aro_ccc: 0.514 (w/o 0.501)	HO

¹ Prep.: processing; B.B.: bounding boxes; LM: landmarks; • = Yes, o = No.

² $S/ST/AU/\mathcal{X}$: {spatial; spatio-temporal; AU-level; sample-level} representation; : $\mathcal{L}/\mathcal{R}/\mathcal{B}/\mathcal{M}/\mathcal{F}$: {landmark; region; label; map; frame}-level graph; \mathbb{C} : landmark coordinates; Φ : label distributions; Δ : triangulation; L/M/F: {learning; manual; full} connections; E: Euclidean distance; H: Hop distance.

³ ar: average accuracy rate; val/arv: valence/arousal; ccc: concordance correlation coefficient; DB1 (DB2): train on database 2, test on database 1; w/o: without graph.

⁴ CV: cross validation; LO: leave-one-subject-out; HO: holdout validation; 10F: 10-folds; SI: subject independent; CD (DB): cross database validation (training database).

for the spatio-temporal graph [89]. The possible reason is that the landmark information is helpful and practical for locating the facial areas where AUs may occur. In this setting, their node representations were close to that in spatial graphs of FER methods, which usually combined geometric coordinates with appearance features (e.g., HOG [36, 40]). Although some AUD methods using AU-level graphs also exploited traditional features (e.g., Gabor [93, 94], LBP [42]) or deep features (e.g., VGG [97]) to introduce the appearance

information, their graph representations were initialized from the AU label distribution of the training set. Thus, the DBN model has become popular in the relational reasoning stage [42, 93, 94]. Another similar trend to graph-based FER is that GNNs have been widely utilized to learn the latent dependency among individual AUs in recent studies, such as GCN [24, 80, 89, 98], GAT [99], GGNN [23], and DG-CNN [38]. But the difference is that fully-connected (FC) layers [23, 36, 80, 98] or regression models [24, 38, 102] are often

TABLE 5
Performance summary of representative graph-based AUD methods

References	Prep. ¹		Representation ²			Reasoning		Database ³	Validation ⁴
	B.B.	LM	Category	Node	Edge	Model	Output		
Zhu et al. [94]	•	49	$AU : B$	C+Gabor	Φ	DBN	MPE	CK+ ar: 0.9048 (w/o 0.8818), f_1 : 0.7072 (w/o 0.4976); DISFA ar: 0.9356 (w/o 0.9459), f_1 : 0.7095 (w/o 0.6553)	2F, 10F CV
Kaltwang et al. [73]	o	66	$S : L$	C	L	LT		DISFA corr: 0.43, mse: 0.39, icc: 0.36	9F CV
Walecki et al. [102]	o	-	$AU : M$	CNN	L	CRF	Ordinal Regression	FERA 2015 [165] icc: 0.63, mae: 1.23; DISFA icc: 0.45, mae: 0.61	HO
Corneanu et al. [97]	•	-	$AU : M$	VGG	Φ	RNN	Sigmoid	BP4D f_1 : 0.617; DISFA f_1 : 0.567	3F-SI CV
Dapogny et al. [40]	•	49	$S : L$	C+HOG	Δ	AE	RF	CK+ auc: 0.953, f_1 : 0.788, nf_1 : 0.865; BP4D: auc: 0.727, f_1 : 0.557, nf_1 : 0.636; DISFA auc: 0.824, f_1 : 0.491	10F-SI CV
Li et al. [23]	•	20	$AU : M$	C+VGG	M+L	GGNN	FC	BP4D auc: 0.741 (w/o 0.736), f_1 : 0.629 (w/o 0.620); DISFA auc: 0.807 (w/o 0.802), f_1 : 0.559 (w/o 0.530)	No report
Niu et al. [98]	•	-	$AU : M$	W	L	GCN	FC	BP4D f_1 : 0.598 (w/o 0.565); EmotioNet f_1 : 0.681 (w/o 0.623)	3F-SI CV/ HO
Liu et al. [80]	•	19	$S : R$	CNN+AE	M	GCN	FC	BP4D auc: 0.873, f_1 : 0.628; DISFA auc: 0.746, f_1 : 0.550	3F-SI CV
Fan et al. [38]	•	20	$S : R$	ResNet	KNN+E	DG-CNN	Heatmap Regression	BP4D icc: 0.72 (w/o 0.67), mae: 0.58 (w/o 0.60); DISFA icc: 0.47 (w/o 0.40), mae: 0.20 (w/o 0.21)	3F-SI CV
Liu et al. [36]	•	68	$S : L$	C+HOG	Δ	CNN	FC	CK+ auc: 0.929	10F-SI CV
Zhang et al. [24]	•	18	$S : R$	HRN	L	GCN	Heatmap Regression	BP4D f_1 : 0.635 (w/o 0.620); DISFA f_1 : 0.620	3F-SI CV
Cui et al. [42]	o	51	$AU : B$	LBP	Φ	DBN	LR /CNN /SVM	CK+ f_1 : 0.830 (w/o 0.785); BP4D f_1 : 0.687 (w/o 0.657); EmotionNet f_1 : 0.626 (w/o 0.620); MMI (CK+) f_1 : 0.532 (w/o 0.482)	5F-SI CV /CD
Cui et al. [37]	o	-	$AU : B$	VGG	Φ	DBN	FC	CK+ f_1 : 0.74 (w/o 0.69); BP4D f_1 : 0.57 (w/o 0.56); MMI f_1 : 0.58 (w/o 0.47)	5F-SI CV
Song et al. [99]	•	-	$AU : M$	ResNet	Mask	GAT	Softmax	BP4D ar: 0.782 (w/o 0.781), f_1 : 0.633 (w/o 0.599); DISFA ar: 0.934, f_1 : 0.600	3F-SI CV
Song et al. [100]	•	-	$AU : M$	ResNet	Φ	Hybrid GNN	Softmax	BP4D f_1 : 0.634 (w/o 0.596); DISFA f_1 : 0.610	3F-SI CV
Song et al. [25]	•	-	$AU : M$	ResNet	Φ	GCN+LSTM	FC	FERA 2015 icc: 0.72 (w/o 0.68), mae: 0.57 (w/o 0.64); DISFA icc: 0.56 (w/o 0.51), mae: 0.22 (w/o 0.35)	3F-SI CV
Chen et al. [89]	•	68	$ST : L$	DCT+CNN	M+Mask	GCN	Softmax	BP4D f_1 : 0.6489 (w/o 0.5842); DISFA f_1 : 0.6585 (w/o 0.5487)	3F-SI CV
Luo et al. [96]	•	-	$AU : M$	ResNet /Transformer	KNN+L	GCN	Softmax	BP4D f_1 : 0.655 (w/o 0.626); DISFA f_1 : 0.631 (w/o 0.591)	3F-SI CV

¹ Prep.: processing; B.B.: bounding boxes; • = Yes, o = No; LM: landmarks.

² $S/S T/AU$: {spatial; spatio-temporal; AU-level} representation; $L/R/B/M$: {landmark; region; label; map}-level graph; C: landmark coordinates; Φ : label distributions; Δ : triangulation; L/M : {learning; manual} connections; E: Euclidean distance.

³ ar: average accuracy rate; f_1 : F1 score; nf_1 : F1-norm score; corr: Pearson correlation coefficient; mae: mean absolute error; mse: mean squared error; icc: intra-class correlation coefficient; auc: area under the receiver operating characteristic curve; DB1 (DB2): train on database 2, test on database 1; w/o: without graph.

⁴ CV: cross validation; LO: leave-one-subject-out; (K)F: k-folds; SI: subject independent; HO: holdout validation; CD: cross database validation.

applied for predictions instead of *softmax* classifier [89, 99].

A particular line of AUD research analyzes the facial affects by estimating the AU intensities, which could have greater information value in understanding complex affective states [166]. Even though a few attempts in estimating AU intensities based on graph structures have existed [38, 73, 97], the study of using the latest spatio-temporal graph representations and GNNs has not been reported. Another big challenge in AUD is few and imbalanced samples. Recent graph-based methods using transfer learning [42, 98] or uncertainty learning [99] were proposed to address this problem. They showed an advantage of the graph-based method in this topic and are helpful to implement AUD in large-scale unlabeled data.

5.4 Micro-Expression Recognition

Micro-expressions are fleeting and involuntary facial affects that people usually exhibit in high stake situations when attempting to conceal or mask their true feelings [151]. The earliest well-known studies came from [167] as well as [168]. Generally, a micro-expression lasts only 1/25 to 1/2 seconds

long and is too subtle and fleeting for an untrained person to perceive. Therefore, developing an automatic micro-expression recognition (MER) system is valuable in reading human hidden affective states. Besides the short duration, low intensity and localization characteristics also make it challenging.

To this end, graph-based MER methods have been designed to address the above challenges and have become appealing in the past two years [82], especially in 2020 [39, 75]. Table 6 lists the reported performance of a few representative recent studies of graph-based MER. These methods fall into the landmark-level spatial graph [75, 82] and the AU-level graph [39] in terms of representation types. For the former, their idea is to use landmarks to locate and analyze specific facial areas to deal with the local response and the subtleness of micro-expressions. The latter aims to infer the AU relationship to improve the final performance. The difference in processing ideas is also reflected in the reasoning procedure. Approaches like GSC [82] and variant CNNs [75] are exploited in the landmark-

level graph to integrate the individual node feature representations. In comparison, GCNs are employed to learn an optimal graph structure of the AU dependency knowledge from training data and make predictions. Nevertheless, one common thing is that all the methods consider the local appearance in a spatio-temporal way by using *optical-flow* or *DNNs*.

A problem in graph-based MER is the lack of large-scale in-the-wild data. The small sample size limits the AU-level graph representation that relies on initializing the AU relationship from the AU label distribution of the training set. The lab-controlled data make it difficult to follow the trend in FER studies, which generalizes the graph-based FAA methods in real-world scenarios. However, the analysis of uncontrolled micro-expressions is fundamental because micro-expressions and macro-expressions can co-occur in many real cases. For example, the furrowing on the forehead slightly and quickly when smiling indicates the true feeling [168]. Since the evolutionary appearance information is crucial for the micro-expression analysis, building a spatio-temporal graph representation that can model the duration and the dynamic of micro-expressions is also a helpful but unexplored topic.

5.5 Other Tasks

The graph-based methods also play a vital role in several other FAA tasks, such as pain detection [73], non-basic affect recognition [85, 106], occluded FER [40, 41], and multi-modal affect recognition [88, 103]. Table 7 summarizes the latest graph-based FAA methods for these tasks. Their node representations and edge initialization strategies for graph constructions in this field are similar to those in graph-based FER, MER, and AUD methods. While for the reasoning step, GCN is the top-1 option. This observation implies that the framework of the graph-based method discussed in this paper can be easily extended to many other FAA tasks and promote performance improvement.

6 OPEN DIRECTIONS

Graph-based FAA methods have been dissected into fundamental components for elaboration and discussion in this review. When encoding facial affect into graphs, strategies vary according to node and edge elements. Relational reasoning approaches infer latent relationships or inherent dependencies of graph nodes in terms of space, time, and semantics. The category of graph representations will affect the technique choice of relational reasoning to a certain extent.

Despite significant advances and numerous work, the graph-based FAA is still an appealing field with many open directions. Due to advantages in modeling and reasoning latent relationships of facial affects, graph-based methods may provide complementary information to help solve some challenges that non-graph-based approaches face. Also, the graph-based method has natural advantages or unexplored research potential in other topics.

6.1 In-the-wild Scenarios

Although many efforts have been made for graph-based FAA in natural conditions [36, 39, 40, 41, 42, 43, 83, 98, 101, 105], even the state-of-the-art performance is far from

actual applications. Factors like illumination, head pose, and part occlusion are challenging in constructing an effective graph representation. For one thing, significant illumination changes and head pose variations will impair the accuracy of face detection and registration, which is vital for establishing landmark-level graphs. ROI graphs without landmarks or NPI graphs [83, 86] should be a possible direction to avoid this problem. Also, missing face parts resulting from camera view or context occlusion make it challenging to encode enough facial information and obtain meaningful connections in an affective graph. Pilot work [40, 41] has tried to exploit a sub-graph without masked facial parts or generate adaptive edge links to alleviate the influence. Unfortunately, there has still been a considerable performance decrease compared to normal conditions. Proposing more effective spatio-temporal graphs can account for these problems based on evolutionary affective information.

6.2 3D and 4D Facial Affects

Using 3D and 4D face images might be another good topic because the 3D face shape provides additional depth information and dynamically contains subtle facial deformations. They are intuitively insensitive to pose and light changes. Some studies have transformed 3D faces into 2D images and generated graph representations [23, 38, 40, 97], but they have not fully taken advantage of the 3D data. Alternatively, non-graph-based [175] and graph-based methods [78] have been explored to conduct FAA directly on 3D or 4D faces. Since the 3D face mesh structure is naturally close to the graph structure, employing the graph representation and reasoning to handle 3D face images will promote the improvement of in-the-wild FAA. Besides, there is also a potential topic of using 3D and 4D data with graph-based methods, especially landmark-level graphs and *GNNs*, in micro-expression recognition.

6.3 Valence and Arousal

Estimating the continuous dimension is a rising topic in FAA. Unlike discrete labels, Valence-Arousal (V-A) is a kind of quantitative annotation with dynamic evolutions, which provide another domain to analyze facial affects, especially in a temporal domain. Large-scale FAA databases (Aff-Wild I [15], II [160]) containing V-A annotations have been released to support the continuous FAA. Existing graph-based methods mainly perform the V-A measurement [38, 73, 102] on lab-controlled databases except for a few studies like [85, 105]. Recent graph-based methods have studied multi-label learning according to intrinsic mappings between facial affect categories and other annotations [23, 42, 105]. Such underlying assumptions can also be extended to the V-A measurement task, where AU-level graphs and *DBNs*, as well as sample-level graphs, are potential directions.

6.4 Context and Multi-modality

Most current FAA methods only consider a single face in one image or sequence. However, people usually have affective behaviors, including facial expressions, body gestures, and emotionally speaking in real cases [176]. These facial affective displays are highly associated with context surroundings that include but are not limited to the affective behavior of other people in social interactions or inanimate objects. Existing studies like [85] and [86] have employed

TABLE 6
Performance summary of representative graph-based MER methods

References	Prep. ¹		Representation ²			Reasoning		Database ³	Validation ⁴
	B.B.	LM	Category	Node	Edge	Model	Classifier		
Liu et al. [82]	•	66	$S : \mathcal{R}$	<i>Optical-flow</i>	<i>KNN</i>	<i>GSC</i>	<i>SVM</i>	SMIC (3 cl.) <i>ar</i> : 0.6795, f_1 : 0.6844; CASME I [169] (4 cl.) <i>ar</i> : 0.7219, f_1 : 0.7236; CASME II (5 cl.) <i>ar</i> : 0.6356, f_1 : 0.6364	LO CV
Lei et al. [75]	•	28	$S : \mathcal{L}$	<i>TCN</i>	<i>F</i>	<i>Graph-TCN</i>	<i>Softmax</i>	CASME II (5 cl.) <i>ar</i> : 0.7398, f_1 : 0.7246; SAMM (5 cl.) <i>ar</i> : 0.7500, f_1 : 0.6985; SAMM (4 cl.) <i>ar</i> : 0.8050, f_1 : 0.7657	LO CV
Xie et al. [39]	•	-	$AU : \mathcal{M}$	<i>CNN</i>	<i>L</i>	<i>GCN</i>	<i>Softmax</i>	CASME II (3 cl.) <i>ar</i> : 0.712, f_1 : 0.355; CASME II (7 cl.) <i>ar</i> : 0.561, f_1 : 0.394; SAMM (3 cl.) <i>ar</i> : 0.702, f_1 : 0.433; SAMM (8 cl.) <i>ar</i> : 0.523, f_1 : 0.357 SMIC (CASME II) (3 cl.) <i>ar</i> : 0.344, f_1 : 0.319; SMIC (SAMM) (3 cl.) <i>ar</i> : 0.451, f_1 : 0.309	LO CV /CD
Kumar and Bhanu [72]	•	51	$S : \mathcal{L}$	$\mathbb{C} + \textit{Optical-flow}$	<i>M+L</i>	<i>GCN+GAT</i>	<i>Softmax</i>	CASME II (3 cl.) <i>ar</i> : 0.8966, f_1 : 0.8695; CASME II (5 cl.) <i>ar</i> : 0.8130, f_1 : 0.7090; SAMM (3 cl.) <i>ar</i> : 0.8872, f_1 : 0.8118; SAMM (5 cl.) <i>ar</i> : 0.8824, f_1 : 0.8279	LO CV
Lei et al. [95]	•	30	$AU : \mathcal{B}$	<i>Embedding</i>	Φ	<i>GCN</i>	<i>Softmax</i>	CASME II (4 cl.) <i>ar</i> : 0.8080 (w/o 0.7880), f_1 : 0.7871; CASME II (5 cl.) <i>ar</i> : 0.7427, f_1 : 0.7047; SAMM (4 cl.) <i>ar</i> : 0.8239, f_1 : 0.7735; SAMM (5 cl.) <i>ar</i> : 0.7426, f_1 : 0.7045	LO CV

¹ Prep.: processing; B.B.: bounding boxes; • = Yes, o = No; LM: landmarks.
² S / AU : {spatial; AU-level} representation; $\mathcal{R} / \mathcal{L} / \mathcal{B} / \mathcal{M}$: {region; landmark; label; map}-level graph; \mathbb{C} : landmark coordinates; Φ : label distributions; $M/L/F$: {manual; learning; fully} connections.
³ *ar*: average accuracy rate; f_1 : F1 score; (N) cl.: (N) affective classes; DB1 (DB2): train on database 2, test on database 1; w/o: without graph.
⁴ CV: cross validation; LO: leave-one-subject-out; CD: cross database validation.

TABLE 7
Performance summary of graph-based methods for special FAA tasks

References	Prep. ¹		Representation ²			Reasoning		Database ³	Validation ⁴
	B.B.	LM	Category	Node	Edge	Model	Output		
Kaltwang et al. [73]	o	66	$S : \mathcal{L}$	\mathbb{C}	<i>L</i>	<i>LT</i>		ShoulderPain [170] <i>corr</i> : 0.23, <i>mse</i> : 0.60	8F CV
Dapogny et al. [40]	•	49	$S : \mathcal{L}$	$\mathbb{C} + \textit{HOG}$	Δ	<i>AE</i>	<i>RF</i>	CK+ (eyes occluded) <i>ar</i> : 0.879; CK+ (mouth occluded) <i>ar</i> : 0.727	10F-SI CV
Zhang et al. [85]	•	-	$S : \mathcal{R}$	<i>VGG</i>	<i>L</i>	<i>GCN</i>	<i>Softmax/FC</i>	EMOTIC (26 cl.) <i>prc</i> : 0.2842; EMOTIC <i>val_er</i> : 0.7, <i>aro_er</i> : 1.0, <i>dom_er</i> : 1.0	HO
Chen et al. [88]	•	68	$ST : \mathcal{L}$	\mathbb{C}	$\Delta + M$	<i>GCN</i>	<i>FC</i>	CES [18] <i>val_ccc</i> : 0.515, <i>aro_ccc</i> : 0.513	HO
He and Jin [106]	o	-	\mathcal{X}	<i>Embedding</i>	<i>M+L</i>	<i>GCN</i>	<i>Softmax</i>	FlickLDL [171] <i>ar</i> : 0.691; TwiterLDL [172] <i>ar</i> : 0.758	HO
Zhou et al. [41]	•	44	$ST : \mathcal{L}$	$\mathbb{C} + \textit{HOG}$	<i>L+H</i>	<i>GCN</i>	<i>SoftMax</i>	CK+ (random occlusion) <i>ar</i> : 0.9551 (w/o 0.6226); Oulu (random occlusion) <i>ar</i> : 0.8121 (w/o 0.5748); AFEW (random occlusion) <i>ar</i> : 0.4047 (w/o 0.2122)	10F-SI CV /HO
Chien et al. [103]	o	-	\mathcal{X}	<i>CNN</i>	<i>Transfer Knowledge</i>	<i>GCN</i>	<i>FC</i>	Amigos [173] (Ascertain) <i>val_uar</i> : 0.798, <i>aro_uar</i> : 0.679; Ascertain [174] (Amigos) <i>val_uar</i> : 0.704, <i>aro_uar</i> : 0.569	CD

¹ Prep.: processing; B.B.: bounding boxes; • = Yes, o = No; LM: landmarks.
² $S / ST / \mathcal{X}$: {spatial; spatio-temporal; sample-level} representation; $\mathcal{L} / \mathcal{R}$: {landmark; region}-level graph; \mathbb{C} : landmark coordinates; Δ : triangulation; M/L : {manual/learning} connections; H : Hop distance.
³ *corr*: Pearson correlation coefficient; *mse*: mean squared error; *ar*: average accuracy rate; *prc*: area under the precision recall curves; *er*: average error rate; *val/aro/dom*: valance/arousal/dominance; *ccc*: concordance correlation coefficient; *uar*: unweighted average recall; (N) cl.: (N) affective classes; DB1 (DB2): train on database 2, test on database 1; w/o: without graph.
⁴ CV: cross validation; (K)F: k-folds; SI: subject independent; HO: holdout validation; CD: cross database validation.

graph reasoning to infer relationships between the target face and other objects in the same image. Facial affects and other helpful contexts can be combined in a graph representation to perform the analysis on a fuller scope, such as the gesture [177, 178]. Another valuable topic is to introduce additional data channels that are multi-modality. Sample-level and spatio-temporal have also been successfully extended to process multi-modal affect analysis tasks with audio [88] and physiological signal [103], respectively, which shows a good research prospect.

6.5 Transfer Learning and Cross-database

Insufficient and invalid annotations are significant challenges that limit the development of FAA research, especially for deep learning. One possible solution is to use graph-based transfer learning, which could build bridges among different label spaces such as discrete-to-continuous labels [105] and emotional-to-AU labels [101]. Efforts of using the graph structure have been explored to solve these

challenges in terms of semi-supervision [98], label correction [42], or uncertainty measurement [99]. On the other hand, the cross-database performance of features extracted using graph-based methods has been demonstrated in all FER [43, 86], AUD [42, 93], MER [39], and cross-corpus analysis [103, 104]. Considering the strength of AU-level and sample-level graphs in searching intrinsic distributions, a universal affective feature encoder could be expected to break down barriers across various databases and achieve better generalization capability.

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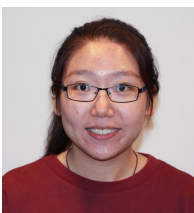
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