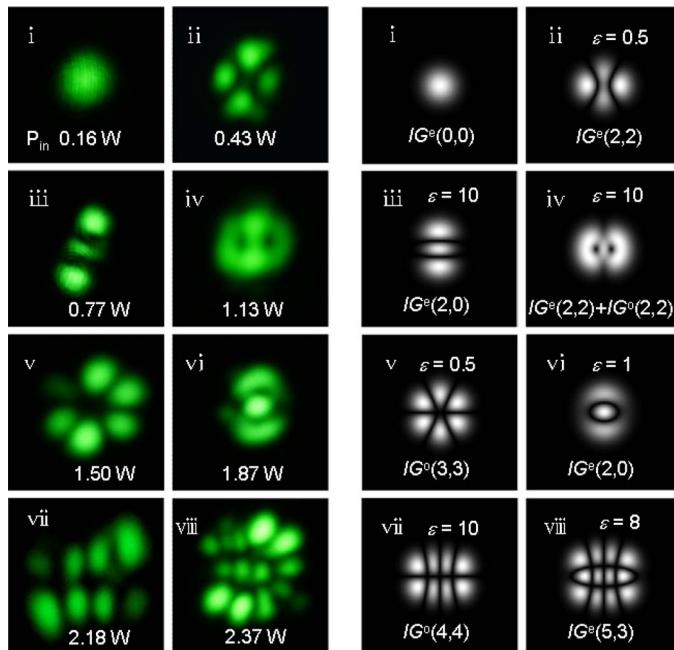


# Direct Generation of Subnanosecond Ince–Gaussian Modes in Microchip Laser

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# Direct Generation of Subnanosecond Ince–Gaussian Modes in Microchip Laser

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**Abstract:** In this paper, a new method is used to direct generate Ince–Gaussian (IG) modes from a pulsed solid-state microchip laser. By moving a circular aperture horizontally, the gain size in the laser medium is adjusted, and different IG laser modes are obtained successively. The output laser possesses a stable pulse duration of 500–600 ps; at the same time, the repetition frequency varies between 7 and 16 kHz. To our knowledge, this is the first time that IG modes are obtained in the subnanosecond laser domain, which will be helpful for making large-energy high-peak-power devices.

**Index Terms:** Ince–Gaussian mode, subnanosecond pulse, microchip laser.

## 1. Introduction

Ince–Gaussian (IG) modes, which are a third family of paraxial wave equation solutions, are orthogonal in elliptic coordinates [1]. They can transit into rectangular and cylindrical coordinate solutions, i.e., Hermite–Gaussian modes [2]–[4] and Laguerre–Gaussian modes [5]–[10], by adjusting ellipticity  $\varepsilon$  [11]. IG modes have been utilized in form of optical vortices for optical trapping [12], [13], optical tweezers [14], [15], and quantum information tasks [16]. Different methods have been used to generate high order IG modes, including off-axis pumping, tilted pumping, or introducing a crosshair inside the cavity [17]–[19]. Single-frequency and nanosecond pulsed IG mode operations of diode-pumped microchip lasers have been reported previously [17], [20].

Pulsed IG modes especially for sub-nanosecond lasers possess high peak power and low average output power. Such properties can provide high efficiency in manipulating small objects and do less harm to them especially for living objects, like biological cells. In order to get sub-nanosecond pulses from microchip lasers, a traditional gain medium and saturable absorber need to be cut thinner, from the millimeter level to the micrometer level. Tilted pumping, which increases threshold power, will take the risk of the laser component's fragmentation.

In this paper, we report the generation of IG modes in a sub-nanosecond microchip laser. A new method, i.e., moving a circular aperture, is invented to adjust the pump beam, and as many as eight types of IG modes have been observed with stable pulse duration of 500–600 ps.

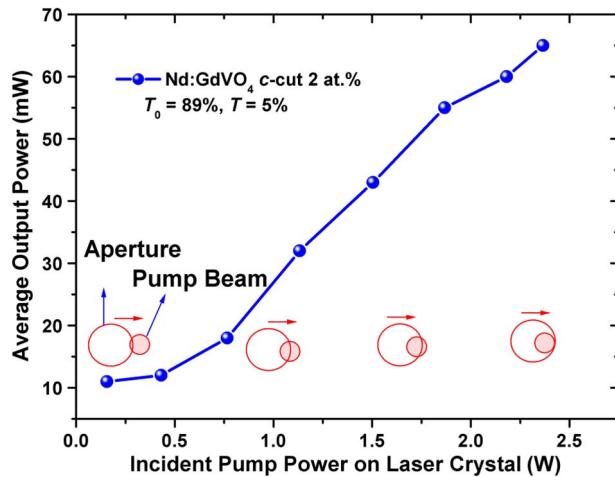


Fig. 1. Average output power versus incident pump power on the Nd:GdVO<sub>4</sub> microchip.

## 2. Experimental Details

In this experiment, the laser system was a laser diode pumped Nd:GdVO<sub>4</sub>/Cr<sup>4+</sup>:YAG microchip laser with a plane-parallel cavity. The gain medium was a 0.4 mm thick, c-cut Nd:GdVO<sub>4</sub> crystal with 2 at.% Nd<sup>3+</sup> doping, which can generate unpolarized laser. One surface of the Nd:GdVO<sub>4</sub> crystal was used as the input mirror, which was anti-reflection (AR) coated at 808 nm and high-reflection (HR) coated at 1064 nm. The other surface was AR coated at 1064 nm and HR coated at 808 nm. A 0.2 mm thick, [111]-oriented Cr<sup>4+</sup>:YAG crystal with initial transmission of 89% was used as the passive Q-switcher. One of its surfaces was AR coated at 1064 nm, and the other surface was partial transmission coated at 1064 nm ( $T = 5\%$ ), served as the output mirror. The pump source was a commercial available fiber coupled 808 nm laser diodes module (LIMO Inc.). An optical coupler comprised of two lenses delivered the pump light into the laser crystal with a beam radius of 100  $\mu\text{m}$ . A copper aperture with radius of 0.5 mm was placed ahead of the input mirror. This aperture can be horizontally moved by a slide rail. The Q-switched pulses were detected by a fast photodiode, and measured by a 16-GHz oscilloscope (DSO-X 91604A, Agilent Inc.). The laser output power was measured by an energy/power meter (Power Max 500 D, Molelectron Inc.). To record the IG modes, a KTiOPO<sub>4</sub> (KTP) crystal cut along the type-II phase-matching direction was used as the frequency doubler to generate green visible laser, then the mode patterns were photographed by a camera (NEX-5N, Sony Inc.)

## 3. Results

Based on the method of Innocenzi *et al.* [21]

$$f = \frac{\pi K_c w_p^2}{P_{ph}(dn/dT)} \left( \frac{1}{1 - \exp(-\alpha l)} \right). \quad (1)$$

In (1) with  $K_c = 0.0117 \text{ W/mmK}$ ,  $dn/dT = 4.7 \times 10^{-6}/\text{K}$ ,  $\alpha = 74 \text{ cm}^{-1}$ , and  $w_p^2/P_{ph} = 0.021 \text{ mm}^2/\text{W}$ ,  $l = 0.4 \text{ mm}$ , the thermal lens focal length  $f$  was calculated to be 173 mm. Combining with ABCD matrix theory, the fundamental beam radius in the resonator was estimated to be 60  $\mu\text{m}$ . The incident pump power was set to be 2.37 W. The average pump intensity on laser crystal was calculated to be 75 MW/m<sup>2</sup>, which was well above the threshold pump intensity of 66 MW/m<sup>2</sup>. It guaranteed laser could oscillate even at small pump area. To generate IG modes, the circular aperture was moved from surrounding to center with a fixed step length of 25  $\mu\text{m}$ . Fig. 1 shows the average output power as a function of incident pump power, at different shapes of pump beam. Fig. 2(a) shows the measured intensity distributions of IG modes with different mode

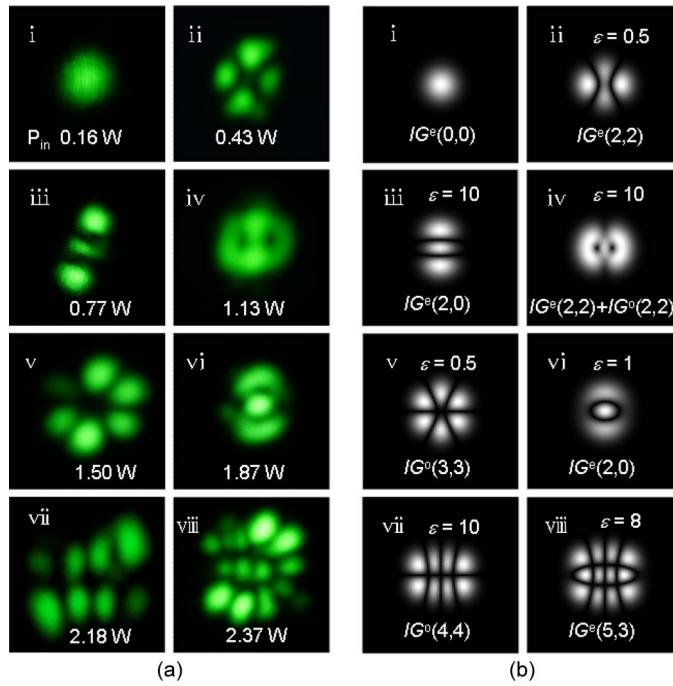


Fig. 2. (a) Intensity distribution of IG modes observed in Nd:GdVO<sub>4</sub>/Cr<sup>4+</sup>:YAG laser under different incident pump power. (b) Analytical solutions corresponding to the experimental results.

numbers  $p$ ,  $m$ , and ellipticity  $\varepsilon$ . The corresponding theoretical simulation results were shown in Fig. 2(b). An  $IG^e(0,0)$  mode was observed at an incident pump power of 0.16 W. As the incident pump power increasing, high order  $IG$  modes such as  $IG^e(2,2)$ ,  $IG^e(2,0)$ ,  $IG^e(2,2) + IG^o(2,2)$ ,  $IG^o(3,3)$ ,  $IG^o(4,4)$ , and  $IG^e(5,3)$  were obtained successively. In theory, the  $IG$  modes in the elliptic coordinate system  $r = (\xi, \eta, z)$  are given by [1]

$$IG_{p,m}^e(r, \varepsilon) = \frac{Cw_0}{w(z)} C_p^m(i\xi, \varepsilon) C_p^m(\eta, \varepsilon) \exp\left[-\frac{r^2}{w^2(z)}\right] \times \exp[i\left[kz + \frac{kr^2}{2R(z)} - (p+1)\psi(z)\right]] \quad (2)$$

$$IG_{p,m}^o(r, \varepsilon) = \frac{Sw_0}{w(z)} S_p^m(i\xi, \varepsilon) S_p^m(\eta, \varepsilon) \exp\left[-\frac{r^2}{w^2(z)}\right] \times \exp[i\left[kz + \frac{kr^2}{2R(z)} - (p+1)\psi(z)\right]]. \quad (3)$$

The elliptic coordinates are defined in  $z$  plane as  $x = f(z)\cosh(\xi)\cos(\eta)$ ,  $y = f(z)\sinh(\xi) \times \sin(\eta)$ , where  $\xi \in [0, \infty)$ ,  $\eta \in [0, 2\pi]$ ,  $f(z) = f_0 w(z)/w_0$  are the radial and angular elliptic variables, semifocal separation, respectively.  $f_0$  is the semifocal separation at the beam waist plane ( $z = 0$ ).  $C$  and  $S$  are normalized constants.  $w(z)$ ,  $w_0$  are the laser beam waists at  $z = z$  and  $z = 0$  planes.  $R(z)$  is the phase front curvature radius.  $\psi(z)$  is the Gouy shift.  $C_p^m$  and  $S_p^m$  are different Ince polynomials corresponding to even and odd  $IG$  modes, respectively.

The analytical solutions that  $m$ ,  $(p-m)/2$  equal number of hyperbolic nodal lines, elliptic nodal lines, with appropriate ellipticity parameter  $\varepsilon$  are in agreement with experimental transverse patterns. Due to the saturable absorber (Cr<sup>4+</sup>:YAG), an additional component, and the pump beam profile, smooth connection circular, we find the difficulty of mimicking images by Fresnel-Kirchhoff integration [22]. A qualitative model was derived. The  $IG$  modes of Nd:GdVO<sub>4</sub>/Cr<sup>4+</sup>:YAG laser were affected by saturated inversion population distribution. According to the analysis of Dong *et al.* [17], the population inversion  $\Delta N$  is proportional to the parameter  $(P_{in}/\pi w_p^2) \cdot \exp(-2r^2/w_p^2)$ . As shown in Fig. 1, when the aperture moved horizontally, the pump intensity  $P_{in}/\pi w_p^2$  was controlled to be a constant from first to last, while effective  $w_p$  has an increasing tendency for this special pump geometry, and therefore,  $\Delta N$  would increase as well.

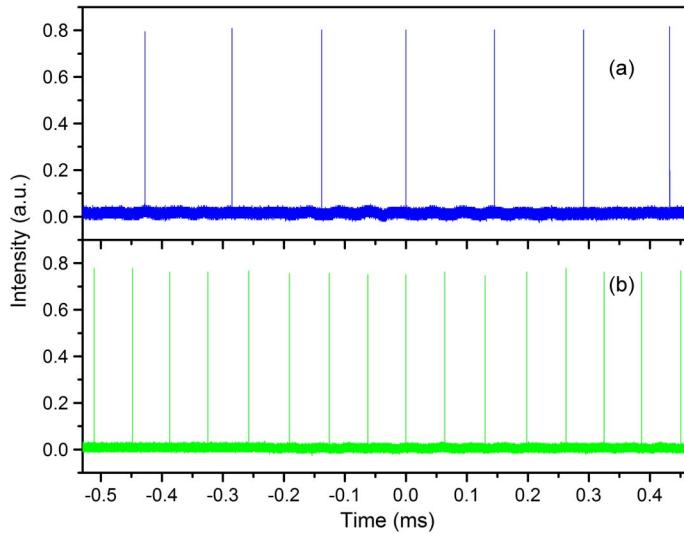


Fig. 3. Pulse trains with repetition frequencies of (a) 7 kHz and (b) 16 kHz for incident pump power of 0.16 W and 2.37 W, respectively.

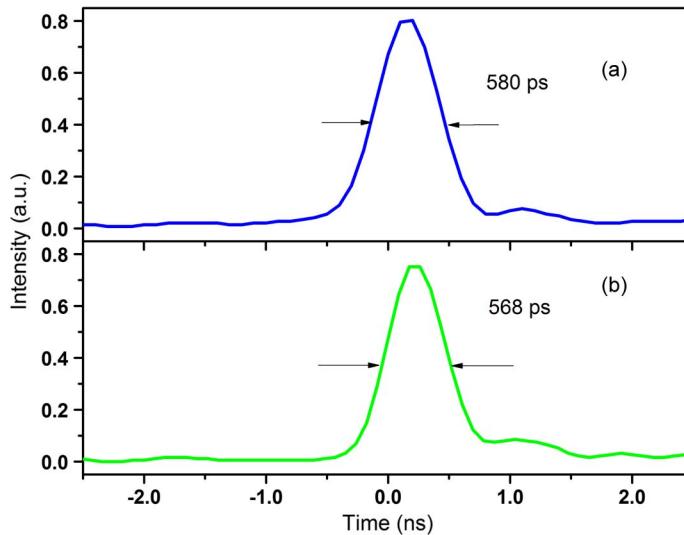


Fig. 4. Pulse profiles with the width of (a) 580 ps and (b) 568 ps for repetition frequencies of 7 kHz and 16 kHz, respectively.

The gain competing in a larger area made high order IG modes oscillating. Meanwhile, the interference pattern of high order IG modes varies slightly different from analytical forms due to thermal lens effect with large area. The experiment proved that even and odd modes can be generated through this method.

Figs. 3 and 4 showed the typical pulse trains and profiles of Nd:GdVO<sub>4</sub>/Cr<sup>4+</sup>:YAG microchip laser under incident pump power of 0.16, 2.37 W. The laser oscillated at 7 and 16 kHz repetition rates with less than 5% time jitter, which is less than 1% pulse amplitude fluctuation. The pulse width of 580, 568 ps were recorded. Table 1 listed the primary parameters for sub-nanosecond IG mode laser. It could be seen that the pulse widths were sustained in a range of 500–600 ps, which was basically independent with the incident pump power. The peak power and repetition frequency increased from 2.3 kW to 7.4 kW and 7 kHz to 16 kHz, respectively. The optical to

TABLE 1

Characteristic parameters of sub-nanosecond *IG* mode microchip laser

Incident pump power (W)	0.16	0.43	0.77	1.13	1.50	1.87	2.18	2.37
Pump beam area ( $10^{-9} \text{ m}^2$ )	2.13	5.73	10.27	15.07	20.00	24.93	29.07	31.40
Average output power (mW)	11	12	18	32	43	55	60	65
Pulse width (ps)	580	568	577	547	588	573	574	568
Repetition frequency (kHz)	7	9	10	11	12	13	15	16
Peak power (kW)	2.7	2.3	3.1	5.3	6.1	7.4	7.0	7.2
<i>IG</i> mode	$IG^e(0,0)$	$IG^e(2,2), \varepsilon = 0.5$	$IG^e(2,0), \varepsilon = 10$	$IG^e(2,2), \varepsilon = 10$	$IG^o(3,3), \varepsilon = 0.5$	$IG^e(2,0), \varepsilon = 1$	$IG^o(4,4), \varepsilon = 10$	$IG^e(5,3), \varepsilon = 8$

optical conversion efficiency ( $\eta_{0-0}$ ) of the fundamental mode,  $IG^e(0,0)$ , was 6.9%, which was higher than those of high order *IG* modes (2.3–2.9%).

#### 4. Conclusion

By moving a circular aperture to vary the pump area, high peak power, sub-nanosecond *IG* modes were obtained from a Nd:GdVO<sub>4</sub>/Cr<sup>4+</sup>:YAG microchip laser. Under an incident pump power of 0.16 W, the  $IG^e(0,0)$  mode was generated with an optical to optical efficiency of 6.9%. When incident pump power increased to 2.37 W,  $IG^e(5,3)$ ,  $\varepsilon = 8$  mode was obtained with 568 ps pulse duration and 7.2 kW peak power. This high performance, miniature *IG* laser device will have good application prospects in many scopes, such as quantum cryptography, quantum teleportation, and quantum computation.

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