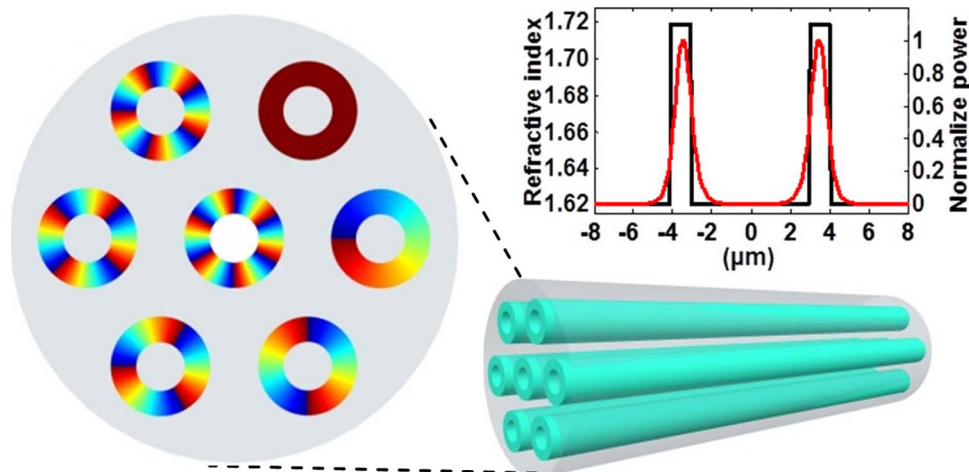


# Multi-Orbital-Angular-Momentum Multi-Ring Fiber for High-Density Space-Division Multiplexing

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# Multi-Orbital-Angular-Momentum Multi-Ring Fiber for High-Density Space-Division Multiplexing

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**Abstract:** A compact low-crosstalk multi-ring fiber transmitting multiple orbital angular momentum (OAM) modes is presented. The multi-OAM-mode multi-ring fiber (MOMRF) consists of 7 rings, each supporting 22 modes with 18 OAM ones (i.e., 154 channels in total), which can be used for high-density space-division multiplexing. The employed high-contrast-index ring structure benefits tight light confinement and large effective refractive index difference of different OAM modes ( $> 10^{-4}$ ), featuring both low-level inter-ring crosstalk ( $< -30$  dB for a 100-km-long fiber) and intermode crosstalk over a wide wavelength range (1520–1580 nm). The designed MOMRF is also compatible with wavelength-division multiplexing technique (e.g., 75 ITU-grid wavelengths from 1520.25 to 1579.52 nm with 100-GHz spacing) and advanced multilevel amplitude/phase modulation formats (e.g., 16-ary quadrature amplitude modulation), which might be used to achieve petabit-per-second total transmission capacity and hundred bits-per-second-per-hertz aggregate spectral efficiency.

**Index Terms:** Orbital angular momentum (OAM), multi-orbital-angular-momentum multi-ring fiber (MOMRF), space-division multiplexing (SDM), optical fiber communications.

## 1. Introduction

“Twisted” light beams, having helical phase fronts along the direction of propagation, carry orbital angular momentum (OAM) which is a fundamental physical quantity of light [1]. OAM-carrying twisted light beams, also called OAM beams, have been widely used in a variety of interesting applications ranging from optical manipulation to quantum information processing [2]–[6]. Very recently, OAM beams have also attracted much attention for increasing transmission capacity and spectral efficiency in both free-space and fiber optical communication systems [7]–[10]. Generally speaking, OAM beams with different charge numbers (i.e. different values of orbital angular momentum) are inherently orthogonal with each other. Hence, it is expected that OAM beams can be employed as information carriers for spatial mode-division multiplexing, providing alternative option to tackle the capacity crunch beyond existing multiplexing techniques.

To some extent, OAM multiplexing is similar to the well-known space-division multiplexing (SDM) with multi-core fiber (MCF) and few-mode fiber (FMF) in fiber optical transmission systems [11], [12]. In general, linearly polarized (LP) modes are adopted in FMF and the number of LP modes to

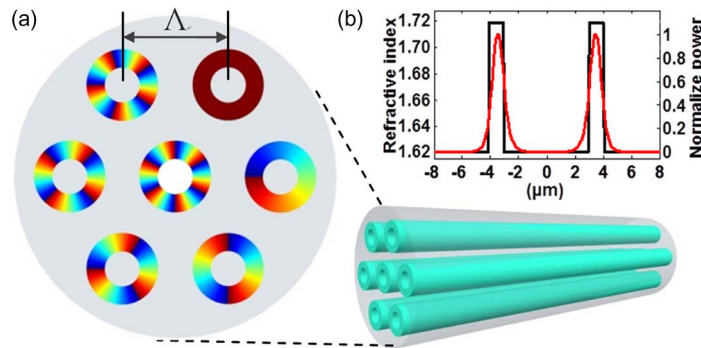


Fig. 1. (a) 3D structure and cross-section of multi-OAM-mode multi-ring fiber (MOMRF). (b) Index profile of single ring (black) and mode profile of  $\text{TE}_{01}$  mode (red) in the ring.

be multiplexed is limited to a small value to relieve inter-mode crosstalk and simplify processing complexity (e.g. multiple-input multiple-output (MIMO)). In order to develop fiber multi-mode communications using OAM, several challenges should be considered: i) special fiber design supporting OAM modes; ii) simultaneous transmission of multiple OAM modes with low-level inter-mode crosstalk; iii) compatible with existing multiplexing techniques. Fiber-based OAM generation and transmission using specially designed high-index ring structure have been reported [8], [13]–[15]. Another laudable goal would be to further optimize the fiber structure to transmit multiple OAM modes without impacting on each other. Additionally, in view of recent works of few-mode multi-core fiber [16], it would be also valuable to combine fiber OAM multiplexing and multi-core-like structure for high-density SDM applications.

In this paper, we propose a simple multi-OAM-mode multi-ring fiber (MOMRF) for SDM. The large difference of effective refractive index of fiber eigenmodes ( $>10^{-4}$ ) in each ring are assumed to benefit negligible inter-mode crosstalk. Moreover, the high-contrast-index ring structure enables a much lower-level inter-ring crosstalk ( $<-30$  dB for a 100-km long fiber). The designed fiber contains 7 rings with each ring supporting 22 modes (18 OAM ones), i.e. 154 channels in total, which can be used for high-density SDM.

## 2. Design of Multi-OAM-Mode Multi-Ring Fiber

Fig. 1(a) illustrates the 3D structure and cross-section of the designed MOMRF in which 7 identical high-index rings are arranged hexagonally. The ring-to-ring distance  $\Lambda$  and the cladding diameter of the MOMRF are  $30 \mu\text{m}$  and  $125 \mu\text{m}$ , respectively. The materials used in the MOMRF are (1) ring: Schott SF4 with  $n_r = 1.72$ , (2) cladding: Schott SF2 with  $n_c = 1.62$  (1550 nm). Practical fabrication of special fiber using similar type of materials has been achieved [17], [18]. Fig. 1(a) also depicts phase distributions of different OAM modes (phase of one mode in each ring is plotted as an example). Fig. 1(b) shows the refractive index profile (black curve) of a single ring with the inner radius  $r_1$  of  $3 \mu\text{m}$  and outer radius  $r_2$  of  $4 \mu\text{m}$ . The calculated mode profile (red curve) of  $\text{TE}_{01}$  mode guided by the ring structure is also shown in Fig. 1(b).

Note that crosstalk is one of the most important parameters characterizing the performance of SDM applications. Generally speaking, there are three types of crosstalk in the MOMRF: (1) inter-mode crosstalk of different order OAM modes in the same ring; (2) inter-ring crosstalk of the same order OAM mode in different rings; (3) crosstalk of different order OAM modes in different rings which can be ignored when both inter-mode and inter-ring crosstalks are negligible. A reasonable way to design and optimize the proposed MOMRF is expected to study and minimize the inter-mode crosstalk and inter-ring crosstalk.

## 3. Results and Discussions

We optimize the fiber design using the aforementioned geometry parameters to effectively suppress both inter-mode and inter-ring crosstalks. We first characterize in detail the guided modes

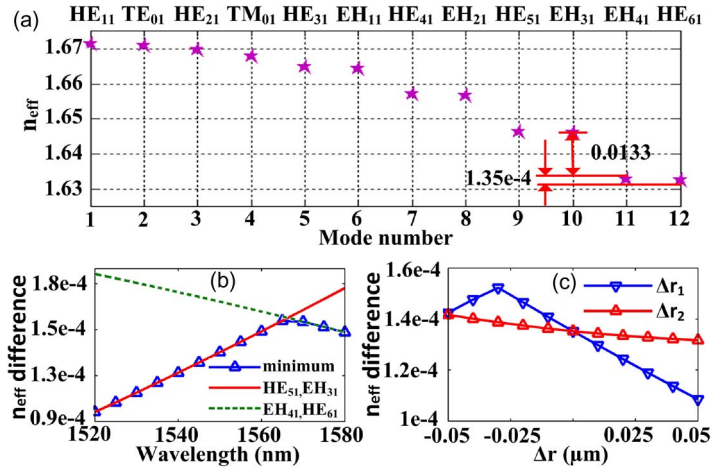


Fig. 2. (a) Effective refractive index ( $n_{eff}$ ) of all fiber eigenmodes in a single ring. (b) Minimum  $n_{eff}$  difference versus wavelength. (c) Minimum  $n_{eff}$  difference versus variation of inner ( $r_1$ ) or outer ( $r_2$ ) ring radius.

in each single ring of the proposed MOMRF and show their properties in terms of effective refractive index ( $n_{eff}$ ), wavelength dependence, and phase distributions. Remarkably, not conventional optical fiber but a high-contrast-index ring fiber is used to support OAM modes as such structure can increase the  $n_{eff}$  difference of fiber eigenmodes [19]. It is believed that large  $n_{eff}$  difference can benefit reduced inter-mode crosstalk.

Fig. 2(a) shows  $n_{eff}$  of all fiber eigenmodes at 1550 nm in each ring calculated by finite-element method. Note that each HE<sub>*mn*</sub> or EH<sub>*mn*</sub> also contains even and odd modes, hence 22 fiber eigenmodes are supported in a single ring of the designed MOMRF. The maximum  $n_{eff}$  difference can be as high as 0.0133 between EH<sub>31</sub> and EH<sub>41</sub> modes, and even the minimum  $n_{eff}$  difference can reach  $1.35 \times 10^{-4}$  between EH<sub>41</sub> and HE<sub>61</sub> modes. With these fiber eigenmodes (i.e. TE<sub>01</sub>, TM<sub>01</sub>, HE<sub>*mn*</sub>, EH<sub>*mn*</sub>), one can obtain 22 modes with 18 OAM ones which are combined by even and odd modes of HE<sub>*mn*</sub> or EH<sub>*mn*</sub> modes with a  $\pm\pi/2$  phase shift [20], i.e. HE<sub>*mn*</sub><sup>even</sup>  $\pm i \times$  HE<sub>*mn*</sub><sup>odd</sup>, EH<sub>*mn*</sub><sup>even</sup>  $\pm i \times$  EH<sub>*mn*</sub><sup>odd</sup>. The corresponding topological charge number of OAM mode is  $\pm(m-1)$  for HE<sub>*mn*</sub><sup>even</sup>  $\pm i \times$  HE<sub>*mn*</sub><sup>odd</sup> while  $\pm(m+1)$  for EH<sub>*mn*</sub><sup>even</sup>  $\pm i \times$  EH<sub>*mn*</sub><sup>odd</sup>, respectively. In particular, the large  $n_{eff}$  difference ( $>10^{-4}$ ) among all the supported fiber eigenmodes are assumed to benefit negligible inter-mode crosstalk [8], [16], [19]. For instance, in a recent OAM-based mode-division multiplexing over a 1.1-km fiber, different modes transmitted along the fiber separately with negligible inter-mode crosstalk owing to the large effective refractive index difference ( $\sim 10^{-4}$ ), which succeeded in the long-length mode-division multiplexing system without using any multiple-input multiple-output (MIMO) processing. Additionally, compared to the well-known FMF supporting only few number of LP modes, the optimized design of high-contrast-index ring fiber can transmit 22 modes (18 OAM ones) simultaneously with low-level inter-mode crosstalk. We also study the dependence of minimum  $n_{eff}$  difference on the wavelength and fabrication tolerance (i.e. variation of inner or outer ring radius). As shown in Fig. 2(b), the minimum  $n_{eff}$  difference almost remains above  $10^{-4}$  within a wavelength range from 1520 to 1580 nm which covers the whole C band and enters into the S and L bands. The wavelength-dependent  $n_{eff}$  difference between HE<sub>51</sub> and EH<sub>31</sub> as well as between EH<sub>41</sub> and HE<sub>61</sub> is also plotted for reference. Actually, Fig. 2(b) indicates that the designed ring structure can be compatible with existing wavelength-division multiplexing (WDM) technique. Within 1520 to 1580 nm, multiple wavelengths (e.g. 75 ITU-grid wavelengths from 1520.25 to 1579.52 nm with 100-GHz spacing) each having 22 modes with low-level inter-mode crosstalk can be multiplexed together to increase the transmission capacity. As shown in Fig. 2(c), the minimum  $n_{eff}$  difference keeps above  $10^{-4}$  with varied inner ( $r_1$ : 2.95 to 3.05  $\mu m$ ) or outer ( $r_2$ : 3.95 to 4.05  $\mu m$ ) ring radius, featuring favorable fabrication tolerance.

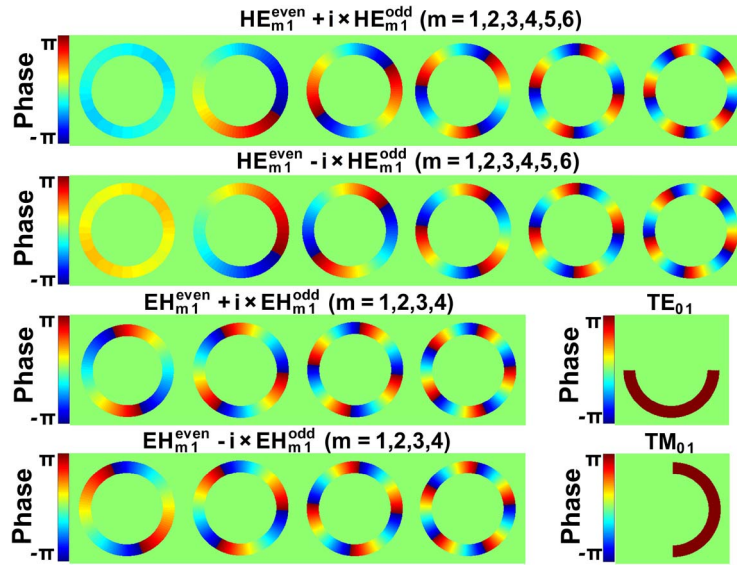


Fig. 3. Spatial phase distributions of the x-component electric field of 22 modes (18 OAM ones) in MOMRF.

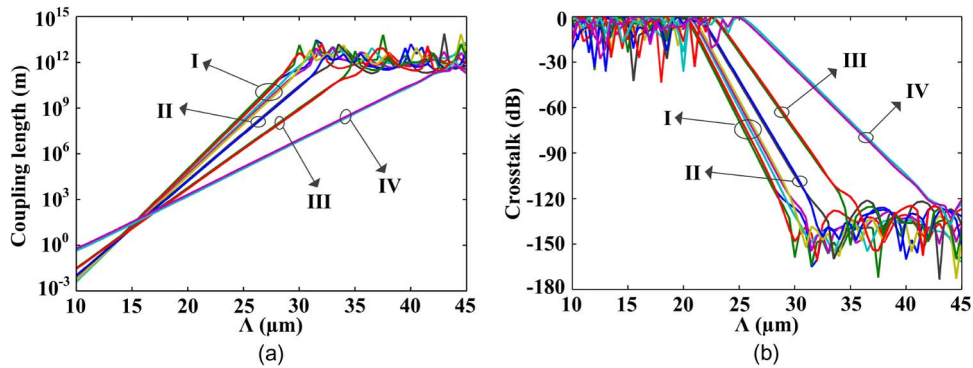


Fig. 4. (a) Coupling length of OAM modes in adjacent rings versus  $\Lambda$ . (b) Crosstalk of OAM modes in adjacent rings versus  $\Lambda$  (propagation length: 100 km).

Fig. 3 depicts calculated spatial phase distributions of the x-component electric field of all 22 modes including 18 OAM ones, i.e.  $TE_{01}$ ,  $TM_{01}$ ,  $HE_{mn}^{even} \pm i \times HE_{mn}^{odd}$  ( $m=1,2,3,4,5,6$ ),  $EH_{mn}^{even} \pm i \times EH_{mn}^{odd}$  ( $m=1,2,3,4$ ). It is noted that  $TE_{01}$  and  $TM_{01}$  feature binary phase distributions of 0 and  $\pi$ .  $HE_{11}^{even} + i \times HE_{11}^{odd}$  and  $HE_{11}^{even} - i \times HE_{11}^{odd}$ , show almost constant phase distributions. In particular, one can clearly see the spiral phase distributions of 18 OAM modes with non-zero topological charge numbers, i.e.  $HE_{mn}^{even} \pm i \times HE_{mn}^{odd}$  ( $m=2,3,4,5,6$ ) and  $EH_{mn}^{even} \pm i \times EH_{mn}^{odd}$  ( $m=1,2,3,4$ ). Similar to few modes in FMF, those 22 modes are orthogonal with each other and can be used for spatial mode-division multiplexing.

After enabling low-level inter-mode crosstalk for multi-OAM modes in each single ring, we further comprehensively analyze the inter-ring crosstalk for the multi-ring structure. In order to determine the  $\Lambda$  necessary for negligible inter-ring crosstalk, we study the power transfer between two adjacent rings. The normalized power transfer between two identical rings is given by  $\sin^2(\pi z / (2L_c))$  with  $z$  being the propagation length and  $L_c$  being the coupling length [21]. The coupled-mode theory method [22], which has the ability to accurately evaluate ultra-long coupling length ( $10^{10}$  m), is adopted to calculate the  $L_c$ . Fig. 4(a) shows  $L_c$  of different OAM modes in adjacent rings as a function

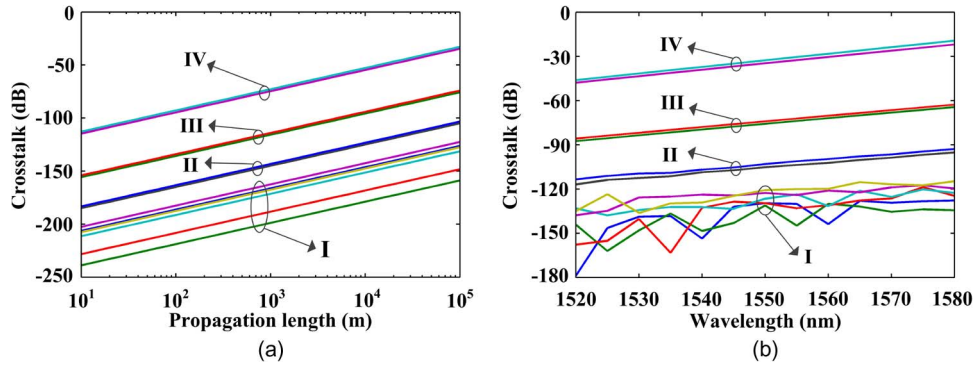


Fig. 5. (a) Crosstalk of OAM modes in adjacent rings versus propagation length. (b) Crosstalk of OAM modes in adjacent rings versus wavelength (propagation length: 100 km).

of  $\Lambda$ . For simple description, we divide 22 modes including 18 OAM ones into four groups, i.e. group I:  $TE_{01}$ ,  $TM_{01}$ ,  $HE_{11}^{even} + i \times HE_{11}^{odd}$ ,  $HE_{11}^{even} - i \times HE_{11}^{odd}$ , and  $HE_{21}$ ,  $HE_{31}$ ,  $EH_{41}$  related OAM modes; group II:  $HE_{41}$  and  $EH_{21}$  related OAM modes; group III:  $HE_{51}$  and  $EH_{31}$  related OAM modes; group IV:  $EH_{41}$  and  $HE_{61}$  related OAM modes. As shown in Fig. 4(a), it is found that  $L_c$  increases with the increase of  $\Lambda$ . This is easy to understand as large separation between adjacent rings can reduce mode overlap and power transfer between adjacent rings, resulting in a long  $L_c$ . One may note the oscillation effect in Fig. 4(a), which can be ascribed to the fact that the adopted coupled-mode theory features its precision limitation when calculating the coupling length longer than  $10^{10}$  m. However,  $10^{10}$  m coupling length is longer enough to ensure a very low inter-ring crosstalk. When  $\Lambda$  is  $30 \mu\text{m}$  and the wavelength is 1550 nm, for the first group I,  $L_c$  has an order of  $10^{10}$  m; while for the last group IV,  $L_c$  has an order of  $10^6$  m. Such phenomenon can be explained with the fact that lower-order modes are confined more tightly than higher-order ones in the ring.

When the propagation length  $z$  is 100 km, Fig. 4(b) plots the inter-ring crosstalk of 22 modes (18 OAM ones) in adjacent rings as a function of  $\Lambda$ . One can clearly see the decrease of inter-ring crosstalk with the increase of  $\Lambda$ . For small values of  $\Lambda$ , the relative small  $L_c$  according to Fig. 4(a) causes rapid oscillation of crosstalk defined by  $10\log_{10}(\sin^2(\pi z/(2L_c)))$ . For large values of  $\Lambda$ , the oscillation of crosstalk is due to limited calculation accuracy of  $L_c$  ( $10^{10}$  m) by coupled-mode theory. When  $\Lambda$  is fixed at  $30 \mu\text{m}$ , the inter-ring crosstalk in adjacent rings for group I is lower than  $-100$  dB, and the maximum inter-ring crosstalk in adjacent rings is about  $-32.8$  dB for  $EH_{41}$  related OAM mode in group IV. Compared with a conventional homogeneous single mode MCF which needs to set the core-to-core distance around  $70 \mu\text{m}$  to obtain a  $-30$  dB inter-core crosstalk for a propagation length of 100 km [21], the compact size of the designed MOMRF structure can be contributed to the high-contrast-index ring configuration and resultant tight mode confinement.

To further assess the performance of the designed MOMRF, we also calculate the inter-ring crosstalk for varied propagation length and wavelength. Fig. 5(a) shows inter-ring crosstalk of OAM modes in adjacent rings as a function of the propagation length. For a 10 km propagation length, the inter-ring crosstalk in adjacent rings is less than  $-90$  dB for OAM modes in groups I, II and III while less than  $-50$  dB for OAM modes in group IV. Lower inter-ring crosstalk can be clearly seen in Fig. 5(a) for shorter propagation length. The low-level inter-ring crosstalk of MOMRF indicates potential use in practical applications, especially suitable for short-distance optical fiber communications (e.g. optical access networks). Even for a 100 km propagation length, the inter-ring crosstalk in adjacent rings is still less than  $-50$  dB for OAM modes in groups I, II and III while less than  $-30$  dB for OAM modes in group IV. Fig. 5(b) shows inter-ring crosstalk of OAM modes in adjacent rings as a function of wavelength under a propagation length of 100 km. Within a wide wavelength range from 1520 to 1580 nm, the inter-ring crosstalk in adjacent rings is less than  $-60$  dB for OAM modes in groups I, II and III while less than  $-20$  dB for OAM modes in group IV. Hence, the MOMRF is also compatible with WDM technique.

The high-contrast-index ring structure with specific types of glass (Schott SF4 and SF2) benefits tight light confinement and large effective refractive index difference of different OAM modes, featuring both low-level inter-ring crosstalk and inter-mode crosstalk in the designed MOMRF. However, the design may pay the cost of relatively large loss. On one hand, it might be practical to use the designed fiber in short-distance applications (1 m ~ 1 km). Under such short distance, the inter-ring and inter-mode crosstalk can be even smaller. On the other hand, the proposed MOMRF design is not limited to these specific materials. Low loss materials might be employed to effectively reduce the propagation loss [8].

Using the designed MOMRF with both negligible inter-ring and inter-mode crosstalk within a wide wavelength range (1520 to 1580 nm), it might be possible to simultaneously transmit 11550 channels (7 rings  $\times$  22 modes  $\times$  75 ITU-grid wavelengths from 1520.25 to 1579.52 nm with 100-GHz spacing) with negligible inter-channel crosstalk, which could increase 11550 times total transmission capacity and 154 times aggregate spectral efficiency compared with a single channel transmission. That is, when using 42.8-Gbaud/s 16-ary quadrature amplitude modulation (16-QAM) signal for each channel [7], 1.98-Pbit/s total transmission capacity and 492.8-bit/s/Hz aggregate spectral efficiency might be available.

#### 4. Conclusion

In summary, we have designed a compact low-crosstalk MOMRF featuring multiple spatial rings and multiple OAM modes in each ring for high-density SDM. It is also compatible with existing WDM technique and advanced multi-level amplitude/phase modulation formats, holding great potential to enable Pbit/s transmission capacity and hundreds bit/s/Hz spectral efficiency. With future improvement, a comprehensive design (materials, geometric parameters) might be considered to further optimize the proposed MOMRF having more rings and each ring supporting more OAM modes over a wider wavelength range (whole C + L bands) with negligible inter-mode and inter-ring crosstalks and low propagation loss.

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