

Disentangling the Frequency Content in Optoacoustics

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Abstract—Signals acquired by optoacoustic tomography systems have broadband frequency content that encodes information about structures on different physical scales. Concurrent processing and rendering of such broadband signals may result in images with poor contrast and fidelity due to a bias towards low frequency contributions from larger structures. This problem cannot be addressed by filtering different frequency bands and reconstructing them individually, as this procedure leads to artefacts due to its incompatibility with the entangled frequency content of signals generated by structures of different sizes. Here we introduce frequency-band model-based (fbMB) reconstruction to separate frequency-band-specific optoacoustic image components during image formation, thereby enabling structures of all sizes to be rendered with high fidelity. In order to disentangle the overlapping frequency content of image components, fbMB uses soft priors to achieve an optimal trade-off between localization of the components in frequency bands and their structural integrity. We demonstrate that fbMB produces optoacoustic images with improved contrast and fidelity, which reveal anatomical structures in in vivo images of mice in unprecedented detail. These enhancements further improve the accuracy of spectral unmixing in small vasculature. By offer-

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ing a precise treatment of the frequency components of optoacoustic signals, fbMB improves the quality, accuracy, and quantification of optoacoustic images and provides a method of choice for optoacoustic reconstructions.

Index Terms—Image reconstruction, photoacoustic tomography, image enhancement, image quality improvement.

I. INTRODUCTION

N CONTRAST to ultrasonography, optoacoustic (OA) imaging systems typically generate acoustic signals with a broadband frequency content due to the ultra-short illumination pulses [1]–[5]. The broad frequency content carries information about structures on different physical scales (i.e., size). Therefore, advanced OA systems use broadband acoustic detectors to ensure that no structural information is lost. Despite the rich information that is contained in the frequency spectrum, typical OA reconstructions do not consider the particular dependencies of image features on frequency. For example, the power of the OA signals scale with the size of the source, resulting in a frequency dependent signal-to-noise ratio (SNR) and images where small structures may be obscured by the high SNR of low frequency contributions. Processing and rendering all frequencies together therefore bias the visual perception of an image towards larger structures. Furthermore, the sensitivity fields of broadband ultrasound detectors employed in state-of-the-art OA systems are also frequency dependent [6], [7]; lower frequencies sample larger volumes, which, in the case of linear ultrasound arrays, may appear as out-of-plane signals in the reconstructed image [7]; and further obscure features formed by higher frequencies.

Current OA image reconstruction techniques do not accurately extract all the information contained in broadband OA signals. Common filtered back-projection methods [8] act as high-pass filters on the image suppressing signals from bulky absorbers, while delay-and-sum algorithms [9] and model-based algorithms [10], [11] treat all frequencies equally, thereby penalizing the high frequencies and leading to less accurate rendering of smaller structures. Both methods result in an oxymoron; they afford visually pleasing images by penalizing either low or high frequency content and ultimately reducing image fidelity.

Separate reconstruction of different frequency bands has been considered in Ultra-broadband Raster-Scan Optoacoustic Mesoscopy (RSOM) [12], [13] and in OA microscopy [14]. However, simple separation of the frequency bands using signal processing filters neglects the entanglement, i.e., superposition of the broadband frequency content of signals that are generated by structures of different sizes [2] which may result in artefacts (e.g., ring artefacts) that can be further amplified by limited view detection [15], [16] or insufficient spatial sampling [16], [17]. Moreover, model-based reconstruction techniques for OA tomography systems have yet to account for the abovementioned dependence of image content on the recorded acoustic frequencies. Out-of-plane signals have been separated from in-plane signals by axially displacing the transducer array and by de-correlating images acquired at different out-of-plane positions with the in-plane image [18], [19]. In another study [20], the probe's trajectory was incorporated into a two-stage iterative 3D model-based reconstruction leading to significant out-of-plane artefact reduction. However, such approaches are impractical since they require the displacement of the transducer and do not consider the frequency-dependence of the detector's sensitivity.

In this work, we propose a frequency-band separated modelbased (fbMB) reconstruction framework for OA tomography that untangles the overlapping frequency content of image components to improve resolution and overall image fidelity. The fbMB method reconstructs multiple images such that each is a partial model-based reconstruction of a portion of the signal and that these images sum up to a reconstruction of the full OA signal data. fbMB imposes soft priors on the frequency content of the signals underlying the different image components to allow integration of frequencies from other bands if required by the model, thereby achieving an optimal trade-off between structural fidelity of these components and localization of the corresponding signals in separate frequency bands. Lastly, fbMB imposes non-negativity constraints on all image components to ensure that artefacts in one component cannot be compensated by negative contributions in others. Since out-of-plane signals have prevalent low frequency content in bulk tissue, by effectively separating the frequency components using fbMB, the effect of out-of-plane signal can be partially decoupled from the weak signal from small structures otherwise obscured [7]. Furthermore, fbMB can be extended to any image reconstruction problem that is based on a linear model of physical phenomena and the computational complexity only increases linearly with the number of components compared to a standard model-based algorithm. We demonstrate on both a synthetic phantom and real OA data that, with a suitable choice of filters depending on the biological application, the new method can efficiently separate structures of different physical scales. Using a dataset of 533 in vivo multispectral OA tomography (MSOT) images of different anatomical sections of mice, we show that the new method generates OA images with lower reconstruction residuals and higher structural similarity index values compared with simple filter techniques, and improved image contrast and resolution compared with a standard model-based algorithm. The fbMB method implements a unique multifrequency-band contrast in MSOT to complement its volumetric imaging, real-time acquisition, and multispectral contrast capabilities. By rendering the rich, high-fidelity OA content from biological structures on all scales, fbMB could expand the applications of MSOT in both preclinical and clinical medicine.

II. METHODS

A. Linear Model of OA Signal Acquisition

In an acoustically homogeneous medium, the propagation of the optoacoustically induced pressure wave p(r,t) is described by the wave equation [10]:

$$\frac{\partial^2 p(\mathbf{r},t)}{\partial t^2} - c^2 \nabla^2 p(\mathbf{r},t) = \Gamma \frac{\partial H(\mathbf{r},t)}{\partial t}, \qquad (1)$$

where *c* is the speed of sound in the medium, \tilde{A} is the dimensionless Grüneisen parameter, which is assumed constant, and *H* is the energy absorbed in tissue per unit volume and per unit time, which is the source for OA fields. For pulsed laser illumination (thermal and stress confinement conditions [21]), the temporal dependence of *H* can in the acoustic regime be approximated δ -distribution, so that $H(r, t) = H_r(t)\delta(t)$.

The solution of Eq. 1 can be described in terms of Green's function for the wave equation [2], [22]. Under the assumption that an object Ω is an OA source, the solution of the wave equation for object Ω can be estimated by assuming that each point r' in the object is the emitter of OA waves, given by the Green's function G, which is given by:

$$G(\mathbf{r},\mathbf{r}',\mathbf{t}) = \frac{\delta\left(t - \frac{|\mathbf{r} - \mathbf{r}'|}{c}\right)}{4\pi |\mathbf{r} - \mathbf{r}'|}.$$
(2)

Eq. 2 represents the elementary wave generated at \mathbf{r}' at t = 0, propagating outwards in a spherical shell. The solution to Eq. 1 at a given point \mathbf{r} can be written as:

$$p(\mathbf{r}, \mathbf{t}) = \frac{\Gamma}{4\pi c^2} \frac{\partial}{\partial t} \left[\int_{\Omega} H_r(\mathbf{r}') \frac{\delta\left(t - \frac{|\mathbf{r} - \mathbf{r}'|}{c}\right)}{|\mathbf{r} - \mathbf{r}'|} d\mathbf{r}' \right], \quad (3)$$

where the integral is estimated along the whole object. Eq. 3 represents the OA statement of the Huygens Principle, since it describes the OA pressure field generated by an object Ω at point **r** as a superimposition of elementary waves generated at points **r'** on the source.

Since light attenuation primarily limits image penetration depth in the considered frequency range (<15 MHz), frequency-dependent acoustic attenuation can be neglected and is not included in the model [23].

B. Model-Based Optoacoustic Reconstruction

Several algorithms have been suggested for the inversion of Eq. (3), i.e., for the estimation of the initial pressure p_0 or H_r , given the OA signal p(r,t) at the detector locations r. Back-projection and model-based algorithms are widely used for OA image formation. While the former is commonly used for its simplicity, the latter has been suggested as more precise reconstruction algorithms for accurate quantitative functional and molecular imaging in OA [11], [24].

Standard model-based algorithms reconstruct OA images by minimizing the difference between the measured OA signal and the signal theoretically predicted by the forward model. Typically, the broadband OA signal is entirely projected into one single image which contains structural information ranging from millimeter to micrometer resolution.

The discretization of Eq. (3) leads to a matrix equation of the form of [10]:

$$p = Mx, \tag{4}$$

where p is the broadband pressure signal recorded; x is the unknown distribution of optical absorption; and M is the linear operator that maps the unknown initial pressure to the recorded signal. The inversion of Eq. (4) is achieved by minimizing the squared error:

$$x^* = \underset{x}{\arg\min} \|p - Mx\|_2^2.$$
(5)

A common problem when using standard model-based inversion is the appearance of negative values due to the bipolarity of the OA signal, which have no physical meaning since optical absorption can only be positive or zero. Furthermore, the OA inversion problem may be ill-posed leading to the appearance of additional spurious negative values introduced during the inversion process as part of the minimization. For these reasons, non-negative constraints are included in the algorithm to guarantee physical integrity of the solution [25], i.e., positive optical absorption:

$$x^* = \underset{x \ge 0}{\arg\min} \|p - Mx\|_2^2.$$
(6)

In contrast to unconstrained inversion, Eq. (6) cannot be solved analytically, and only iterative methods are applicable. Furthermore, since the problem in Eq. (6) is ill-posed and leads to inversion uncertainty, it requires additional regularization to impose additional constraints.

Thereby, Eq. (6) is modified by adding a Tikhonov regularization term, i.e.

$$x^* = \underset{x \ge 0}{\arg\min} \|p - Mx\|_2^2 + \lambda \|Lx\|_2^2,$$
(7)

where λ is the regularization parameter, and $\|\cdot\|_2$ is the L^2 -norm. The matrix L can be selected as the identity matrix, which gives preference to solutions with a small norm, and penalizes any content in the data that is not in agreement with the model, like noise. Regularization is required to achieve a stable and unique solution.

The regularized problem in Eq. (7) can be formulated to the same form as Eq. (5):

$$x^{*} = \underset{x \ge 0}{\operatorname{arg\,min}} f(x) = \underset{x \ge 0}{\operatorname{arg\,min}} \left\| \tilde{p} - \tilde{M}x \right\|_{2}^{2}, \tag{8}$$

with

$$\tilde{p} = \begin{pmatrix} p \\ 0 \end{pmatrix}$$

and

$$\tilde{M} = \begin{pmatrix} M \\ \lambda^{1/2}L \end{pmatrix}$$

In this work, the Projected Conjugate Gradient [24] is used as non-negative least square (NNLS) methods to solve Eq. (8). For standard model-based reconstruction, the Tikhonov regularization parameter λ in Eq. 7 is tuned by considering the L-curve, i.e., the plot of the solution norm $||Lx||_2$ versus the residual norm $||p - Mx||_2$. The optimal trade-off for λ is achieved close to the corner of the L-curve.

C. Frequency-Band Model-Based Reconstruction (fbMB)

The newly proposed frequency-band model-based reconstruction (fbMB) framework allows us to decompose the OA signal in different components and reconstruct multiple nonnegative images with scale specific contrast. Soft priors on the frequency content of signals generated on different scales steer the acoustic spectrum towards higher or lower frequencies, while allowing overlaps when required by the system model. Thus, for multiscale reconstruction, the matrix equation in Eq. (4) is modified as follows:

$$p = M \left(x_1 + \dots + x_n \right), \tag{9}$$

where *p* is the broadband pressure signal recorded; and x_1^*, \ldots, x_n^* are the unknown distributions of optical absorption at *n* scales.

D. Soft Priors on Frequency Bands

In the framework of L^2 regularization, a priori information about the tissue being imaged can be included [26] to ensure convergence of the reconstruction algorithm to the correct optical absorption distribution on different scales. For this reason, soft priors on the frequency band separation are added into the inversion. The priors are considered "soft" because they do not force a rigid frequency band separation, instead they allow overlap between frequency bands to preserve the physical accuracy of the solution. The regularized inversion problem with soft priors can be written as:

$$(x_1^*, \dots, x_n^*) = \underset{(x_1, \dots, x_n \ge 0)}{\arg \min} \|p - M (x_1 + \dots + x_n)\|_2^2 + \lambda \|L (x_1 + x_2 + \dots + x_n)\|_2^2 + \eta \mu_1 \|(id - F_1) M x_1\|_2^2 + \dots + \eta \mu_n \|(id - F_n) M x_n\|_2^2,$$
(10)

where F_1, \ldots, F_n are the *n* band-pass filters, and $\eta, \mu_1, \ldots, \mu_n$ the regularization parameters for the soft priors such that $\mu_1 + \cdots + \mu_n = 1$.

The regularized problem in Eq. (10) can be formulated in the same form as Eq. (8):

with

$$\tilde{p} = \begin{pmatrix} p \\ 0 \\ \vdots \\ 0 \end{pmatrix}$$

and \tilde{M} given by:

$$\begin{pmatrix} M & \dots & M \\ \lambda^{1/2}L & \dots & \lambda^{1/2}L \\ (\eta\mu_1)^{1/2}(id-F_1)M & 0 & \dots & 0 \\ 0 & \ddots & \vdots \\ \vdots & \ddots & 0 \\ 0 & \dots & 0 & (\eta\mu_n)^{1/2}(id-F_n)M \end{pmatrix}$$

The Projected Conjugate Gradient [25] is used as nonnegative least square (NNLS) methods to solve Eq. (11).

The Tikhonov regularization parameter λ in Eq. (10) is chosen in agreement with the one selected for standard model-based reconstruction. The regularization parameters $\eta, \mu_1, \ldots, \mu_n$ in fbMB in Eq. (10) are selected by considering the reconstruction residuals curves, i.e., the plot of the residual norm $\|p - Mx\|_2$ for different values of the regularization parameters. The values are tuned as follows: first, the values of μ_i are fixed and set equal (i.e., $\mu_1 = 0.5$, $\mu_2 = 0.5$ for twoband model-based reconstruction [2bMB]) and the residual norms for different values of η are plotted with the regularization parameter η chosen at the corner of the curve. After tuning the values of η , the regularization parameters μ_1, \ldots, μ_n are selected according to the configuration that gives the lowest residual norm.

Numerical inversions are usually computationally demanding and imposing the additional non-negative constraint increases the inversion time. However, the computational complexity of fbMB is increased only by a constant factor (linear in the number of components) compared to standard modelbased reconstruction, since the model needs to be evaluated once for every component x_i and the filters need to be applied.

E. Filter Selection for the Soft Priors

Standard Butterworth band-pass filters are used as soft priors F_1, \ldots, F_n in (Eq.10). The low and high pass cut-off frequencies and the relative bandwidth $BW_{\%}$ are chosen following the Shannon-Nyquist Theorem [27] and in agreement with Omar *et al.* [12] such that:

$$BW_{\%} = \frac{BW_1}{f_{c,1}} = \frac{BW_2}{f_{c,2}} = \frac{BW_3}{f_{c,3}} = \cdots$$

where BW_n is the bandwidth and $f_{c,n}$ the central frequency of the filter F_n , which are defined as the absolute difference and the mean value of the low pass and high pass cut-off frequencies, respectively. Therefore, after selecting the value of the relative bandwidth $BW_{\%}$ and the first high pass cut-off frequency $f_{H,n}$, the next high pass cut-off frequency $f_{H,n+1}$ can be calculated as:

$$f_{H,n+1} = \frac{2 + BW_{\%}}{2 - BW_{\%}} f_{H,n}$$

In the case of two-band decomposition, band-pass filters with frequency bands 100 kHz to 1.23 MHz and 1.23 to 15.17 MHz are chosen in the soft priors, with a value of $BW_{\%}$ equal to 1.7. For three scale decomposition, band-pass filters with frequency bands 100 to 500 kHz, 500 kHz to 2.5 MHz,

and 2.5 to 12.5 MHz are selected, for a value of $BW_{\%}$ equal to 1.33.

Notably, the fbMB method is flexible because it is robust with respect to the choice of the filters used in the soft priors.

F. MSOT System Setup

OA measurements were conducted using a commercially available, real-time, multispectral optoacoustic tomographic (MSOT) small animal scanner (inVision 256-TF, iThera Medical, Munich, Germany). The system features 360° ring illumination and 270° acoustic detection. A tunable OPO laser provides excitation pulses with a duration of 5-10 ns in the wavelength range of 680-980 nm at 10 Hz repetition rate (InnoLas Laser, Germany). For tissue illumination, 10 arms of a fiber bundle are attached to both sides of the transducer and arranged at an angle of 13° to the image plane. The laser fluence on the surface of the imaged objects was below $20 mJ/cm^2$, thereby within the American National Standards Institute (ANSI) safety limit for laser exposure. The acoustic detection includes 256 cylindrically focused transducers (Imasonic SAS, France) with 5 MHz central frequency and -6 dBbandwidth of 150% arranged in a circle of 40 mm radius to surround the sample. Fig. 1a reports the simulated electrical impulse response in receive-only mode in the time and frequency domain for a single transducer obtained with the KLM (Krimholtz, Leedom and Matthaei) model [28]-[30].

Each focused transducer is 0.735×15 mm in size with 0.1 mm inter element spacing and 37 mm elevational radius. A 256-channel analog-to-digital converter is used to digitize the transducer signals at a sampling rate of 40 MS/s with an amplitude resolution of 12-bits.

G. Experiments

OA images of an excised kidney from a nude mouse (4 weeks old) were acquired to demonstrate the structures enhancement of the new proposed algorithm fbMB in an organ with well-defined features of varying scales. Ten minutes after the animal euthanasia the kidney was excised and embedded in a supporting turbid agar gel in a cylindrical mold (12 mm in diameter and 2.5 cm in height). The agar gel was made by mixing 1.6% w/v agar gel (Agar for microbiology, Fluka analytical) with 0.8% v/v Intralipid 20% (Sigma).

The multiscale capabilities of the new algorithm were tested with an *in vivo* mouse dataset, including 533 OA images from different anatomical sections, from the brain to the lower abdomen.

2D OA images were continuously acquired at a single wavelength (800 nm) for anatomy visualization, or at multiple wavelengths (31 wavelengths, from 680 to 980 nm with a step size of 10 nm) for spectral unmixing quantification.

For 3D whole body imaging, 2D images of consecutive anatomical sections were collected with 200 μ m resolution between adjacent frames and then stacked together for volumetric imaging. Animal procedures were approved by the Government of Upper Bavaria. Nude mice (3-4 weeks old) were anesthetized and placed lying prone in the animal holder such that the transducer array faced the ventral side. After data acquisition, the mice were euthanized by cervical dislocation.

H. Validation

For algorithm validation, the performance of fbMB was compared with standard model-based reconstruction and simple filtering techniques.

In the case of standard model-based reconstruction, the acquired OA signals are filtered prior to reconstruction by applying a Butterworth bandpass filter in the frequency range between 0.1 and 13.3 MHz to reject signals beyond the sensitivity of the transducers.

For simple filtering techniques, i.e., Butterworth and Wavelet, the OA signals are divided into different frequency bands by applying a bank of band pass filters and reconstructing each frequency band separately with standard model-based algorithm. In the case of simple Butterworth filtering, the band-pass filters are chosen identically to the ones selected in the soft priors (see Methods, Section E). For the simple Wavelet filtering technique, the Matlab functions swt and iswt are used for two and three scale decomposition. The Daubechies mother wavelet with two vanishing moments 'db2' was selected as previously reported [31]. The advantage of using Wavelet decomposition over standard filters is that it does not require the a priori knowledge of the frequency information contained in the signal and guarantees optimal temporal and frequency resolution for each band.

The efficiency of fbMB to separate different OA components was quantified against standard filtering techniques (i.e., Butterworth or Wavelet bandpass filters) in terms of physical and structural accuracy considering standard modelbased reconstruction as ground truth. The proposed method is physically accurate, in the sense that OA images at different bands are related to the corresponding OA signals via the physical model employed in the method, while the sum of the OA signals corresponding to the components explains the acquired signal data. For structural accuracy we indicate the capability of the algorithm to compensate for potential ripples and artefacts generated by the frequency band separations.

Herein, we use the "normalized reconstruction residuals" to quantify the physical accuracy of reconstructions from fbMB and standard filtering techniques relative to a standard modelbased algorithm. First, we evaluate the relative error r for each reconstruction, defined as:

$$\mathbf{r} = \frac{\|p - Mx\|_2^2}{\|p\|_2^2}$$

where x is the reconstructed image, M is the forward model for the specific model-based reconstruction, p is the recorded pressure signal, and $\|\cdot\|$ is the 2-norm. We normalize the relative errors obtained for fbMB and standard filtering techniques by the relative error r0 of standard model-based reconstruction to obtain the normalized reconstruction residuals r/r0.

Moreover, we use the structural similarity index (SSIM) [32] between the reference images (reconstructed with standard model-based) and the images obtained with the two different methods, i.e., fbMB and standard filtering techniques (sum of all components), to evaluate the structural accuracy.

Notably, images reconstructed with 2bMB and standard filtering techniques (and relative quantification metrics) are always compared to the ones obtained with a standard modelbased algorithm, which in this paper is taken as ground truth.

To quantify image quality improvement of fbMB against standard model-based reconstruction, two different metrics are proposed: image entropy, as an objective indicator of the image information content; and perception-based image quality evaluator (PIQE) to account for human visual system perception [33]. The two indices were estimated on the threechannel RGB images.

I. Visualization

fbMB decomposes the original acquired OA signal into its components without modifying the signal energy in the different frequency bands. Hence, the blend (sum) of the grayscale images of the different components still results in an image with poor contrast from small structures and visual perception biased towards the low frequency components, as is observed in model-based reconstruction.

Therefore, to visualize the multiscale information content with high contrast, the different components were first colorcoded (i.e., images are converted from grayscale to RGB) and then blended (summed up). The color coding for the different frequency bands was as follows: since the visual human perception is more sensitive to yellow and green colors, these colors were used to render the high frequency components which have a low SNR. To balance the high SNR and image intensity of the low frequency components, blue and violet colors (which human eyes are less sensitive to) were used.

To adjust image contrast, since OA images are characterized by a high dynamic range of intensity values due to inhomogeneous light deposition inside the tissue (fluence), a histogrambased thresholding method was applied to all OA images by removing the 0.5% highest and 0.02% lowest pixel values. The threshold values were chosen empirically to lower the image dynamic range and improve the perceptual information content from deep tissue.

III. RESULTS

The proposed fbMB method separates OA signal contributions from different frequency bands by integrating the filtering process with soft priors into the reconstruction model, and by applying non-negativity constraints on all components. In the resulting multiscale images, anatomical structures of different sizes are more accurately represented. An illustrative example of two-band model-based reconstruction (2bMB) is provided in Fig. 1b. The 2bMB reconstruction is applied to the OA signal acquired by the system and generates OA images of specific frequency band components: a low frequency image (Band 1, Image domain in Fig. 1b) containing mainly signals from larger structures and a high frequency image (Band 2, Image domain in Fig. 1b) corresponding to smaller structures. OA images with multiscale contrast are generated by colorcoding and blending the different components (2bMB, Image domain in Fig. 1b). c (2bMB, Signal domain in Fig. 1b). In the following, we report our findings in phantoms and in ex vivo



Fig. 1. Frequency content disentanglement in OA imaging and fbMB reconstruction. a) Transducer electrical impulse response (EIR) in receive-only mode in the time and frequency domain for a single detector using the Krimholtz, Leedom and Matthaei (KLM) model. b) Schematic of the twoband model-based reconstruction algorithm (2bMB). c) A synthetic phantom with well-defined features of varying size. Reconstructed OA images of the phantom for d) two-band model-based and e) standard model-based reconstruction (MB). The 2bMB image was obtained by color-coding and blending the different frequency band components. The red arrows in the magnified ROIs indicate a small structure enhanced with the new method. f) Mean power spectra of the OA signals corresponding to the two different frequency band components of the phantom showing frequency overlaps between the components due to soft priors in the reconstruction. g) Ex vivo mouse kidney embedded in agar and magnification of the selected anatomical cross section in the middle segment. OA images of the Kidney cross section reconstructed using h) two-band model-based and i) standard model-based reconstruction. j) Mean power spectra of the OA signals corresponding to the two frequency band components. Visible anatomical details in the vascular network of the excised kidney for 2bMB: main renal vessel (RA/V), interlobal (IV), arcuate (AV), renal pelvis (RP), and cortical (CV) vessels. k) Transverse ex vivo cryosection of the mouse kidneys section used for OA. In vivo OA images of the mouse kidney section reconstruction. Kidney (K), aorta (AO), spleen (SP) and spinal cord (SC). n) OA frequency content for the corresponding frequency band components for two-band decomposition.

and in vivo mouse data. The data are supported with measures of merit, such as the reconstruction residuals, the SSIM index, the image entropy and the Perception-based Image Quality Evaluator (PIQE).

Section A details the effectiveness of the proposed method to separate different frequency band components in OA imaging. Sections B and C describe the validation of the method against standard signal filtering and simple modelbased reconstruction. Section D reports spectral unmixing results to demonstrate multiscale quantification of specific chromophores.

A. Disentanglement of the Frequency Content by fbMB

The capability of the algorithm to generate images with band-specific contrast is first demonstrated on a controlled synthetic phantom with well-defined features of different sizes (Fig. 1c). The phantom features a network of vessel-like structures with diameters ranging from 1.3 mm to 240 μ m, which are embedded in a circular absorbing background that is 1.7 cm in diameter and absorbs 10 times less than the vessel-like structures (see Methods section). We tested two-band decomposition by applying a 2bMB algorithm. For 2bMB, two band-pass filters with frequency bands 100 kHz to 1.23 MHz and 1.23 to 15.17 MHz were chosen for the soft priors, with 1.7 $BW_{\%}$ (see Methods section).

Fig. 1d shows images of the phantom that were reconstructed by the two-band model-based (2bMB) algorithm. The new algorithm successfully decomposes images into components on different physical scales. Low frequency images (Fig. 1d, Band 1) contain mainly signals from larger structures ranging from 1.6 cm to 600 μ m in diameter, while high frequency images (Fig. 1d, Band 2) correspond to small structures that are less than 600 μ m across. Color-coding and blending the frequency band components generates OA images with multiscale contrast as reported in the Methods section (Fig. 1d, 2bMB). Compared with standard model-based reconstruction (MB in Fig. 1e), 2bMB affords a more accurate image and improved visualization of small features (red arrows in the ROIs).

Fig. 1f reports the mean power spectra of the OA signals (i.e., square root of the average power spectra density of the detected acoustic signals from the 256 transducers) generated by the structures on different scales for the 2bMB algorithm, which demonstrate that the frequency contents of the different reconstructed components overlap significantly. This finding confirms that the new method achieves a disentanglement of different-sized structures. The separation of this overlapping content is enabled by the soft priors on the filtering process in the reconstruction, which allows the components to integrate frequencies from other bands if the model requires it (see Methods section).

Next, the algorithm was applied to OA images of an ex vivo mouse kidney (Fig. 1g) to demonstrate the ability of frequency band contrast to reveal structures and vessels of different sizes in tissue. Fig. 1h shows an OA image after decomposition into two bands. As with the phantom, the algorithm efficiently separated the different anatomical components in the kidney. Low frequency components contain primarily OA signals from the organs and large vessels. High frequency components have better in-plane focus and show small vessel networks with high accuracy. Furthermore, as shown in Fig. 1j the OA spectra of the different bands overlap in the frequency domain, again confirming the effect of the soft priors on the reconstructed images, which enable each component to integrate frequencies from other bands to assure consistency with the underlying physics. Blending the two bands (2bMB in Fig. 1h) afforded OA images in which fine details, such as small vasculature inside bulk tissue, were rendered with significantly higher contrast than possible with standard reconstruction (Fig. 1i).

The frequency disentanglement approach was then applied to reconstruct an image of a kidney section in a live mouse to enhancement *in vivo*. Fig. 1k shows the transverse cryosection of an ex vivo mouse kidneys section approximately corresponding to the anatomical section selected for in vivo OA imaging. Fig. 11 shows the different OA frequency band components of the in vivo mouse kidney section, obtained by applying 2bMB. The low-frequency bands contain signals from organs such as the kidneys (K) and spleen (SP), or large structures such as the abdominal aorta (AO) and the spinal cord (SC). The high-frequency components contain signals from small vessels such as the microvasculature in the kidney, the splenic vessel (SPV), and the hepatic vessels (HEV). As expected, the OA signals from these structures again overlap in the frequency domain (Fig. 1n), supporting the physical fidelity of the reconstructed in vivo images. Finally, the OA images obtained by blending the different frequency band components (2bMB in Fig. 11) visualize with high contrast the entire OA information content, which is

not possible with the standard model-based reconstruction (MB in Fig. 1m).

Finally, we tested three-band model-based (3bMB) reconstruction to evaluate the effect of a finer frequency band decomposition on the image contrast. For 3bMB, three bandpass filters with frequency bands 100 to 500 kHz, 500 kHz to 2.5 MHz, and 2.5 MHz to 12.5 MHz were selected for the soft priors, with 1.33 $BW_{\%}$ (see Methods). Similar to 2bMB, 3bMB successfully separates the different OA frequency band components in the images. Low frequency images contain signal from bulky absorbing tissue and large structures, while the high frequency images contain signals from smaller structures (Fig. 2a,c,e). Furthermore, as shown in Fig. 2b,d,f, the individual bands overlap consistently in the frequency domain due to the soft priors in the reconstruction.

To demonstrate that, depending on the biological application, 3bMB can improve the visualization of small vasculatures compared with 2bMB, the kidney region was specifically selected due to its well-defined features of varying scale. By increasing the number of bands from two to three, we observed that the high frequency structures are further decoupled from the middle and low frequencies, thus demonstrating that by finer decomposition of the signal, the image resolution further increases, and the visual perception of small structures improves. For example, the three-band reconstruction of the ex-vivo kidney section in 3bMB in Fig. 2c reveals further anatomical details of the vascular network of the kidney with high accuracy. An example is the main renal vessel (RA/V) entering the kidney and progressively branching into the interlobal (IV), arcuate (AV), and cortical (CV) vessels, which cannot be identified in the 2bMB image (2bMB in Fig. 1g) or the standard model-based reconstructed image (MB in Fig. 1h). 3bMB thus allows detailed visualization of the entire blood supply in the kidney.

Notably, the appearance of low frequency diffusive components in the high frequency images (Band 3 in Fig. 2a, c, e) is a demonstration of the softness of the priors in the fbMB which allows the inclusion of low frequencies for high frequency bands (if necessary) to be consistent with the mode. Indeed, the inclusion of low frequency components in the high frequency band (Band 3 in Fig. 2b, d, f) is a result of the trade-off between frequency localization and model consistency.

B. Comparison of 2bMB Against Simple Techniques

Compared to standard filtering methods, the proposed algorithm affords images with significantly higher physical and structural accuracy. If an image is decomposed into a superposition, each component should comply with the underlying physics. We can quantify the physical accuracy by comparing the estimated residual errors, i.e., the difference between the recorded OA signals and the model of the imaging system applied to the reconstructed image, where the model components should produce an image without introducing artefacts (e.g., ripples at edges). Structural fidelity between two images can be quantified using the SSIM index, which was used herein to compare the output of the proposed algorithm to that of standard model-based reconstruction. In this way, we validated the physical and structural integrity of the fbMB reconstruction



Fig. 2. 3bMB reconstruction. a) Three-band decomposition of OA images of the synthetic phantom from Fig. 1b. The 3bMB images were obtained by color-coding and blending the three components. The red arrows in the magnified ROIs indicate a small structure enhanced with the new method. b) Mean power spectra of the OA signals of the phantom for three different frequency band components with frequency overlaps between the components due to soft priors in the reconstruction. c) 3bMB reconstructions of the excised kidney cross section shown in Fig. 1f. Visible anatomical details in the vasculature network of the kidney for 3bMB: main renal vessel (RA/V), interlobal (IV), arcuate (AV), and cortical (CV) vessels. Renal pelvis (RP), medullary pyramids (MP). d) Mean power spectra of the OA signals corresponding to the three frequency band components. e) In vivo 3bMB reconstructions of the mouse kidney section of Fig. 1j. f) OA frequency content of the three frequency band components.



Fig. 3. Comparison of 2bMB against simple filtering techniques. a) Reconstruction of an in vivo mouse liver section using 2bMB (top), simple Butterworth (middle), and simple Wavelet (bottom) filtering techniques. b) Normalized reconstruction residuals and c) SSIM index of 2bMB and simple filtering techniques, compared to standard model-based reconstruction.

against standard signal filtering with Butterworth filters and Wavelet filters (Fig. 3) on a dataset of 533 OA images from different anatomical sections.

Fig. 3a displays representative multiscale OA images from a mouse liver section obtained with 2bMB reconstruction and model-based reconstruction after the application of Butterworth and Wavelet bandpass filters. All three methods separate different frequency bands of OA contrast in the liver section, highlighting bulky tissue (band 1) or vasculature (band 2). However, as shown in Fig. 3b, 2bMB generates OA images with lower normalized reconstruction residuals (mean of 1.3) compared to Wavelet (mean of 4.7) and Butterworth (mean value of 6.8). The residuals are normalized relative to those obtained with standard model-based reconstruction (see Methods section). Therefore, the new proposed decomposition approach has only a small regularizing effect when compared



Fig. 4. Comparison of 2bMB against standard MB. a) Maximum Intensity Projection (MIP) images of volumetric OA mouse data in the YZ and XZ planes for the two frequency band components obtained with 2bMB reconstruction. b) Comparisons of 2bMB reconstructions to standard model-based (MB) reconstructions for both volumetric data (left) and 2D sections (right) of the mouse. Image quality indicators c) entropy and d) Perception-based Image Quality Evaluator (PIQE). Transverse whole mouse sections containing the: 1 brain, 2 neck, 3 lungs, 4 liver, 5 kidneys, 6 colon, 7 lower abdomen. Anatomical abbreviations in alphabetical order: aorta (AO); bladder (BI); colon (C); common carotid (CC); common carotid/jugular (CC/J); confluence sinus (CS); dorsal artery and vein (DA/V); deep cerebral vessel (DCV); dorsal intercostal artery and vein (DIA/V); external jugular (EJ); facial artery (FA); femoris muscle (FM); intestine (I); ilica artery and vein (ILA/V); liver left (LL); liver right (LR); lungs (Lu); middle caudal artery and vein (MCA/V); mandibula-facial arteries and veins (MFA/V); masseter muscle (MM); pectoral muscle (PM); portal vein (PV); rib (R); right kidney (RK); splenic artery and vein (SA/V); spleen (SP); straight abdominal muscle (SAM); spinal cord (SC); superficial epigastric cranial artery and vein (SECA/V); trachea (T); trapezius muscle (TM); transverse sinus (TS); and vena cava (VC).

to standard model-based reconstruction, while the other methods deviate from the data significantly. Hence, the new method assures a solution with the highest physical accuracy, wherein the sum of the different OA components most accurately reflects the original OA signals.

In addition, as shown in Fig. 3c, the new algorithm generates images with the highest SSIM index measure of 0.6 when compared to the reference reconstruction, while the filtering techniques achieve values of 0.39 (Wavelet) and 0.21 (Butterworth).

Therefore, integrating the filtering process with soft priors into the inversion assures that no artefacts are generated by the decomposition and that the integrity of the structure being imaged is better preserved. The still low value of structural similarity of 0.6 for the 2bMB reconstruction is due to the regularizing effect of the frequency band decomposition.

C. Comparison of 2bMB Against Standard Model-Based Reconstruction

Fig. 4 demonstrates the effectiveness of 2bMB to separate anatomical structures on different scales in *in vivo* whole-body images of a mouse.

The improved contrast of 2bMB image (obtained by colorcoding and blending images at different frequency bands) was quantified against a standard model based reconstructed image (MB) using two measures of merit: the image entropy and the Perception-based Image Quality Evaluator (PIQE).

Fig. 4a shows the maximum intensity projection (MIP) images of the mouse in the YZ and XZ planes for twoband decomposition (Band 1 and Band 2) reconstructed with the 2bMB algorithm. As expected, the low frequency image contains OA signals from large anatomical structures, such as organs, muscles, and large vessels, while the high frequency image shows the vasculature network inside of the mouse.

Several anatomical structures can be identified in the lowfrequency band image (blue), including: the carotid artery and the jugular vein in the mouse neck; the aorta and the vena cava running parallel in the mouse abdomen, branching into the iliac artery/vein in the lower abdomen; the trapezius muscle in the upper part of the spine; the femoral muscle in the lower extremities of the mouse; the kidneys; and the liver lobes in the abdomen. Visible in the high-frequency band image (yellow) are the dorsal intercostal veins and arteries between the ribs, which provide blood supply in the thoracic wall, and the superficial epigastric artery and vein,



Fig. 5. Spectral linear unmixing of in vivo mouse liver and kidneys sections. a) Absorption spectra of oxygenated hemoglobin (HbO₂) and deoxygenated hemoglobin (Hb) in the range 680 – 980 nm. b) Linear spectral unmixing of Hb and HbO₂ in mouse liver and kidneys sections obtained from OA images reconstructed with MB and 2bMB. Magnification of two ROIs in the left lobe of the liver and in the kidney-spleen region.

both cranial and inferior. Fig. 4b shows the image quality improvement of 2bMB in both 3D and 2D mouse sections, compared to standard model-based reconstruction (MB). The 2bMB images, obtained by color-coding and blending the different bands (Fig. 4a), display more anatomical details and broadband OA contrast than OA images from standard MB reconstruction, which appear blurred and lack contrast for small structures. For example, the dorsal artery and vein are clearly visible in the 2bMB images but hidden in the MB images due to the proximity of the liver and lungs. Fig. 4c,d report the values of entropy and PIQE estimated for 533 in vivo OA images from different mouse anatomical sections, which quantify the image quality improvement of 2bMB compared to standard MB reconstruction in a large dataset. The OA images reconstructed with the proposed method exhibit increases in entropy of 50%, higher visual contrast, and a reduction in the PIQE index of 19%, implying an overall improved visual image quality.

D. Spectral Unmixing

2bMB also improves image quantification via spectral unmixing in OA imaging by utilizing the regularization effect of the decomposition to prevent negative values of low frequency signals from compromising the signal quantification in small vasculature. Fig. 5a displays the absorption spectra of oxygenated hemoglobin (HbO₂) and deoxygenated hemoglobin (Hb) in the range 680 - 980 nm. Fig. 5b shows the Hb and HbO₂ spectral linear unmixing results for mouse cross sections of the liver and kidneys, obtained from both 2bMB and standard MB reconstruction. Notably, the proposed method improves linear unmixing results in small vessels, which are otherwise obscured by low frequency signals. The magnification of a region-of-interest (ROI) in the right lobe of the liver clearly shows the small vasculature that supply blood to the liver; the magnification of a ROI in the left kidney demonstrates Hb and HbO₂ quantification in the splenic vessel, as well as in the small vasculature in the kidney cortex.

IV. DISCUSSION

OA imaging yields rich information content due to the detection of broadband acoustic signals. However, it is challenging to faithfully render objects in different size regimes with a single image, which compromises the accuracy of subsequent physical and spectral analyses. To overcome this challenge, we developed fbMB, a method which employs soft priors on the frequency bands to generate OA images with frequency-band-specific contrast; low-frequency images contain bulk tissue, organs, and out-of-plane signals, while high-frequency images contain small vasculature and anatomical details. The method is a practical solution to the longstanding problem to reliably separate OA contrast from different frequency bands and thereby counteract the bias towards low frequencies in OA imaging.

Contrary to standard back-projection and model-based reconstructions, the new algorithm allows, for the first time, access to the full structural content of broadband OA images, which is of great value for preclinical and clinical applications. In combination with the three spatial dimensions (3D), the time dimension (4D), and the optical wavelength dimension (5D), fbMB adds a sixth "ultrasound frequency dimension" (6D) to OA imaging, thus enabling analysis of images over multiple scales [4]. The acquisition and visualization of sixdimensional OA data enables the full range of OA contrast mechanisms, i.e., real time volumetric imaging at multiple wavelengths of structures with a wide range of sizes, offering unique performance among current biomedical imaging modalities.

The ability of fbMB to separate different frequency bands without generating artefacts was quantitatively evaluated on a dataset of 533 *in vivo* OA images from different mouse anatomical sections. By imposing soft priors on the filters and allowing frequency bands to overlap, the new method provides a unique solution to the decomposition problem, which is less prone to reconstruction errors and artefacts than rigid filtering. Moreover, fbMB generates OA images with richer informational content and better visual and structural perception compared to standard model-based reconstruction. The resulting OA images are more detailed and resolve anatomical structures with high biological accuracy, increasing the biomedical value of OA imaging systems.

Spectral unmixing applied to fbMB reconstructions enables quantification of absorbers at resolutions ranging from millimeters to micrometers. In general, spectral unmixing algorithms are applied to OA images reconstructed with standard model-based algorithms due to their higher accuracy compared to back-projection algorithms. However, a common problem for OA image quantification is that negative values in low frequencies of the signal originating from larger structures or artefacts [30] compromise the quantification of small-scale features. Here instead, the multiscale representation of different chromophores through fbMB prevents negative values from low frequencies to interfere with the signal from smaller structures and enables in principle label-free quantification of the vasculature down to the capillary level. This result may expand applications of OA image quantification in, for example, cardiovascular imaging by providing anatomical information from macro- to microvasculatures, in cancer imaging by detecting angiogenesis and tissue perfusion, and in neuroimaging by mapping the hemodynamics in the brain vasculatures with high resolution.

The fbMB method allows a broad range of applications and extensions. For instance, beyond multiscale contrast, one could include the spectral dimension into the reconstruction, which could enable simultaneous unmixing for multiscale quantification of specific chromophores in the same schema. A variation of the introduced method could also help to decouple absorption and light fluence, which exhibits a global low spatial frequency component [21], thus potentially improving OA signal quantification in small vasculatures and in bulk tissue.

In addition, a dedicated filter design in the soft priors could improve the current results for special applications. Indeed, each of these frequency bands has biological and clinical potential, ranging from assessing mechanisms in organs and bulky tissues at the macroscopic scale to detecting physiological processes at microscopic levels (e.g., in the microvasculature). Similarly, a dedicated image post-processing (i.e., image histogram thresholding) may be necessary to achieve optimal image quality for certain specific application, wavelength, or anatomical section.

Notably, the method is also applicable to other image reconstruction problems that suffer from the same bias towards low frequencies. Furthermore, the method can be easily rescaled and extended to OA microscopy and mesoscopy.

Recently, applications of machine learning in imaging have afforded real time implementations of previously computationally expensive reconstruction methods. The acceleration of fbMB through deep learning, would allow real time feedback of multiple frequency band components to the system user in clinical applications. This would enhance the clinical usage of MSOT for screening and diagnosis.

The proposed method enables a unique frequency-band contrast for OA imaging encoding the entire OA content in a single image. The improved image quality and visual perception of anatomical structures will advance the translation of OA technology in clinical practice.

SOURCE CODE

The source code for the presented fbMB framework is available at https://github.com/juestellab/mb-rec-msot.

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