

Predicting SiC MOSFET Behavior Under Hard-Switching, Soft-Switching, and False Turn-On Conditions

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Abstract—Circuit-level analytical models for hard-switching, soft-switching, and dv/dt -induced false turn on of SiC MOSFETs and their experimental validation are described. The models include the high-frequency parasitic components in the circuit and enable fast, accurate simulation of the switching behavior using only datasheet parameters. To increase the accuracy of models, nonlinearities in the junction capacitances of the devices are incorporated by fitting their nonlinear curves to a simple equation. The numerical solutions of the analytical models provide more accurate prediction than an LTspice simulation with a three-fold reduction in the simulation time. The analytical models are evaluated at 25 °C and 125 °C. The effect of snubber capacitors on the soft-switching waveforms is explained analytically and validated experimentally, which enables the techniques to be used to evaluate future soft-switching solutions. Finally, the dv/dt -induced false turn-on conditions are predicted analytically and validated experimentally. It was observed that consideration of nonlinearities in the junction capacitances ensures accurate prediction of false turn on, and that the small shoot-through current due to false turn on can increase the switching loss by 8% for an off-state gate bias of -2 V.

Index Terms— dv/dt -induced false turn on, parasitic effect, SiC MOSFET switching analysis, shoot-through current, soft-switching, switching losses.

I. INTRODUCTION

TRANSFORMING the device-level advances of SiC technology (lower on-state losses, lower parasitic capacitances, and potentially higher switching frequencies) into smaller and more efficient converters present numerous challenges. One of the challenges is understanding and optimizing the more rapid switching waveforms, including predicting and managing parasitic oscillations, switching losses and electromagnetic interference (EMI).

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To understand the SiC MOSFET static and dynamic behavior, several modeling approaches have been proposed, including semiconductor physics models [1] and behavioral models [2]–[4]. Most of the models are complex or poorly incorporate the circuit parasitic components, and so produce inaccurate circuit waveforms. Although the behavioral Spice model of [2] has a detailed model of the nonlinear Miller capacitor C_{gd} , it did not consider any parasitic inductance at the source or drain terminal. The model was extended in [3] considering the nonlinearity in all the device capacitances; however, the approximation of drain-to-source capacitance C_{ds} , during the switching transients was complex as it was considered to fall exponentially for gate–source voltages around the threshold level. Recently, another PSpice-based behavioral model of a SiC MOSFET module was reported in [4] which included a model for the nonlinear Miller capacitor, C_{gd} dependent on the physical parameters of the MOSFET, such as doping concentrations of the drift and JFET regions and the active chip area. The model also requires an estimation of the transition voltage near the knee point of the $C_{gd} - V_{ds}$ curve to model C_{gd} accurately.

Analytical modeling of the switching transients can be a good approach to understand the switching behavior of SiC MOSFETs [5]. The models can then be extended to incorporate circuit parasitics, soft-switching of the power devices and also false turn-on conditions. One of the key objectives of this work is to develop an analytical model to evaluate the SiC MOSFET’s full switching behavior.

Although the analysis of dv/dt -induced false turn on has been widely examined for low-voltage Si MOSFETs [6]–[8], very little has been published [9] for the SiC MOSFET. Opposing views are apparent in the published literature on Si MOSFETs with regard to the impact of common source inductance on the false turn on. Elbanhawy [6] and Black [7] suggest that common source inductance reduces the chance of false turn on, whereas Jianjing and Chung [8] suggest the opposite. Jianjing and Chung [8] give the most detailed analysis of a 80 V Si MOSFET’s false turn on by including almost all the parasitic components. However, the model did not consider the nonlinear characteristics of the device capacitances which are shown in this work to be critical for determining the dv/dt -induced false turn on of SiC MOSFETs. An experimental analysis of temperature-dependent losses associated with SiC MOSFET’s false turn on was presented in [9] and compared with an Si insulated gate bipolar transistor (IGBT). An analytical model

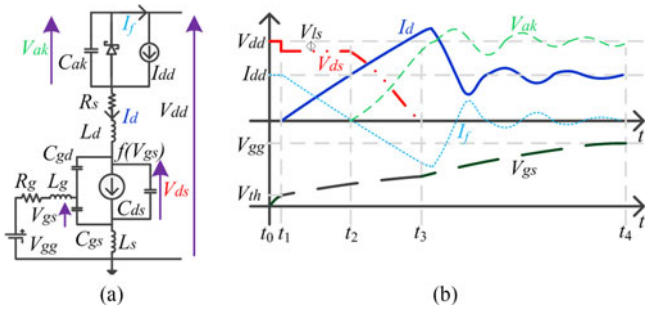


Fig. 1. (a) Equivalent circuit of DPT circuit during the active region of SiC MOSFET. (b) DPT circuit waveforms during turn on.

was also introduced to predict only the gate-to-source voltage of the MOSFET and IGBT during false turn on, again considering only fixed device capacitances. However, the losses associated with the output capacitance of the devices were not quantified; these losses can be determined from the modeling approach presented in this paper.

In this paper, Section II presents a theoretical overview of three different SiC MOSFET switching circuits. The associated waveforms establish the basis of the analytical models explained in Sections III and IV, which also show how the models can be implemented in MATLAB. Section V verifies the modeling approach for hard-switching, soft-switching and dv/dt -induced false turn-on conditions. Finally, Section VI draws conclusions.

II. OVERVIEW OF SiC MOSFET SWITCHING

A. Hard-Switching

To investigate hard-switching, the double-pulse test (DPT) circuit is used, see Fig. 1(a). The diagram includes the main circuit parasitics, such as the MOSFET common source inductance L_s , drain inductance L_d , gate lead inductance L_g , parasitic capacitances of the MOSFET C_{gs} , C_{gd} , and C_{ds} , diode and load inductor lumped parasitic capacitance C_{ak} , and the equivalent series resistance of the power loop R_s . Fig. 1(b) shows simplified turn-on waveforms for the MOSFET, including drain-to-source voltage V_{ds} , drain current I_d , gate-to-source voltage V_{gs} , Schottky diode voltage V_{ak} , and the diode current I_f .

V_{gs} increases during $t_0 - t_1$ in an exponential manner as the gate current charges the MOSFET input capacitances C_{gs} and C_{gd} . V_{gs} reaches the threshold level V_{th} at t_1 and I_d starts to increase. At the same time, diode current I_f also starts to fall from the load current level I_{dd} and at time t_2 , the current commutation between the diode and MOSFET finishes. During this subperiod, $t_1 - t_2$, due to the voltage drop V_{ls} across L_d and L_s , V_{ds} reduces from the input dc voltage V_{dd} .

At time t_2 , V_{ds} starts to fall as the voltage starts to increase across the diode parasitic capacitor C_{ak} . The MOSFET current I_d increases beyond the load current level due to the charging current of C_{ak} until V_{ak} reaches the level $V_{dd} - V_{ls}$ at time t_3 . At this point, V_{ds} reaches its on-state voltage level $V_{ds(on)}$.

After t_3 , I_d rises slightly then starts to reduce as the energy in the stray inductances transfers to C_{ak} in a resonant manner. This resonance continues until all the resonating energy is dissipated

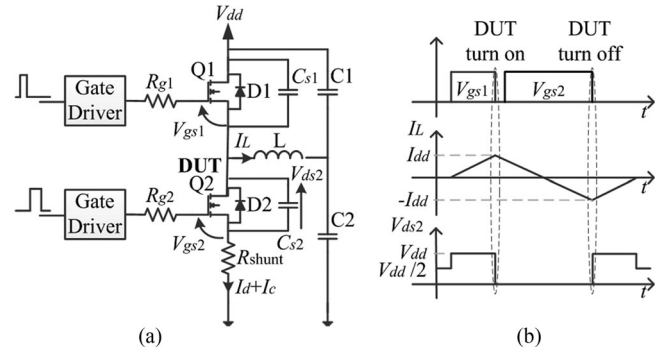


Fig. 2. (a) Test circuit for soft-switching. (b) Ideal circuit waveforms.

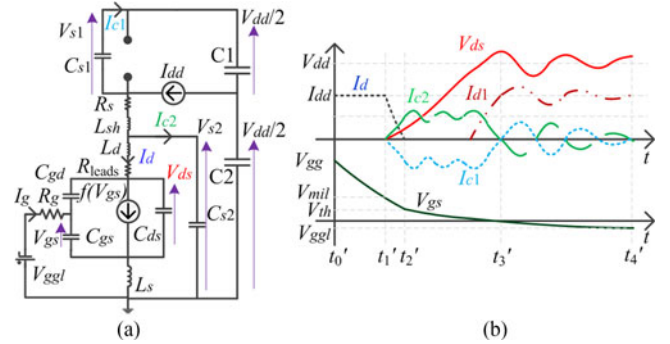


Fig. 3. (a) Soft-switching circuit during the active region of SiC MOSFET Q2. (b) Circuit waveforms during turn off.

by the stray resistance R_s of the circuit. Finally, the drain current is equal to the load current I_{dd} , the diode voltage V_{ak} becomes equal to the dc voltage V_{dd} , and V_{gs} is equal to the gate supply voltage V_{gg} . The switching transient at turn off follows a reverse process to that seen at turn on. The subintervals for turn off are the same as those at turn on but occur in the reverse order.

B. Soft-Switching

To facilitate the soft-switching test, a different arrangement of the DPT circuit, shown in Fig. 2(a), was used where $C1$ and $C2$ are large voltage dividing capacitors. Two snubber capacitors, C_{s1} and C_{s2} are added across Q1 and Q2 to reduce the MOSFET turn-off losses and control the dv/dt . The total capacitance across the devices is therefore the sum of the snubber capacitor and the device output capacitances. The capacitances are charged and discharged in a lossless manner as Q1 and Q2 turn off [see Fig. 2(b)]. During the turn-off instant of the device under test (DUT) Q2, C_{s1} and C_{s2} slow down the voltage transient to reduce the turn-off losses. Energy is stored in C_{s2} whilst C_{s1} is discharged. The energy stored by C_{s2} is recovered into the conversion process when Q1 turns off.

Fig. 3(a) shows the soft-switching circuit during the turn off of the DUT, Q2. Here, I_{c1} and I_{c2} are the currents flowing through the snubber capacitors C_{s1} and C_{s2} , respectively. The turn-off waveforms are shown in Fig. 3(b).

The gate-to-source voltage V_{gs} decreases during $t_0' - t_1'$ in an exponential manner as the gate current discharges the MOSFET input capacitances C_{gs} and C_{gd} . V_{gs} reaches the Miller level

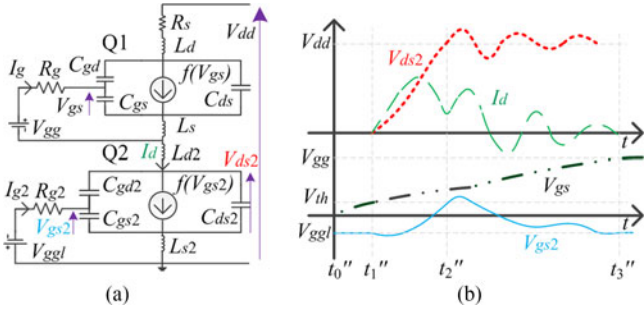


Fig. 4. (a) Equivalent circuit of the DPT during false turn on of Q2 while Q1 turns on. (b) DPT waveforms.

V_{mil} at t_1' , V_{ds} starts to increase, and I_d starts to decrease. Due to the snubber capacitors, V_{ds} increases gradually while I_d falls, reaching zero at t_2' as V_{gs} reaches its threshold level, V_{th} . In this subperiod, I_{dd} commutates to the snubber capacitors.

During the subperiod $t_2' - t_3'$, I_{dd} is shared equally by the two snubber branches. Due to the parasitic inductance in the current paths, both I_{c1} and I_{c2} will be oscillatory. Toward the end of the $t_2' - t_3'$ subperiod, V_{ds} will reach V_{dd} and the upper device will start to conduct (I_{d1}) terminating the snubber branch currents. After t_3' , the circuit capacitances and inductances will continue to resonate until a steady state is reached when the upper device current I_{d1} equals the load current I_{dd} , I_{c1} and I_{c2} become zero, and V_{gs} equals the negative bias level of V_{gg1} .

C. dv/dt -Induced False Turn On

To investigate the dv/dt -induced false turn on, the DPT circuit in Section II-B was used with some minor modifications. In Fig. 2, the inductor L was connected to the ground, the snubber capacitors were removed, and the DUT was held off by setting a negative gate bias on Q2. A single pulse was applied to the gate of Q1 and as the device turned on a high dv/dt was imposed across Q2 which created a displacement current through the output capacitors of Q2. Depending on the speed at which Q1 turns on, the gate resistance of Q2, R_{g2} , the negative gate bias, V_{gg1} , and the stray inductances associated with Q2, a false turn on of Q2 could happen if the induced gate-to-source voltage V_{gs2} exceeds the threshold level. The presence of the load inductor ensures that the initial voltage across Q2 is zero, although the inductor current remains virtually zero due to its large inductance (460 μ H) and the component is neglected in the analysis. It was assumed that the effect of inductor current on the dv/dt is negligible compared with the effect of gate resistances and device capacitances and the validity of this assumption was confirmed by the experimental measurements in Section V. Also, the current sensed at the source of Q2 by the shunt resistance R_{shunt} will include the displacement current through the output capacitor of Q2 and its channel current if false turn on happens.

The false turn-on process is explained in Fig. 4 using the equivalent circuit in Fig. 4(a). During $t_0'' - t_1''$, Q1 remains turned off as $V_{gs} < V_{th}$. At t_1'' , the current starts to flow in the channel of Q1 as well as in the drain of Q2 (I_d), while the output capacitance

of Q1 discharges and the output capacitance of Q2 is charged. The induced voltage across L_{s2} initially reduces V_{gs2} , but V_{gs2} then increases due to the Miller current flowing through R_{g2} . If V_{gs2} crosses the threshold level, Q2 turns on and I_d increases. At t_2'' , Q1 becomes fully on and V_{ds2} reaches the dc voltage V_{dd} , and the dv/dt across Q2 starts to decrease. During the rest of subperiod $t_2'' - t_3''$ V_{gs2} gradually decreases to V_{gg1} , while the oscillations in V_{ds2} and I_d are damped by the resistance of the circuit R_s .

III. MODELING OF SiC MOSFET HARD-SWITCHING TRANSIENTS

Modeling the SiC MOSFET turn-on and turn-off transients requires the solution of four equivalent circuits corresponding to the four distinct stages of each transient. The modeling approach is similar to the published Si-MOSFET analytical models [10], [11], but the difference is the incorporation of the major circuit parasitic components in all of the transient stages. Also, no assumptions are used in the model to predict the voltage transitions between the equivalent circuits. The “ode45” differential equation solver was used in MATLAB to solve the state equations for each subperiod. The final values from one subperiod form the initial conditions for the next sub-period.

The equivalent circuits for the turn-on and turn-off transient states are shown in Fig. 5. Here, L_d is the sum of the inductances of the MOSFET drain lead L_{drain} , printed circuit board (PCB) current paths L_{pcb} , diode leads L_{lead} , and current shunt resistor L_{shunt} . Four state variables, V_{gs} , V_{ds} , I_d , and \dot{I}_d (rate of change of drain current), were considered and were solved using four state-space equations. A step gate pulse from V_{gg1} to V_{gg} was used to initiate the turn-on transient. The other two inputs were the supply voltage V_{dd} and load current I_{dd} . The four subperiods during the turn-on transient correspond to 1) turn-on delay, 2) drain current rise, 3) drain-to-source voltage fall, and 4) ringing stages. The gate inductance L_g was neglected because it is small (around one fourth) compared with the power loop inductance $L_d + L_s$, and the validity of this assumption was confirmed by the experimental measurements in Section V.

A. Turn-On Model

A step gate pulse from V_{gg1} to V_{gg} initiates turn on which drives the solution of the turn-on transient model ($V_{gg1} < 0$).

1) *Subperiod 1 ($t_0 - t_1$) (Turn-On Delay)*: After the gate pulse is applied, the gate current charges the MOSFET input capacitors C_{gs} and C_{gd} . The MOSFET stays off until V_{gs} reaches V_{th} and the load current, I_{dd} circulates through the Schottky diode. The drain current is zero and the drain-to-source voltage is equal to the dc-link voltage V_{dd} in this subperiod. From (1)–(3), shown below, the state equations (4) and (5), also shown below, for this subperiod can be found, where $I_d = 0$ and $C_{iss} = C_{gs} + C_{gd}$. After solving state equations (4) and (5) in MATLAB using $V_{g,in} = V_{gg}$ and the initial conditions, $V_{gs}(0) = V_{gg1}$ and $I_g(0) = 0$, V_{gs} and I_g for this subperiod can be found. The turn-on delay, $t_1 - t_0$, is the time required for V_{gs}

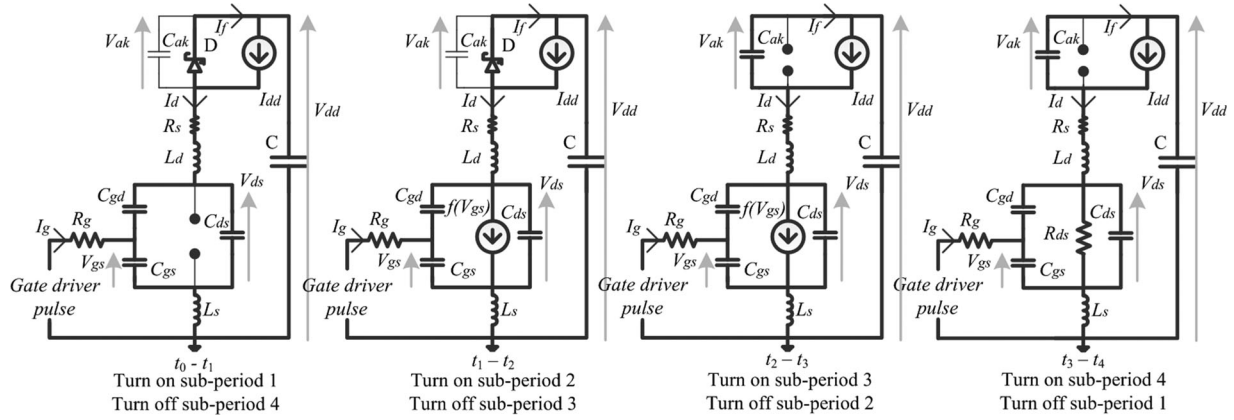


Fig. 5. Equivalent circuits for turn on and turn off sub-periods corresponding to the hard-switching DPT circuit.

to reach V_{th} from V_{gg1}

$$R_g I_g = V_{g.in} - V_{gs} - L_s \frac{dI_d}{dt} - L_s \frac{dI_g}{dt} \quad (1)$$

$$I_g = C_{gs} \frac{dV_{gs}}{dt} + C_{gd} \frac{dV_{gd}}{dt} \quad (2)$$

$$V_{gs} = V_{gd} + V_{ds} \quad (3)$$

$$\frac{dV_{gs}}{dt} = \frac{I_g}{C_{iss}} \quad (4)$$

$$\frac{dI_g}{dt} = -\frac{V_{gs}}{L_s} - \frac{R_g I_g}{L_s} + \frac{V_{g.in}}{L_s}. \quad (5)$$

2) *Subperiod 2* ($t_1 - t_2$) (*Current Rise Time*): The current commutation between the diode and MOSFET happens in this stage. As the MOSFET is in the saturation region its channel current will be directly proportional to $(V_{gs} - V_{th})$. V_{ds} decreases in this stage because of the di/dt -induced voltages across L_s and L_d as shown in the following equation:

$$V_{ds} = V_{dd} - (L_s + L_d) \frac{dI_d}{dt} - R_s I_d. \quad (6)$$

The drain current can be found by combining the channel current with the MOSFET output capacitance current as shown in the following equation, where $C_{oss} = C_{ds} + C_{gd}$:

$$I_d = g_m (V_{gs} - V_{th}) + C_{oss} \frac{dV_{ds}}{dt} \quad (7)$$

To simplify the model, the impact of the gate current I_g on the common source inductance L_s was neglected assuming I_g is much smaller than the drain current I_d

$$R_g I_g = V_{g.in} - V_{gs} - L_s \frac{dI_d}{dt}. \quad (8)$$

The state equations (A1) for this subperiod are derived using (2), (3), and (6)–(8) and are shown in the Appendix. The current rise time, $t_2 - t_1$ is the time required for V_{gs} to reach V_{mil} from V_{th} , where $V_{mil} = I_{dd}/g_m + V_{th}$ and g_m is the transconductance of the MOSFET. The drain current will reach the load current level at the end of this subperiod.

3) *Subperiod 3* ($t_2 - t_3$) (*Voltage Fall Time*): The voltage V_{ak} across the Schottky diode capacitance C_{ak} is expressed

as (9), shown below, and V_{ds} can be expressed as (10), also shown below, for this subperiod. The state equations (A2) for this subperiod are derived using (2), (3), and (7)–(10) and are shown in the Appendix. The voltage fall time $t_3 - t_2$ is the time required for V_{ds} to reach $V_{ds(on)}$ from V_{ds} (t_2)

$$\frac{dV_{ak}}{dt} = \frac{1}{C_{ak}} (I_d - I_{dd}) \quad (9)$$

$$V_{ds} = V_{dd} - (L_s + L_d) \frac{dI_d}{dt} - V_{ak} - R_s I_d. \quad (10)$$

4) *Subperiod 4* ($t_3 - t_4$) (*Ringing Period*): As the MOSFET is now in the ohmic region, the drain current can be expressed as (11), shown below. The state equations (A3) for this subperiod, derived using (2), (3), and (8)–(11), are shown in the Appendix. High-frequency parasitic inductances are considered in this subperiod as well as shown in (10). The time for this subperiod $t_4 - t_3$ is approximated by the time required for V_{gs} to reach V_{gg} from V_{gs} (t_3)

$$I_d = \frac{V_{ds}}{R_{ds}} + C_{oss} \frac{dV_{ds}}{dt}. \quad (11)$$

B. Model Implementation

Fig. 6 shows a summary of the turn-on solution process in MATLAB. The state equations are solved using the parameters and parasitic values shown in Table I (see Section IV-C). When solving (A2) for subperiod 3, the nonlinearities in junction capacitances were considered. These voltage-dependent parasitic capacitances of the MOSFET (C_{gd} , C_{iss} , and C_{oss}) and the Schottky diode (C_{ak}) were modeled by fitting their datasheet curves to (12), shown below, which is based on the equation typically used for low-voltage silicon MOSFETs [10]. C_{ov} and C_{hv} are the low-voltage and high-voltage capacitance values used to calculate the curve fitting coefficients x and C_j . The C_{hv} term was included in (12) to achieve acceptable fitting of the variable capacitance curve over the wide voltage range of the 1200 V SiC MOSFETs

$$C = \frac{1}{\frac{1}{C_{ov}} + \frac{1}{C_j} V^x} + C_{hv}. \quad (12)$$

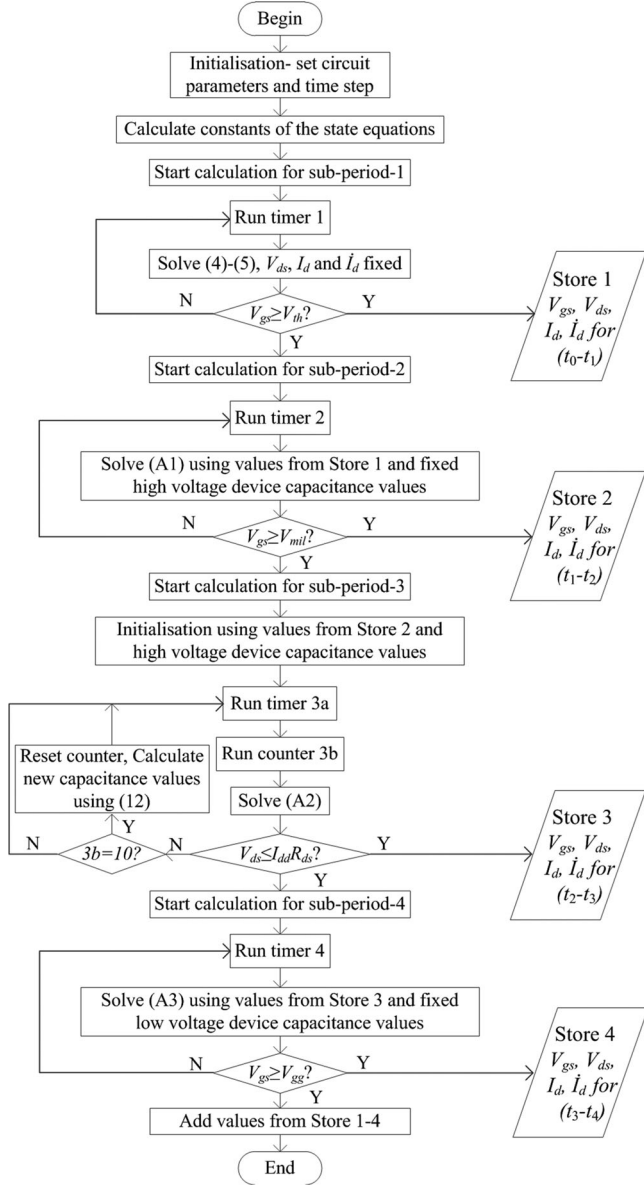


Fig. 6. Flow chart of turn-on solution process.

The linear state equations (A2) were solved in a loop with the junction capacitance values being updated after every ten time steps until V_{ds} reached $V_{ds(on)}$. Then, (A3) was solved for subperiod 4, using the low-voltage junction capacitance values, until V_{gs} reached V_{gg} when the simulation finally ends.

Datasheet values of the devices' capacitances [12]–[14] were compared with the fitted model, (12) in Fig. 7 for a SiC MOSFET, C2M0080120D and two SiC Schottky diodes, Cree C4D10120D and ROHM SCS230KE2. Fig. 7 shows that the variation of the devices' capacitances is well captured. The program updates the capacitor values around 100 times during a 600 V, 20 A switching transient which was judged to provide a good balance between accuracy and speed of simulation.

C. Turn-Off Model

A gate voltage transition from V_{gg} to V_{ggl} initiates the turn-off sequence. The four turn-off subperiods (see Fig. 5) are identical

 TABLE I
PARAMETERS AND PARASITIC VALUES

Section	Parameter	Value	Parameter	Value
Power circuit	V_{dd}	600 V	I_{dd}	8–20 A
	$R_{shunt}(DC)$	10 m Ω	L_{pcb}	20 nH
	$R_{shunt}(100\text{ MHz})$	53 m Ω	$C_L(100\text{ MHz})$	6.5 pF
	$R_{pcb}(100\text{ MHz})$	100 m Ω	$R_L(100\text{ MHz})$	16.8 Ω
	$R_{leads}(100\text{ MHz})$	70 m Ω	L_{shunt}	8 nH
Gate drive circuit	V_{gg}	20 V	V_{ggl}	−4 V
	R_g	11.27 Ω (including $R_{gint} = 4.6\ \Omega$)		
SiC MOSFET C2M0080120D	$R_{ds}(25\text{ }^\circ\text{C})$	80 m Ω	$g_m(25\text{ }^\circ\text{C})$	8.1 S
	L_s	10.5 nH	L_{drain}	7.5 nH
	$R_{ds}(125\text{ }^\circ\text{C})$	130 m Ω	$g_m(125\text{ }^\circ\text{C})$	7.9 S
Snubber circuit	C_{s1}, C_{s2}	1 nF		
Cree Diode, C4D10120D	L_{lead}	12.5 nH	V_F	0.93 V
	$R_d(25\text{ }^\circ\text{C})$	10 m Ω		
ROHM Diode, SCS230KE2	L_{lead}	12.5 nH	V_F	0.95 V
	$R_d(25\text{ }^\circ\text{C})$	15 m Ω		

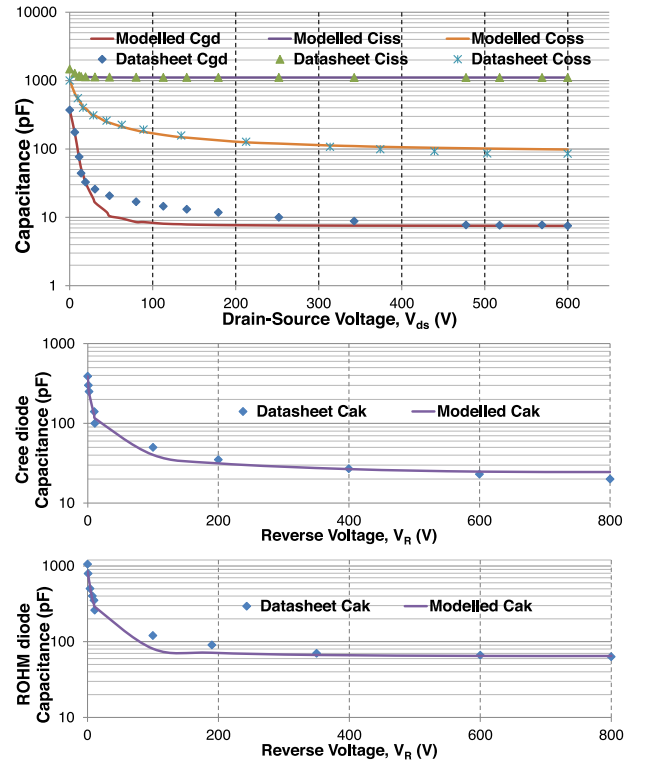


Fig. 7. Datasheet capacitances of the C2M0080120D MOSFET and Schottky diodes and the nonlinear model.

to the turn-on subperiods but occur in reverse order. The state equations can be derived in a similar manner. After the negative gate pulse is applied, the MOSFET input capacitors C_{gs} and C_{gd} begin to discharge. Equations (4) and (5) are the state equations for the subperiod 1 (turn-off delay) and the state variables can be solved using $V_{g,in} = V_{ggl}$ and the initial conditions, $V_{gs}(0) = V_{gg}$ and $I_g(0) = 0$. The state equations for subperiods 2 and 3 will be exactly the same as the corresponding turn-on equations, (A2) and (A1), respectively. In subperiod 4, the MOSFET is in the cut-off region and the MOSFET output capacitor C_{oss} resonates with the stray inductances of the circuit.

The drain current can be expressed as (13), shown below. The state equations (A4) for this subperiod are derived using (2), (3), (6), (8), and (13) and are shown in the Appendix

$$I_d = C_{oss} \frac{dV_{ds}}{dt}. \quad (13)$$

IV. MODELING OF SiC MOSFET SOFT-SWITCHING AND dv/dt -INDUCED FALSE TURN ON

A. Soft-Switching

To model the soft-switching transient, only the turn-off transient of the lower device (DUT) in Fig. 2(a) was analyzed because this transient also corresponds to turn on of the upper device. The equations modeling soft-switching can be derived from Fig. 3. Similar to hard-switching, the soft-switching model is based on the solution of four distinct stages of the transient 1) turn-off delay, 2) drain current fall, 3) drain-to-source voltage rise, and 4) ringing periods. Two additional state variables, snubber capacitor current I_{c2} , and its rate of change \dot{I}_{c2} were used in addition to the other four state variables V_{gs} , V_{ds} , I_d , and \dot{I}_d . The resulting state-space equations were solved sequentially.

Subperiod 1' ($t'_0 - t'_1$) (Turn-off delay): This is exactly the same as the turn-off delay subperiod of the hard-switching model.

Subperiod 2' ($t'_1 - t'_2$) (Current fall period): The system of state equations (A5) for this subperiod can be formed from (2), (3), (7), (8), and (14)–(17), shown below. Here, V_{s1} and V_{s2} are the voltages across the snubber capacitors. $t'_2 - t'_1$ is the time required for V_{gs} to reach V_{th} from V_{mil}

$$V_{ds} = V_{dd} - V_{s1} - (R_s + R_{leads})I_d - R_s I_{c2} - (L_s + L_d) \frac{dI_d}{dt} - L_{sh} \frac{d}{dt} (I_d + I_{c2}) \quad (14)$$

$$\frac{dV_{s1}}{dt} = \frac{1}{C_{s1}} (I_d + I_{c2} - I_{dd}) \quad (15)$$

$$\frac{dV_{s2}}{dt} = \frac{I_{c2}}{C_{s2}} \quad (16)$$

$$V_{s1} + V_{s2} = V_{dd} - R_s (I_d + I_{c2}) - L_{sh} \frac{d}{dt} (I_d + I_{c2}). \quad (17)$$

Subperiod 3' ($t'_2 - t'_3$) (Voltage rise period): The state equations (A6) for this subperiod are derived using (2), (3), (8), (13), and (14)–(17). $t'_3 - t'_2$ is the time required for V_{s1} to reach zero from $V_{s1}(t'_2)$.

Sub-period 4' ($t'_3 - t'_4$) (Ringing period): Because the diode on-state resistance R_d was considered, one additional state variable V_{s1} has to be solved in this subperiod. The state equations (A7) are derived using (2), (3), (8), (13), (14), and (16)–(18), shown below. $t'_4 - t'_3$ is approximated by the time required for V_{gs} to reach V_{ggl} from $V_{gs}(t'_3)$

$$\frac{dV_{s1}}{dt} = \frac{1}{C_{s1}} \left(I_d + I_{c2} - \frac{V_{s1} + V_F}{R_d} - I_{dd} \right). \quad (18)$$

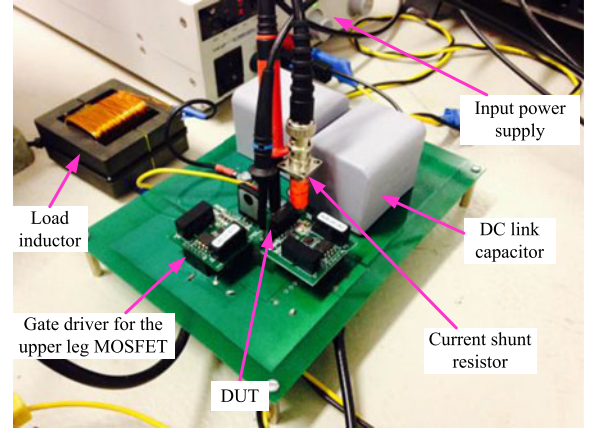


Fig. 8. Experimental setup for DPT tests.

B. dv/dt -Induced False Turn On

The equations modeling the dv/dt -induced false turn on can be derived from Fig. 4. In this case, there are three subperiods: 1) turn-on delay, 2) voltage and current transitions, and 3) ringing period. The upper MOSFET Q1 is modeled in the same way as in the turn-on transient in Section III-A except now the voltage and current transitions happen simultaneously and the load current, $I_{dd} = 0$. Apart from the four state variables V_{gs} , V_{ds} , I_d , and \dot{I}_d associated with Q1 another additional state variable, the gate-to-source voltage of Q2 V_{gs2} is added to the model to determine the false turn on of Q2. The state equations for subperiod $t''_0 - t''_1$ are exactly same as those for subperiod $t_0 - t_1$ of the hard-switching model with V_{gs2} fixed at V_{ggl} . For the second and third subperiods, the state equations (A8) and (A9), shown in the Appendix, are derived from Fig. 4(a) assuming Q2 remains in the off state. Circuit equations (2), (3), and (7)–(11) of the previously described hard-switching model in Section III-A are used to derive (A8) and (A9). When solving (A8), all the device parasitic capacitances are modeled by fitting their nonlinear curves to (12) as explained in Section III-B.

C. Numerical Solution of Analytical Model

The analytical models were solved in MATLAB using datasheet information for R_{ds} , g_m , R_d , V_F , package inductances and device capacitances [12]–[14], and measured values from the PCB layout; see Table I. The power circuit parasitic values were measured using a precision impedance analyzer, Agilent 4294A. The resistance of the power loop, R_s is the sum of the ac resistances of current shunt resistor R_{shunt} , PCB current paths R_{PCB} , MOSFET and diode resistances (R_{ds} , R_d , and R_{leads}). The interwinding parasitic capacitance of the load inductor, C_L and its high-frequency ac resistance, R_L were included in the model in the ringing subperiods.

V. SIMULATION AND EXPERIMENTAL RESULTS

A 600 V, 20 A DPT circuit shown in Fig. 8 was considered. A Cree SiC MOSFET gate driver circuit, CRD-001 was used. T&M Research's high-bandwidth (2 GHz) current shunt resistor, SDN-414-01 was used to measure the source current.

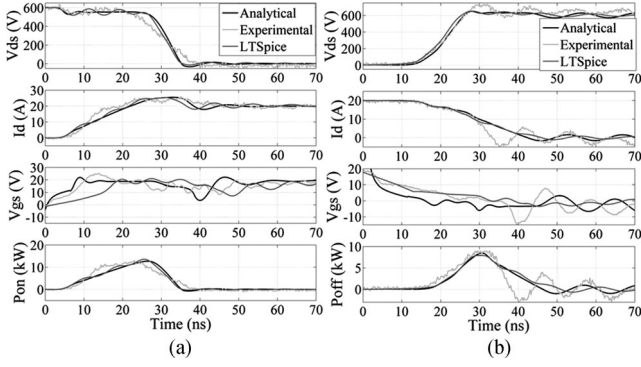


Fig. 9. Measured, predicted, and Spice simulation results with Cree C4D10120D diode 600 V, 20 A at $T_j = 25^\circ\text{C}$, (a) turn on and (b) turn off.

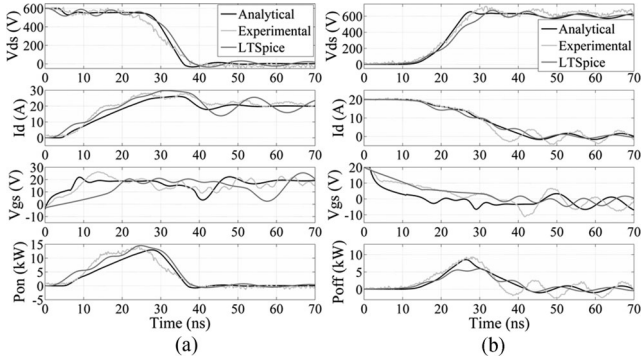


Fig. 10. Measured, predicted, and Spice simulation results with ROHM SCS230KE2 diode 600 V, 20 A at $T_j = 25^\circ\text{C}$, (a) turn on and (b) turn off.

LeCroy high-voltage high-bandwidth passive probes, PPE2KV (400 MHz) and PP008 (500 MHz) were used to measure V_{ds} and V_{gs} , respectively. A de-skew calibration test was performed in the Teledyne LeCroy 400 MHz Wave Runner 44Xi-A oscilloscope to compensate the different propagation delays between V_{ds} and I_d . The connection of the load inductor can be changed to enable hard-switching, soft-switching, and false turn-on tests to be performed using the same circuit for fair comparison.

The DPT circuits were also simulated in LTSpice using the manufacturers' Spice models of the SiC MOSFET (C2M0080120D library beta version) and Schottky diodes (C4D10120D-11/2014 version and SCS230KE2-02/2013 version). A time step of 0.01 ns was selected for both the numerical calculation of the model and the LTSpice simulation as the SiC MOSFET switching transient times are around tens of ns.

A. Hard-Switching

Experimental, calculated, and LTSpice simulation transients for hard-switching operation at 600 V 20 A are shown in Figs. 9 and 10 for two different Schottky diodes when the junction temperature of the MOSFET (T_j) was around 25°C . The V_{ds} and V_{gs} waveforms include the voltages across the device package inductances and resistances. The experimental dV_{ds}/dt was 31 kV/ μs at turn on and 46 kV/ μs at turn off. The experimental di/dt was 1.5 kA/ μs at turn on and 1.1 kA/ μs at turn off. In both figures, the calculated and LTSpice simulated voltage and current transients showed a good match with the experimental

TABLE II
SWITCHING LOSS COMPARISON 25°C OPERATION

Conditions	State	Loss (μJ)			
		Experiment	Analytical	LTSpice	Fixed Cap
600 V 20 A with Cree C4D10120D	Turn on	236	225	228	265
	Turn off	117	120	130	251
	Total	353	345	358	516
600 V 20 A with ROHM SCS230KE2	Turn on	234	232	302	263
	Turn off	126	116	104	252
	Total	360	348	406	515
600 V 13 A with Cree C4D10120D	Turn on	115	123	128	145
	Turn off	54	49	59	137
	Total	169	172	187	282
600 V 13 A with ROHM SCS230KE2	Turn on	125	128	184	143
	Turn off	55	48	43	140
	Total	180	176	227	283

results. The V_{ds} and I_{ds} waveforms are first multiplied to get P_{on} and P_{off} and then integrated to calculate the switching energy losses. The losses from the experiments are summarized in Table II. It is evident that compared to the LTSpice models the analytical models gave a better switching loss estimation (less than 10% error in most cases). The maximum errors from the analytical models were around 13% for individual losses and around 3% for the total switching losses. However, the maximum errors from the LTSpice simulations were around 47% for individual losses and around 26% for the total switching losses (with the ROHM diode). The maximum errors from the LTSpice simulations with the Cree diode were around 11% for both the individual losses and the total switching losses. The DPT circuit was also tested using higher and lower gate resistances and lower supply voltages; the percentage errors in the predicted switching losses were found to be similar to those in Figs. 9 and 10.

Both experimental and LTSpice turn-off losses include the energy stored in the device output capacitance and other circuit stray capacitances, which eventually is dissipated during the turn-on transient. Ideally, this loss should be part of the turn-on loss, however due to practical limitations, it is almost impossible to measure the MOSFET channel current. Therefore, this loss is normally considered to be a part of the turn-off loss. The analytical model enables the actual turn-on and turn-off losses to be calculated from the modeled channel current of the MOSFET and V_{ds} .

The analytical modeling results considering constant device capacitances as assumed for Si MOSFETs in [10] and [11] have a very poor correlation with the experimental results. Using the SiC MOSFET datasheet [12], C_{gd} was calculated from the Miller charge Q_{gd} assuming linear drain-to-source voltage transitions and C_{oss} was calculated from the C_{oss} stored energy. Diode capacitances C_{ak} were calculated using the total capacitive charge from their respective datasheets [13], [14]. The results are omitted in Figs. 9 and 10 for clarity, but the switching losses are listed in Table II which showed as high as 154% error in estimating the individual losses and 69% error in the total switching losses.

The advantage of the proposed analytical model over the LTSpice model is a three times reduction in calculation time, a

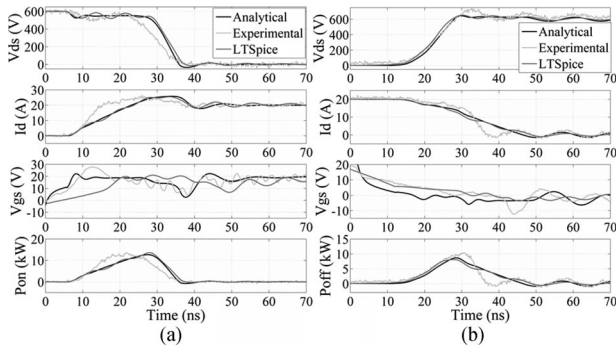


Fig. 11. Measured, predicted, and Spice simulation results with the Cree C4D10120D diode 600 V, 20 A at $T_j = 125^\circ\text{C}$, (a) turn on and (b) turn off.

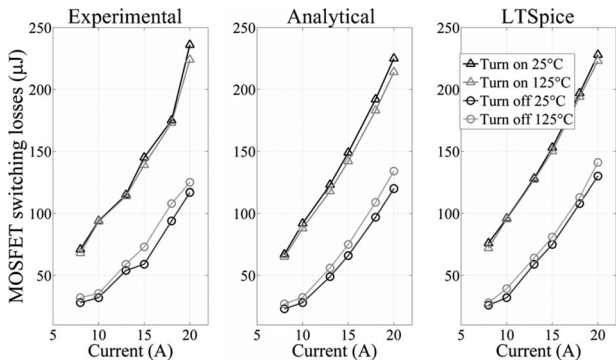


Fig. 12. Measured, predicted, and Spice simulation of turn on and turn off energy loss for different currents at $T_j = 25^\circ\text{C}$ and 125°C , $V_{dd} = 600\text{ V}$.

single turn-on transient takes 0.6 s to complete on an Intel Core i7 3.4 GHz computer. Therefore, the model has the potential to be used in a design optimization program, where increasing the speed of the simulation is one of the key challenges because of the numerous iterations within the program. Also the effect of temperature on the switching transients can be evaluated easily by changing the temperature-dependent parameters in Table I. However, the modeling of ringing in the different waveforms is still limited in both the analytical and LTSpice models as it can be seen that the measured results are more oscillatory than the predictions (see Figs. 9 and 10). Additional parasitic elements such as drain-to-gate external parasitic capacitance and accurate approximation of the high-frequency ac inductance of the power loop may need to be considered for better modeling of the ringing.

Experimental, calculated, and LTSpice simulation transients and switching energy losses for hard switching operation with the Cree diode at higher MOSFET junction temperature $T_j = 125^\circ\text{C}$ are shown in Figs. 11 and 12. Fig. 11 compares the calculated and LTSpice simulation transients with the experiment transients for high-temperature DPT operation at 600 V, 20 A. The temperature-dependent parameters V_{th} , g_m , and R_{ds} were updated in the analytical model and the manufacturers' high-temperature Spice model of the SiC MOSFET was used in LTSpice. Fig. 12 compares the calculated and LTSpice simulated switching energy losses with the experimental losses for a wide

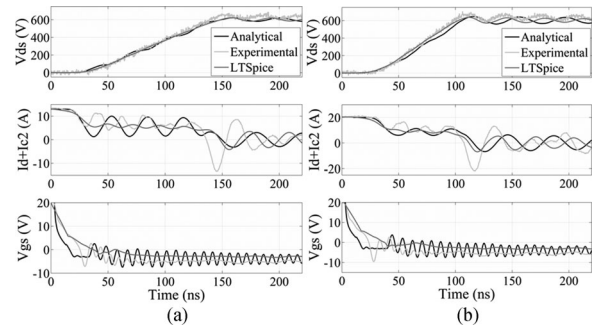


Fig. 13. Measured, predicted, and Spice simulation results for soft-switching turn off 600 V at 25°C : (a) 13 A and (b) 20 A.

range of load currents (8 to 20 A) at both $T_j = 25^\circ\text{C}$ and 125°C with V_{dd} fixed at 600 V.

From both Figs. 11 and 12, it is clear that the calculated and LTSpice simulated transients and switching energy losses show an excellent match with the experimental results. As expected, the turn-on losses are reduced and the turn-off losses are increased with the higher junction temperature (consistent with the MOSFET datasheet [12]). In most cases, errors from the analytical models were less than 10% and from the LTSpice models were less than 13% (similar to the 25°C results). However, the modeling of the ringing becomes more challenging at higher temperature. Comparing the I_d waveforms at turn off between Figs. 11(b) and 9(b) it is clear that the turn-off oscillation is more heavily damped, which was attributed to the increased MOSFET-lead resistances at higher temperature.

B. Soft-Switching

The DPT circuit was tested in the soft-switching configuration using identical SiC MOSFETs as used in the hard-switching tests as the upper and lower leg devices. Fig. 13 shows experimental, analytical, and simulation results of soft-switching at 600 V, 13 A, and 20 A. Comparing Fig. 13(b) with Fig. 9, the snubber circuit has reduced both the dv/dt by a factor of seven and the frequency of oscillations by a factor of three. Here, the analytical model predicts much more ringing in the V_{gs} waveforms which is attributed to the high-frequency ac resistance of the upper MOSFET-connections (Q1), which needs to be predicted more accurately to enable a better match.

The analytical model also enables the calculation of the small turn-off loss of 4 and 10 μJ for 13 and 20 A operations, respectively, by separating the MOSFET drain current I_d from the shunt resistor current $I_d + I_{c2}$. The turn-on losses will be approximately zero as the MOSFET turns on with zero voltage across it because of its body diode conduction. Therefore, for 20 A soft-switching operation, around 92% of the hard-switching energy was saved during turn off making the total soft-switching loss reduction 97% compared to the hard-switching conditions.

C. dv/dt -Induced False Turn On

The test circuit was operated with two Cree SiC MOSFETs in the phase leg to investigate false turn on at different

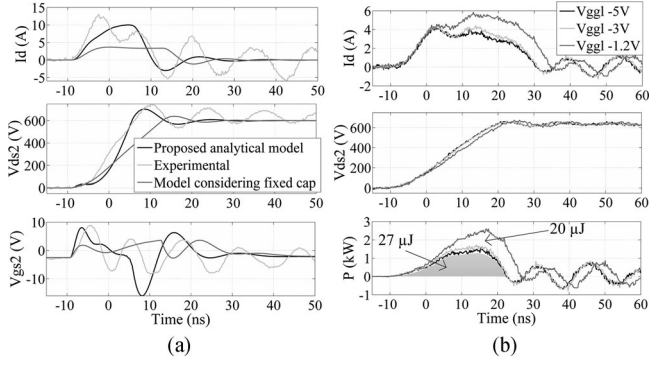


Fig. 14. (a) Q2's false turn on, 11.27Ω gate resistance for both MOSFETs ($V_{gg1} = -2 \text{ V}$). (b) False turn on by reducing V_{gg1} ($R_{g1} = 34.6 \Omega$ and $R_{g2} = 24.6 \Omega$) and loss calculation.

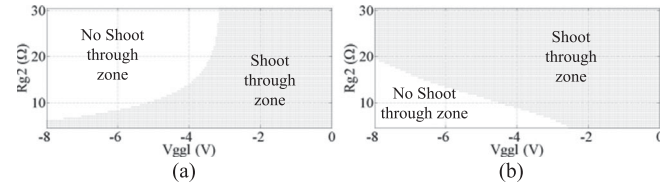


Fig. 15. Predicted false turn-on zones from the model ($R_{g1} = 11.27 \Omega$). (a) Variable capacitance model and (b) fixed capacitance model.

conditions by changing the gate resistances and negative gate-bias voltages. The analytical model accurately predicted the false turn-on conditions by calculating the voltage across the gate-to-source capacitance (C_{gs2}) of the lower MOSFET during the turn-on transient of the upper device. Fig. 14(a) shows the experimental and analytical results for the lower MOSFET (Q2), while the upper MOSFET (Q1) turns on at 600 V with a speed of $40 \text{ kV}/\mu\text{s}$ causing false turn on of the bottom device. The experimental V_{gs2} does not give an accurate indication of false turn on as it consists of voltages across the internal gate resistance (R_{gint}) of the MOSFET, common source inductance (L_{s2}) and C_{gs2} .

Fig. 14(a) also shows that analytical results considering constant device capacitances, as assumed in [8] and [9], have a poor correlation with the experimental results. This again confirms the importance of including the nonlinearity in the device capacitances. To check the efficacy of the modeling approach, two specific gate resistances were selected for the upper and lower MOSFET, 34.6 and 24.6Ω , respectively. Now the negative gate bias, V_{gg1} was changed gradually to find a voltage, where V_{gs2} , the gate-source voltage of the lower MOSFET crosses the threshold level. It was found that for a negative gate bias of 1.2 V false turn on happens for the lower MOSFET [see Fig. 14(b)]. Analytical modeling also predicts a similar value for V_{gg1} during the false turn on of the lower MOSFET.

The analytical modeling results considering nonlinear and constant device capacitances are again compared in Figs. 15 and 16. Considering the upper MOSFET turning on at 600 V with a gate resistance (R_{g1}) of 11.27Ω , Fig. 15 shows the combinations of lower MOSFET gate resistance R_{g2} (varied from 4.6 to 30Ω) and V_{gg1} (varied from 0 to -8 V) which cause false turn on of the lower MOSFET. In one analytical model, the MOSFET device capacitances were nonlinear [see Fig. 15(a)],

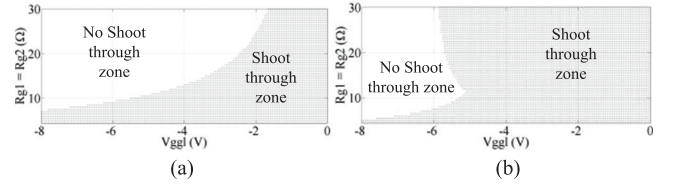


Fig. 16. Predicted false turn-on zones from the model ($R_{g1} = R_{g2}$). (a) Variable capacitance model and (b) fixed capacitance model.

and in the other model, the MOSFET device capacitances were taken as average values [see Fig. 15(b)]. It is clear that when V_{gg1} is between -2.5 and -8 V , the fixed capacitance-based model gives inaccurate prediction of false turn on. Also in the nonlinear capacitance-based model, the chance of shoot-through reduces with the increased R_{g2} because the high common source inductance L_{s2} is dominating the shoot-through mechanism [8]. Fig. 16 shows a similar analysis when both of the gate resistances are equal, $R_{g1} = R_{g2}$. Comparing Fig. 16(a) with Fig. 16(b), when V_{gg1} is between -1.7 and -8 V , the fixed capacitance-based model gives inaccurate prediction of false turn on.

The shoot-through current due to false turn on increases the switching loss of the bottom and top devices by around 20 and $7 \mu\text{J}$, respectively, because of the increased device current. However, $27 \mu\text{J}$ of energy is stored in the bottom device and the circuit parasitic capacitances [see Fig. 14(b)]. Ideally, this energy should not be considered as dv/dt -induced loss as it is part of total stored capacitive energy in the device and circuit parasitic capacitances. The total dv/dt -induced loss was the same ($27 \mu\text{J}$) as for the experiment in Fig. 14(a) which makes the additional loss 8% of the total switching loss of the MOSFET (considering 600 V , 20 A operation with the Cree diode and assuming false turn-on loss is independent of the load current).

VI. CONCLUSION

The analytical model presented in the paper, and validated experimentally can be used to enable rapid and accurate evaluation of circuit waveforms, device switching losses, and dv/dt -induced false turn-on events. The analytical model uses only datasheet parameters so the impact on circuit operation and switching losses of SiC MOSFETs or diodes at different temperatures with different snubber capacitor values and circuit parasitics can be evaluated. In comparison with the established Si-MOSFET analytical models, this paper showed how those models must be enhanced and refined in order to represent accurately the behavior of SiC MOSFETs.

The paper also described the analytical and experimental evaluation of the impact of soft-switching on the MOSFET switching loss, dv/dt and parasitic ringing, which provides an understanding of the benefits of soft-switching in very high-speed SiC circuits. The switching loss was reduced by 97% with soft-switching along with an 86% reduction in dv/dt during the switching transients, which is likely to reduce significantly the EMI signature and unwanted parasitic events such as dv/dt -induced false turn on. These improvements suggest that the use of soft-switching techniques in high-speed SiC MOSFET-based converters could offer significant performance benefits.

It was shown that false turn on can increase switching energy loss of the MOSFET but not as significantly as reported in some recent papers. For example, in the results reported here, almost half of the switching energy losses associated with the false turn on of the devices is actually the stored capacitive energy in the device and circuit parasitic capacitances—conventionally, it was included in the total false turn-on-related losses.

Finally, it was shown that to predict the SiC MOSFET's switching behavior accurately, it is important to model the non-linear device capacitances. If these capacitances are assumed fixed, inaccurate circuit waveforms will result and there will be serious errors in the estimation of losses, and shoot-through events. Therefore, it is recommended that the Spice model of a SiC MOSFET or Schottky diode should include a good model of device capacitances for better prediction of its behavior.

APPENDIX

$$\begin{bmatrix} \dot{V}_{gs} \\ \dot{V}_{ds} \\ \dot{I}_d \\ \ddot{I}_d \end{bmatrix} = \begin{bmatrix} -(a1+a2) & a3 & a4 & 0 \\ -b1 & 0 & b2 & 0 \\ 0 & 0 & 0 & 1 \\ d1 & 0 & -d2 & -d3 \end{bmatrix} \begin{bmatrix} V_{gs} \\ V_{ds} \\ I_d \\ \dot{I}_d \end{bmatrix} + \begin{bmatrix} u1+u2+u3 \\ v1 \\ 0 \\ -w1 \end{bmatrix} \quad (\text{A1})$$

$$\begin{bmatrix} \dot{V}_{gs} \\ \dot{V}_{ds} \\ \dot{I}_d \\ \ddot{I}_d \end{bmatrix} = \begin{bmatrix} -(a1+a2) & 0 & a4 & -a5 \\ -b1 & 0 & b2 & 0 \\ 0 & 0 & 0 & 1 \\ d1 & 0 & -d4 & -d3 \end{bmatrix} \begin{bmatrix} V_{gs} \\ V_{ds} \\ I_d \\ \dot{I}_d \end{bmatrix} + \begin{bmatrix} u1+u2 \\ v1 \\ 0 \\ w2-w1 \end{bmatrix} \quad (\text{A2})$$

$$\begin{bmatrix} \dot{V}_{gs} \\ \dot{V}_{ds} \\ \dot{I}_d \\ \ddot{I}_d \end{bmatrix} = \begin{bmatrix} -a1 & -a4/R_{ds} & a4 & -a5 \\ -b2/R_{ds} & 0 & b2 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & d2/R_{ds} & -(d2+d5) & -d3 \end{bmatrix} \begin{bmatrix} V_{gs} \\ V_{ds} \\ I_d \\ \dot{I}_d \end{bmatrix} + \begin{bmatrix} u1 \\ 0 \\ 0 \\ w2 \end{bmatrix} \quad (\text{A3})$$

$$\begin{bmatrix} \dot{V}_{gs} \\ \dot{V}_{ds} \\ \dot{I}_d \\ \ddot{I}_d \end{bmatrix} = \begin{bmatrix} -a1 & 0 & a4 & -a5 \\ 0 & 0 & b2 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & -d2 & -d3 \end{bmatrix} \begin{bmatrix} V_{gs} \\ V_{ds} \\ I_d \\ \dot{I}_d \end{bmatrix} + \begin{bmatrix} u1 \\ 0 \\ 0 \\ 0 \end{bmatrix} \quad (\text{A4})$$

$$\begin{bmatrix} \dot{V}_{gs} \\ \dot{V}_{ds} \\ \dot{I}_d \\ \ddot{I}_d \\ \dot{I}_{c2} \\ \ddot{I}_{c2} \end{bmatrix} = \begin{bmatrix} -(a1+a2) & 0 & a4 & -a5 & 0 & 0 \\ -b1 & 0 & b2 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ d1 & 0 & -d2 & -d6 & d7 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \\ -d1 & 0 & f1 & f2 & -f3 & -f4 \end{bmatrix}$$

$$\times \begin{bmatrix} V_{gs} \\ V_{ds} \\ I_d \\ \dot{I}_d \\ I_{c2} \\ \dot{I}_{c2} \end{bmatrix} + \begin{bmatrix} u1+u2 \\ v1 \\ 0 \\ -w1 \\ 0 \\ w1+y1 \end{bmatrix} \quad (\text{A5})$$

$$\begin{bmatrix} \dot{V}_{gs} \\ \dot{V}_{ds} \\ \dot{I}_d \\ \ddot{I}_d \\ \dot{I}_{c2} \\ \ddot{I}_{c2} \end{bmatrix} = \begin{bmatrix} -a1 & 0 & a4 & -a5 & 0 & 0 \\ 0 & 0 & b2 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & -d2 & d6 & -d7 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & f1 & f2 & -f3 & -f4 \end{bmatrix} \begin{bmatrix} V_{gs} \\ V_{ds} \\ I_d \\ \dot{I}_d \\ I_{c2} \\ \dot{I}_{c2} \end{bmatrix} + \begin{bmatrix} u1 \\ 0 \\ 0 \\ 0 \\ 0 \\ y1 \end{bmatrix} \quad (\text{A6})$$

$$\begin{bmatrix} \dot{V}_{gs} \\ \dot{V}_{ds} \\ \dot{I}_d \\ \ddot{I}_d \\ \dot{I}_{c2} \\ \ddot{I}_{c2} \\ \dot{V}_{s1} \end{bmatrix} = \begin{bmatrix} -a1 & 0 & a4 & -a5 & 0 & 0 & 0 \\ 0 & 0 & b2 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & -d2 & d6 & -d7 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & f1 & f2 & -f3 & -f4 & f5 \\ 0 & 0 & g1 & 0 & g1 & 0 & -g2 \end{bmatrix} \begin{bmatrix} V_{gs} \\ V_{ds} \\ I_d \\ \dot{I}_d \\ I_{c2} \\ \dot{I}_{c2} \\ V_{s1} \end{bmatrix} + \begin{bmatrix} u1 \\ 0 \\ 0 \\ 0 \\ 0 \\ y1+y2 \\ -z1 \end{bmatrix} \quad (\text{A7})$$

$$\begin{bmatrix} \dot{V}_{gs} \\ \dot{V}_{ds} \\ \dot{I}_d \\ \ddot{I}_d \\ \dot{V}_{gs2} \end{bmatrix} = \begin{bmatrix} -(a1+a2) & 0 & a4 & -a5 & 0 \\ -b1 & 0 & b2 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ d1/2 & 0 & -(d2+d8)/2 & -d3/2 & 0 \\ -a6 & 0 & a7 & -a8 & 0 \end{bmatrix}$$

$$\times \begin{bmatrix} V_{gs} \\ V_{ds} \\ I_d \\ \dot{I}_d \\ V_{gs2} \end{bmatrix} + \begin{bmatrix} u1+u2 \\ v1 \\ 0 \\ -w1/2 \\ u4 \end{bmatrix} \quad (\text{A8})$$

$$\begin{bmatrix} \dot{V}_{gs} \\ \dot{V}_{ds} \\ \dot{I}_d \\ \ddot{I}_d \\ \dot{V}_{gs2} \end{bmatrix} = \begin{bmatrix} -a1 & -a4/R_{ds} & a4 & -a5 & 0 \\ -b2/R_{ds} & 0 & b2 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & d2/(2R_{ds}) & -(d2+d8)/2 & -d3/2 & 0 \\ -a6 & a7 & -a8 & 0 & 0 \end{bmatrix}$$

$$\times \begin{bmatrix} V_{gs} \\ V_{ds} \\ I_d \\ \dot{I}_d \\ V_{gs2} \end{bmatrix} + \begin{bmatrix} u1 \\ 0 \\ 0 \\ 0 \\ u4 \end{bmatrix} \quad (A9)$$

where $a1 = 1/(R_g C_{iss})$, $a2 = g_m C_{gd}/(C_{iss} C_{oss})$, $a3 = L_s/(R_g C_{iss} L_{sd})$, $a4 = C_{gd}/(C_{iss} C_{oss})$, $a5 = L_s/(R_g C_{iss})$, $a6 = 1/(R_{g2} C_{iss2})$, $a7 = C_{gd2}/(C_{iss2} C_{oss2})$, $a8 = L_{s2}/(R_{g2} C_{iss2})$, $b1 = g_m/C_{oss}$, $b2 = 1/C_{oss}$, $d1 = g_m/(C_{oss} L_{sd})$, $d2 = 1/(C_{oss} L_{sd})$, $d3 = R_s/L_{sd}$, $d4 = (C_{ak} + C_{oss})/(C_{ak} C_{oss} L_{sd})$, $d5 = 1/(C_{ak} L_{sd})$, $d6 = R_{leads}/L_{sd}$, $d7 = 1/(C_{s2} L_{sd})$, $d8 = 1/(C_{oss2} L_{sd})$, $f1 = 1/(C_{oss} L_{sd}) - 1/(L_{sh} C_{s1})$, $f2 = R_{leads}/L_{sd} - R_s/L_{sh}$, $f3 = L_{e1}/C_{s2} + 1/(L_{sh} C_{s1})$, $f4 = R_s/L_{sh}$, $f5 = 1/(R_d L_{sh} C_{s1})$, $g1 = 1/C_{s1}$, $g2 = 1/(C_{s1} R_d)$

$L_{sd} = L_s + L_d$, $L_{sh} = L_{shunt} + L_{pcb} + L_{lead}$, $L_{e1} = (L_{sh} + L_{sd})/(L_{sh} L_{sd})$, $u1 = V_{g.in}/(R_g C_{iss})$, $u2 = g_m V_{th} C_{gd}/(C_{iss} C_{oss})$, $u3 = (R_s L_s - V_{dd} L_s)/(R_g C_{iss} L_{sd})$, $u4 = V_{ggl}/(R_{g2} C_{iss2})$, $v1 = g_m V_{th}/C_{oss}$, $w1 = g_m V_{th}/(C_{oss} L_{sd})$, $w2 = I_{dd}/(C_{ak} L_{sd})$, $y1 = I_{dd}/(C_{s1} L_{sh})$, $y2 = V_F/(R_d C_{s1} L_{sh})$, $z1 = I_{dd}/C_{s1} + V_F/(R_d C_{s1})$.

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