# Unequal Timeliness Protection Massive Access for Mission Critical Communications in S-IoT

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Abstract-In this paper, we propose three unequal timeliness (UT) protection massive access (UTMA) schemes in satellite-based Internet of Things (S-IoT) for mission critical communications (MCC) user equipments (UEs) with three types of timeliness requirements: independent successive UTMA (IS-UTMA), extended cognitive offloading UTMA (ECO-UTMA), and independent cognitive offloading UTMA (ICO-UTMA). First, MCC UEs are grouped according to their timeliness requirements, and a multi-dimensional codebook is introduced to resolve the UE collisions in massive access. Then, the IS-UTMA exclusively allocates time slots and pilots to different MCC UE groups to perform massive access, while the ECO- and ICO-UTMA allow timeliness critical group to share resources with timeliness tolerant group to improve the system timeliness. To capture the timeliness evaluation of each MCC UE group, we utilize age of information (AoI) to model the information freshness and derive closed-form expressions of average AoI (AAoI) by tracing the access failure probability (AFP) and instantaneous AoI. Furthermore, we establish the parameter optimization problems to minimize AAoI under desired AFP requirements. Extensive simulations validate the accurate of theoretical derivations, and demonstrate the effectiveness of the proposed UTMA scheme with joint optimized parameters, which can achieve minimum AAoI under desired AFP than the state-of-the-art schemes.

*Index Terms*—Satellite-based Internet of Things, unequal timeliness protection, mission critical communications, age of information, grant free random access.

#### I. INTRODUCTION

**R**ECENTLY, the fifth-generation (5G) communications have been deployed in various fields such as industrial automation [1], smart agriculture, and remote healthcare [2], becoming an important cornerstone for providing timeliness

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massive access of status updates in these applications. However, due to rural environment and extreme weather conditions, the existing terrestrial networks cannot support these timeliness applications in a cost-effective manner [3]. Thanks to the extensive coverage of satellites, satellite-based Internet of Things (S-IoT) is one of the key directions for achieving ubiquitous intelligent connections in the next generation of mobile networks [4], and several mega constellations of low earth orbit (LEO) high-throughput satellites (HTS) are planned and begin to launch, such as Starlink and OneWeb [5], [6].

These upcoming S-IoT are expected to support mission critical communications (MCC) with an end-to-end delay can be as low as 30 ms [7], since the worst two-way propagation delay is expected to be 26 ms for LEO at 600 km [8]. However, massive MCC user equipments (UEs) in different applications exhibit various timeliness requirements for status updates. Recently, 3rd Generation Partnership Project (3GPP) Release 17 has discussed the access failure probability (AFP) and packet delay budget (PDB) requirements of the different MCC services for future non-terrestrial networks (NTN) [8]. Specifically, three types of timeliness requirements are considered in this paper: 1) timeliness stringent MCC UEs (TSUs) in the Intelligent Transport Systems (ITS), where PDB  $\leq 30$  ms and AFP  $\leq 10^{-5}$  [8]; 2) timeliness critical MCC UEs (TCUs), such as the Mission Critical user plane Push To Talk voice [9], requires PDB of 60 ms and the AFP as low as  $10^{-6} \sim 10^{-5}$ [8]; and 3) timeliness tolerant MCC UEs (TTUs), where the Mission Critical Data needs PDB 200 ms and the AFP  $10^{-6}$ [8], [10]. Moreover, the exponential growth of MCC UEs due to the emerging timeliness applications leads to severe UE collisions in massive access. Hence, designing a unequal timeliness (UT) protection massive access (UTMA) scheme to simultaneously satisfy various timeliness requirement, and resolve UE collisions in S-IoT holds significant practical value.

In addition, maximizing the throughput or minimizing delay cannot fully guarantee the timeliness requirements, because the delay only captures the latency from the transmission of a status update to its successful decoding at the satellite [11]. Thus, a related indicator named age of information (AoI) is proposed to study the timeliness of massive access at satellite [12]. The AoI is defined as the elapsed time since the latest resolved status update generated by UE [13], and the satellite calculates the average AoI (AAoI) by fairly measuring the AoI of each type of MCC UEs to get the timeliness of them. Then, we can design different UTMA schemes for

© 2024 The Authors. This work is licensed under a Creative Commons Attribution 4.0 License. For more information, see https://creativecommons.org/licenses/by/4.0/ each type of MCC UEs to satisfy their different timeliness requirements.

# A. Related Works

Considering the hundreds of kilometers between HTS and UEs, the conventional grant-based (GB) random access will result in huge communication overhead due to the propagation delay, which cannot guarantee the timeliness [14]. The grant-free (GF) random access can reduce the propagation delay and signaling overhead caused by conventional GB random access schemes. Therefore, GF random access is an inevitable choice for massive access in S-IoT [15]. However, GF random access would lead to serious collisions, because the UEs randomly choose pilot sequences and perform access [16], if two or more UEs select the same pilot, the collision occurs.

The authors in [17] and [18] studied non-orthogonal multiple access (NOMA) for random access in satellite communications, where NOMA provides a degree of freedom in the power domain by transmitting superimposed signals in the same time-frequency resource block, which can resolve UE collisions. However, the power domain NOMA cannot extend to more than three UEs in each group under the desired AFP in practical, which limits the usage in massive access of S-IoT.

In addition, several works to resolve the UE collisions are proposed in [12], [19], [20], [21], and [22] from a time domain perspective. The authors in [19] propose a random access scheme with quality-of-service (QoS) guarantees, in which UEs are grouped based on their QoS requirements, and multi-slot access frames are divided into multiple time slots to resolve UE collisions and satisfy the QoS requirements. The authors in [20] propose a random access scheme based on the irregular repeat-slot ALOHA (IRSA) protocol, where different priority UE groups have independent transmission slots. However, the above two schemes do not consider performance optimization for low-priority UE groups. A multi-slot pilot allocation (MSPA) random access scheme with unequal access latency (UAL) protection is proposed in [21] and [22], where the UEs are divided into groups based on their UAL requirements under certain AFP. With a precise design to allocate the number of access slots and pilots, the MSPA scheme can guarantee the QoS of high priority UE groups while enhancing the performance of lower priority UE groups. Further, a grant free age-optimal (GFAO) random access protocol is proposed in [12] for S-IoT, where the GFAO protocol can achieve the lowest AoI under certain AFP by adjusting the number of access slots in each frame. However, the timeliness is sacrificed for reliability in the above mentioned time domain multiply slots random access schemes, and they are difficult to meet the extremely timeliness requirements in MCC scenarios.

Recently, Polyanskiy et al. propose a T-fold code domain random access scheme to resolve UE collisions in unsourced random access [23], [24], [25]. The T-fold scheme relies on the concatenated codes, where the outer code can recover the collided messages, and the inner code is used for error correction. The inner code enables the base station (BS) to decode the modulo-2 sum of all codewords transmitted in the same time slot. When the number of collided UEs  $\leq T$ , the outer code can recover each message from the modulo-2 sum with zero error probability. However, the complexity of codebook in T-fold scheme would significantly increase with T, which limits the implementation in massive access. The authors in [26] proposed a LT-collision resolution GF random access (LT-GFRA) scheme for massive access, where a pilot set containing L orthogonal pilots combines a T-order codebook to resolve up to LT UE collisions, which shows the potential to achieve stringent timeliness for massive access in S-IoT.

## B. Contributions

In this paper, we design an UTMA scheme for MCC UEs in S-IoT, where the MCC UEs are grouped according to their different timeliness requirements. Then, we introduce a multi-dimensional codebook and orthogonal pilot set to resolve UE collisions, and design different UTMA schemes for each type of MCC UEs, which can guarantee the desired AFP and timeliness requirement simultaneously. The main contributions in this paper are concluded as follows.

- Unequal Timeliness Protection Massive Access Scheme: To the best of our knowledge, this is the first work on designing an UTMA scheme for MCC UEs in S-IoT. In our UTMA scheme, we group the TSUs, TCUs and TTUs into three priority groups according to their timeliness requirements, and each group is allocated different access stage and pilots, where each pilot corresponds to a T-order codebook. Specifically, we design three types of UTMA schemes: 1) Independent successive UTMA (IS-UTMA), where each group performs random access in successive time slot according to its priority; 2) Extended cognitive offloading UTMA (ECO-UTMA), where part of TTUs can offload in the TCUs access stage; and 3) Independent cognitive offloading UTMA (ICO-UTMA), where part of TTUs can offload in the TCUs access stage, and pilot set for both types of UEs are pre-allocated in advance.
- Analysis for UTMA Scheme: Through the analysis of UE collisions and decoding failure probability under the *T*-order codebook and *L* orthogonal pilots, we derive the closed-form expressions of AFP of each group under the shadowed-Rician fading channel for three UTMA schemes. Then, with the help of theoretical results of AFP, we model the timeliness of each group via AoI and track the instantaneous AoI evolution process to derive the closed-form expression of the AAoI. Monte Carlo simulation results validate the accuracy of the theoretical derivations.
- Optimization and Validation of UTMA Scheme: To meet the timeliness requirements of TCUs group and improve the AAoI of TTUs group under the desired AFP, we construct the joint parameter optimization problems of AAoI for the ECO- and ICO-UTMA schemes under diverse AFP constraints, number of pilots and number of UEs. To solve the non-convex joint parameter optimization problems, we decompose each optimization problem into two simplified sub-problems to obtain the optimal parameters for the ECO- and ICO-UTMA schemes. Simulation



Fig. 1. The system model of unequal timeliness protection massive access for MCC UEs under a LEO HTS.

results show that the proposed UTMA schemes can provide UT protection for each group by resolve UE collisions in code domain, and exhibit significantly lower AAoI than existing scheme.

The remainder of this paper is organized as follows. Section II shows the system model and the principles of UTMA scheme. Section III describes the AoI and AFP analysis for the UTMA scheme. The performance optimization for UTMA scheme is depicted in section IV. Section V gives the simulation results and Section VI exhibits the conclusion.

# II. SYSTEM MODEL AND UTMA SCHEME

In this section, we first present the system model of the proposed UTMA scheme. Then, we concretely describe the three UTMA schemes, including the procedure of UTMA random access scheme.

#### A. System Model

As shown in Fig. 1, we consider a LEO S-IoT system with wide coverage of K MCC UEs, where the orbit type is circular orbiting around the Earth in a Walker Delta constellation [5], and a 0.5 m electronic phased array antenna can be utilized in Ka-band uplink communications for UEs [27]. Considering that the altitude of LEO HTS is set as 600 km with antenna gain no less than 50 dBi [27], the worst two-way propagation delay is expected to be 26 ms [8]. Without loss of generality, the covered MCC UEs are grouped into three priority UE groups according to their access timeliness requirements: TSUs, TCUs and TTUs, where the PDB of TSUs, TCUs and TTUs are set as 30 ms, 60 ms and 200 ms, respectively [8], [9], [10]. The access frame is divided into three access stages denoted as  $N_1$ ,  $N_2$ , and  $N_3$ , and each access stage equals to one time slot. Assume that the length of time slot equals to the duration from an activated UE generating a status update packet to the HTS decoding the packet. Thus, due to the PDB requirement of each type MCC UEs, the length of one access frame and one time slot are set as 90 ms and 30 ms, respectively [8], [9], [10]. Moreover, the number of activated UEs in each group is denoted as  $K_{TSUs}$ ,  $K_{TCUs}$  and  $K_{TTUs}$ correspondingly.

Considering the multipath and shadow fading effects caused by the surrounding environment, such as buildings, trees, and 3213

terrain [28], we utilize the widely-used shadowed-Rician fading channel to model the satellite-to-ground link [4], [29], [30], [31], which aligns closely with the observed land mobile satellite (LMS) channel data and provides substantial analytical and numerical advantages for predicting system performance. Moreover, the terrestrial MCC UEs are quasi-static and the Doppler effects in our system can be modeled as a constant multiplicator factor [32], thus the LEO HTS can utilize a guard band that double than the Doppler shifts to relieve the influence on our system [14]. The probability density function (PDF) of channel power gain  $r = |h|^2$  is as follows [29],

$$f(r) = \left(\frac{2bm}{2bm+\Omega}\right)^m \frac{1}{2b} \exp\left(-\frac{r}{2b}\right)$$
  
$$\cdot_1 F_1\left(m, 1, \frac{\Omega r}{2b(2bm+\Omega)}\right), \tag{1}$$

where b is the average power of multi-path components, m is Nakagami-m parameter,  $\Omega$  is the average power of line of sight (LoS), and  $_1F_1(a, b, c)$  is confluent hypergeometric function.

The Zadoff-Chu (ZC)sequence has excellent auto-correction and cross-correlation properties along with its low peak-to-average power ratio [33], which leads to an outstanding detection capability in NTN [34], [35]. Thus, we utilize ZC sequence as pilot sequence to estimate channel gain and synchronize. We denote a pilot set of L orthogonal pilot sequences as  $\mathbf{D} = \{\xi_1, \xi_2, \xi_3, \dots, \xi_L\}$  in our system, and the activated UE l can uniformly random select a pilot  $\xi_i$  from the allocated pilots. Then, the activated UE l encodes its status update by a T-order codebook. The design of T-order concatenated code is from [36], where the Bose-Chaudhuri-Hocquenghem (BCH) outer code can recover up to T UE collisions on any pilot, and the low density parity check (LDPC) inner code is used for channel error correction. Thus, the HTS can recover up to LT UEs in one time slot [26].

Therefore, assuming that  $\mathbf{Z}_j$  is the set of UEs who select  $\xi_j$  in a time slot, we can divide the pilots into four cases as follows:

- 1) Singleton UE pilot:  $|\mathbf{Z}_j| = 1$ ;
- 2) Fully decodable collision pilot:  $2 \le |\mathbf{Z}_j| \le T$ ;
- *3) Partially decodable collision pilot:*  $|\mathbf{Z}_{i}| > T$ ;

4) Empty pilot:  $|\mathbf{Z}_j| = 0$ , which can be perfectly detected by the HTS and is ignored in the following.

Let  $X_l$  denote the status update of UE l selected  $\xi_j$  and encoded by the *T*-order codebook,  $Y_d$  denotes the status update packet received by HTS, and we have:

$$Y_d = \sum_{j=1}^{L} \sum_{l \in \mathbf{Z}_j} \sqrt{P_T} h_l \left( X_l \otimes \xi_j \right) + N, \tag{2}$$

where  $P_T$  is the transmission power,  $h_l$  is the channel gain,  $\otimes$  denotes the Kronecker product and  $N \sim C\mathcal{N}(0, \sigma^2)$  represents the additive white Gaussian noise (AWGN). Then, the HTS performs pilot detection on  $Y_d$ , and the status updates over pilot  $\xi_i$  is

$$Y_d^j = \sum_{l \in \mathbf{Z}_j} \sqrt{P_T} h_l X_l + N_d, \tag{3}$$



Fig. 2. Resource scheduling logic diagram of three UTMA schemes, where  $P_{us}'$  and  $P_{us}$  are the AFP of offloaded TTUs in  $N_2$  for ECO- and ICO-UTMA scheme, respectively.

and the channel estimation for  $\xi_j$  via the least-squares (LS) algorithm is

$$\hat{h}_{\xi_j} = \sum_{l \in \mathbf{Z}_j} h_l + \hat{N}.$$
(4)

Then, the HTS first performs successive cancellation (SC) to recover the encoded status update of the strongest UE in the  $Y_d^j$ . Hence, for v < T, in the *v*-th iteration of SC, the signal to interference plus noise ratio (SINR) is:

$$\operatorname{SINR}_{v,\operatorname{SC}} = \frac{P_T |h_v|^2}{\sum_{i=1}^{v-1} \delta P_T |h_i|^2 + \sum_{i=v+1}^{|\mathbf{Z}_j|} P_T |h_i|^2 + \sigma^2}, \quad (5)$$

where  $\delta$  is the residual interference power coefficient. If the *v*-th SC is successful, the encoded status update of this UE will be subtracted from  $Y_d^j$  and the HTS will perform decoding to recover the corresponding packet. Otherwise, the HTS will perform joint decoding (JD) on the remaining signal, and the corresponding SINR is:

$$SINR_{v,JD} = \frac{\sum_{i=v}^{|\mathbf{Z}_j|} P_T |h_i|^2}{\sum_{i=1}^{v-1} \delta P_T |h_i|^2 + \sigma^2}.$$
 (6)

Note that the encoding of the *T*-order codebook only consists of mapping a message to a primitive element  $\alpha$  in  $GF(2^m)$ , and then computing its odd power  $(\alpha, \alpha^3, \ldots, \alpha^{2T-1})$ , which requires  $\mathcal{O}(T^2)$  multiplications [25]. Further, the decoding of the received status updates is similar to standard Gorenstein Peterson Zierler (GPZ) decoding of the BCH code, and the decoding complexity of the SC then JD procedure is  $\mathcal{O}(T + \rho kT \log^2 T \log \log T)$ [R35], where  $\rho$  denotes the normalized stopping set proportion of the SC decoder and k denotes the length of message. Therefore, the complexity of the proposed UTMA scheme can be  $\mathcal{O}(T + T^2 + \rho kT \log^2 T \log \log T)$ . In addition, the AFP of above SC then JD procedure for  $Y_d^j$  is analyzed in Section III-B.

#### B. The Proposed UTMA Schemes

As shown in Fig. 2, the activated MCC UEs are grouped into TSUs, TCUs and TTUs according to their access timeliness requirements, and perform access in three access stage  $N_1, N_2, N_3$  in our UTMA scheme. At the beginning of each frame, the HTS broadcasts a control signal to activated MCC UEs for estimating the average channel gain and synchronization for the GF random access. In the independent successive (IS)-UTMA, each group performs random access in successive time slot according to its priority as shown in Fig. 2(a), and in the two cognitive offloading (CO)-UTMA schemes, part of TTUs can offload in the TCUs access stage as shown in Fig. 2(b) and (c), which can resolve the UE collisions in  $N_3$  and improve the overall access timeliness of TTUs. Note that the pilot set **D** is pre-allocated for TCUs and TTUs in ICO-UTMA scheme.

1) In  $N_1$ : Only TSUs can perform access to ensure stringent access timeliness requirement and randomly select pilots from **D** in three types UTMA schemes. At the end of  $N_1$ , the HTS decodes the received status updates.

2) In  $N_2$ : There are three different cases in this access stage, and at the end of  $N_2$ , the HTS decodes the received status updates.

**Case 1** In the IS-UTMA scheme, only TCUs perform access and can randomly select pilots from **D**.

**Case 2** In the ECO-UTMA scheme, all TCUs and  $K'_{31}$  TTUs perform access and randomly select pilots from **D**, and the ratio of offloading TTUs is  $\beta' = \frac{K'_{31}}{K_{\text{TTUs}}}$ .

**Case 3** In the ICO-UTMA scheme, **D** is divide into  $\mathbf{D}_1 = \{\xi_1, \xi_2, \xi_3, \dots, \xi_p\}$  and  $\mathbf{D}_2 = \{\xi_{p+1}, \xi_{p+2}, \xi_{p+3}, \dots, \xi_L\}$ , where  $\alpha = \frac{p}{L}$  is the pilot allocation ratio, and all TCUs and  $\beta = \frac{K_{31}}{K_{\text{TTUS}}}$  of TTUs perform access and they randomly select pilots from  $\mathbf{D}_1$  and  $\mathbf{D}_2$ , respectively.

3) In  $N_3$ : All the activated TTUs that failed to access and unscheduled in  $N_2$  perform access and randomly select pilots from **D**, and the HTS decodes the received status updates at the end of  $N_3$ .

# C. Procedure of UTMA Random Access Scheme

Fig. 3 shows four types of 2-step GF random access procedure in different access stages corresponding to Fig. 2 with the same mark of cases, for example, the three access stages of IS-UTMA are marked the red solid circle as shown



Fig. 3. Four types of 2-step GF random access procedure in the *i*-th frame in our UTMA scheme for  $N_1$ ,  $N_2$  and  $N_3$ , where the marks on different types are corresponding to Fig. 2 with the same mark of cases.

in Fig. 2(a), and their random access procedure in each access stage are the same as shown in Fig. 3 (a) marked with the red solid circle. Moreover, for the CO-UTMA scheme, the random access procedure in each access stage is introduced as follows.

**Step 1** As shown in Fig. 2(a), each activated TSU uniformly random selects a pilot from **D** with equal probability  $\frac{1}{L}$ , and utilizes the *T*-order codebook to encoding its status update at the beginning of  $N_1$ . Then, the TSUs send the selected pilots and the encoded status updates to HTS.

**Step 2** The HTS first performs pilot detection and channel estimation based on the received pilot signal. Then, the HTS decodes the received status updates from each pilot by the SC then JD decoder at the end of  $N_1$ , and recovers up to T TSUs collisions on each detected pilot. Once the HTS finishes the decoding, it broadcasts a feedback of the decoding states to all TSUs.

**Step 3** Similar to Step 1, at the beginning of  $N_2$ , the activated TCUs and the offloading TTUs uniformly random select a pilot from **D** in ECO-UTMA scheme as shown in Fig. 2(b), or from **D**<sub>1</sub> or **D**<sub>2</sub> in ICO-UTMA scheme, respectively, as shown in Fig. 2(c). Then, the TCUs and offloading TTUs send the selected pilots and the encoded status updates to HTS.

**Step 4** Similar to Step 2, the HTS decodes the received status updates at the end of  $N_2$ , and broadcasts a feedback of the decoding states to all TCUs and TTUs.

**Step 5** In the CO-UTMA scheme, only the activated TTUs that failed to access and unscheduled in  $N_2$  perform access in  $N_3$ . We assume that  $P_{us}'$  and  $P_{us}$  are the AFP of the offloaded TTUs in  $N_2$  for ECO- and ICO-UTMA schemes, respectively. Thus,  $\beta' P_{us}' + (1 - \beta') K_{TTUs}$  and  $\beta P_{us} + (1 - \beta) K_{TTUs}$  TTUs uniformly random select pilots from **D** and encodes their status updates, respectively. Then, the selected pilots and the encoded status updates are sent to the HTS.

**Step 6** Similar to the Step 2, the HTS decodes the received status updates at the end of  $N_3$  and broadcasts the decoding states to all TTUs.

# III. PERFORMANCE ANALYSIS OF UTMA SCHEME

In this section, we present the analysis of the AAoI and AFP of each MCC UE group for three UTMA schemes. First, we utilize AoI to model the timeliness of each group. By analyzing the UE collisions and decoding failure probability, we derive the closed-form expressions of AFP for each group under the shadowed-Rician fading channel in three UTMA schemes. Further, we derive the closed-form expressions of AAoI by tracing the AFP and instantaneous AoI.

# A. AoI Evolution in UTMA Scheme

Recall the instantaneous AoI observed at the receiver is defined as the difference between the current time and the generation time of the last recovered status update at the source. Therefore, we define  $G_l(t)$  as the generation timestamp of the last status update from UE l that recovered by the HTS at time t, where t = 0, 1, 2, ... is normalized to one frame. Then, the instantaneous AoI  $\Lambda_l(t)$  of UE l observed at the HTS can be expressed as follows [38]:

$$\Lambda_l(t) = t - G_l(t). \tag{7}$$

In our UTMA scheme, an access frame is divided into three access stages, and each access stage equals to one time slot. Therefore, we assume that  $\Lambda_l^q(f)$  represents the instantaneous AoI observed at the HTS for the UE l of group q in the f-th frame, where  $q \in \{\text{TSUs}, \text{TCUs}, \text{TTUs}\}$ . Fig. 4 shows the evolution of instantaneous AoI for UE l in different cases, and the analysis is as follows:

1) TSUs: The TSUs generate and send status updates at the beginning of each frame, and the HTS decodes the status updates at the end of  $N_1$  to ensure the timeliness of TSUs. As shown in Fig. 4, a TSU l is failed to access in the first frame and  $\Lambda_l^{\text{TSUs}}$  increases with t, and it successfully accesses in  $N_1$  of the second frame, and  $\Lambda_l^{\text{TSUs}}$  is set to 1 at t = 4. Define  $D_l^q(f, N_j)$  as the state value of UE l of group q in the access stage  $N_j$  of the f-th frame. If the activated TSU lsuccessfully accesses,  $D_l^q = 0$ , otherwise,  $D_l^q = 1$ . Therefore, the instantaneous AoI evolution of the TSU l in the f-th frame can be expressed as follows:

$$\Lambda_l^{\text{TSUs}}(f) = \begin{cases} 1, & \text{if } D_l^{\text{TSUs}}(f, N_1) = 0\\ \Lambda_l^{\text{TSUs}}(f-1) + 3, & \text{if } D_l^{\text{TSUs}}(f, N_1) = 1. \end{cases}$$
(8)

2) TCUs: The activated TCUs generate status updates at the beginning of each frame and transmits at the beginning of  $N_2$ , and the HTS decodes the status update sent by the TCU at the end of  $N_2$ . As shown in Fig. 4, a TCU *l* successfully accesses in  $N_2$  of the first and third frames and the corresponding  $\Lambda_l^{TCUs}$ 



Fig. 4. The evolution of instantaneous AoI observed at the HTS for UE l in different cases.

is set to 2 at t = 2 and t = 8, respectively, and when TCU l is inactivated or fail to access in the second frame,  $\Lambda_l^{\text{TSUs}}$  increases with t. Therefore, if the TCU l successfully accesses in  $N_2$  of the f-th frame,  $\Lambda_l^{\text{TCUs}}(f)$  is set to 2 at the end of  $N_2$ . Otherwise,  $\Lambda_l^{\text{TCUs}}$  increases with t. The instantaneous AoI evolution of the TCU l in the f-th frame can be expressed as:

$$\Lambda_l^{\text{TCUs}}(f) = \begin{cases} 2, & \text{if } D_l^{\text{TCUs}}(f, N_2) = 0\\ \Lambda_l^{\text{TCUs}}(f-1) + 3, & \text{if } D_l^{\text{TCUs}}(f, N_2) = 1. \end{cases}$$
(9)

3) TTUs: The instantaneous AoI evolution of TTU l can be divided into four different cases:

**Case a** The TTU l is offloading to send status update in  $N_2$  of the f-th frame and successfully accesses, the corresponding  $\Lambda_l^{\text{TTUs}}(f) = 2$  at the end of  $N_2$ , as the AoI of scheduled TTU  $\Lambda_l^{\text{TTUs}}(1) = 2$  at t = 2 as shown in Fig. 4.

**Case b** The TTU *l* successfully accesses in  $N_3$  of the *f*-th frame, and  $\Lambda_l^{\text{TTUs}}(f) = 3$  at the end of  $N_3$ , as the AoI of unscheduled TTU  $\Lambda_l^{\text{TTUs}}(1) = 3$  at t = 3 as shown in Fig. 4.

**Case c** The TTU l successfully accesses in  $N_2$  of the (f-1)-th frame and fails to access in the f-th frame,  $\Lambda_l^{\text{TTUs}}(f) = \Lambda_l^{\text{TTUs}}(f-1) + 4$ , as the AoI of TTU  $\Lambda_l^{\text{TTUs}}(2) = \Lambda_l^{\text{TTUs}}(1) + 4$  at t = 6 as shown in Fig. 4.

**Case d** The TTU l is unscheduled or failed to access in  $N_2$  in the (f-1)-th frame, and also fails to access in the f-th frame,  $\Lambda_l^{\text{TTUs}}(f) = \Lambda_l^{\text{TTUs}}(f-1) + 3$ , as the AoI of TTU  $\Lambda_l^{\text{TTUs}}(3) = \Lambda_l^{\text{TTUs}}(2) + 3$  at t = 9 as shown in Fig. 4.

Therefore, the instantaneous AoI evolution of the TTU l in the f-th frame can be expressed as:

$$\begin{split} \Lambda_l^{\rm TTUs}(f) = & \\ \begin{cases} 2, & \text{if } D_l^{\rm TTUs}(f,N_2) = 0\\ 3, & \text{if } D_l^{\rm TTUs}(f,N_3) = 0\\ \Lambda_l^{\rm TTUs}(f-1) + 4, & \text{if } D_l^{\rm TTUs}(f-1,N_2) = 0\\ & \text{and } D_l^{\rm TTUs}(f) = 1\\ \Lambda_l^{\rm TTUs}(f-1) + 3, & \text{otherwise.} \end{cases} \end{split}$$

#### B. Derivation of AFP in UTMA Scheme

As mentioned in Section II-A, the pilots can be divided into four cases: 1) Singleton UE pilot; 2) Fully decodable collision pilot; 3) Partially decodable collision pilot; 4) Empty pilot. For T = 2, denote  $\gamma$  as the decoding threshold, if the UE *l* selects  $\xi_j$  and fails to access, it may be caused by one of the following three cases.

**Case I**  $\xi_j$  is a singleton UE pilot, if  $SINR_{1,SC} < \gamma$ , decoding is failure and UE *l* fails to access.

**Case II**  $\xi_j$  is a fully decodable collision pilot, i.e., UE land UE p both select  $\xi_j$ . If  $|h_l|^2 > |h_p|^2$ , the UE l fails to access due to  $SINR_{1,\text{JD}} < \gamma$ . Otherwise,  $SINR_{2,\text{SC}} < \gamma$  for  $|h_l|^2 < |h_p|^2$ .

**Case III**  $\xi_j$  is partially decodable collision pilot, i.e., the UE l shares  $\xi_j$  with two or more UEs. Note that the HTS decodes the status updates on  $\xi_j$  in descending order according to their channel gain, and we can assume that the channel gain of UE l is ranked at v-th. If  $|h_l|^2$  is not the lowest, then the UE l fails to access due to  $SINR_{v,\text{JD}} < \gamma$ . Otherwise,  $SINR_{v,\text{SC}} < \gamma$  for UE l has the lowest  $|h_l|^2$ .

Therefore, the AFP of UE l can be derived based on the above three cases, i.e.,  $|\mathbf{Z}_j| = 1$ ,  $|\mathbf{Z}_j| = 2$ , and  $|\mathbf{Z}_j| > 2$ .

1) 
$$|\mathbf{Z}_j| = 1$$
: The probability of **Case I** is as follows:

$$\Pr\left(|\mathbf{Z}_j|=1\right) = \binom{K}{1} \left(\frac{1}{L}\right) \left(1 - \frac{1}{L}\right)^{K-1}.$$
 (11)

In **Case I**, the decoding fails when  $SINR_{1,SC} \leq \gamma$ , where  $\gamma = 2^R - 1$  and R is the inner code rate. To facilitate the subsequent analysis, the PDF of shadowed-Rician channel in Eq.(1) can be simplified as follows:

$$f(r) = \omega e^{-\eta r},\tag{12}$$

where  $\omega = \frac{P_T}{2b\sigma^2} (\frac{2bm}{2bm+\Omega})^m$ ,  $\eta = \frac{mP_T}{(2bm+\Omega)\sigma^2}$ . Therefore, by setting b = 0.063, m = 1,  $\Omega = 0.000897$  [39], the decoding failure probability is:

$$\Pr\left(\frac{P_T|h_l|^2}{\sigma^2} < \gamma\right) = \Pr\left(|h_l|^2 < \epsilon\gamma\right) = 1 - e^{-w\epsilon\gamma}, \quad (13)$$

where  $\epsilon = \frac{\sigma^2}{P_T}$ . Thus, combining the UE collisions and decoding failure probability, the AFP of UE *l* under  $|\mathbf{Z}_j| = 1$  is:

$$AFP_{l,|\mathbf{Z}_j|=1} = \Pr\left(|\mathbf{Z}_j|=1\right)\Pr\left(\frac{P_T|h_l|^2}{\sigma^2} < \gamma\right)$$
$$= \frac{K(L-1)^{K-1}\left[1 - \exp\left(-\frac{w\gamma}{\epsilon}\right)\right]}{L^K}.$$
 (14)

2)  $|\mathbf{Z}_j| = 2$ : In **Case II**, the probability of both UEs choosing  $\xi_j$  is:

$$\Pr\left(|\mathbf{Z}_j|=2\right) = \binom{K}{2} \left(\frac{1}{L}\right)^2 \left(1-\frac{1}{L}\right)^{K-2},\qquad(15)$$

and the decoding failure probability is:

$$\Pr\left(\frac{P_{T}|h_{1}|^{2}}{P_{T}|h_{2}|^{2} + \sigma^{2}} < \gamma, \frac{\sum_{i=1}^{2} P_{T}|h_{i}|^{2}}{\sigma^{2}} < \gamma\right) + \Pr\left(\frac{P_{T}|h_{2}|^{2}}{\delta P_{T}|h_{1}|^{2} + \sigma^{2}} < \gamma\right) = \Pr\left(|h_{1}|^{2} + |h_{2}|^{2} < \epsilon\gamma\right) + \Pr\left(|h_{2}|^{2} - \delta\gamma|h_{1}|^{2} < \epsilon\gamma\right),$$
(16)

where  $|h_1|^2 + |h_2|^2 \sim Erlang(2, w)$ . By deriving the PDF of  $|h_2|^2 - \delta\gamma |h_1|^2$ , the AFP can be obtained for  $|\mathbf{Z}_j| = 2$ :

$$AFP_{l,|\mathbf{Z}_j|=2} = \frac{\binom{K}{2}(L-1)^{K-2}}{L^K} \cdot \left[2 - \left(1 + \frac{w\gamma}{\epsilon} + \frac{1}{1+\delta\gamma}\right) \exp\left(-\frac{w\gamma}{\epsilon}\right)\right].$$
(17)

3)  $|\mathbf{Z}_j| > 2$ : In **Case III**, there are  $|\mathbf{Z}_j| = k$  ( $k = 3, 4, \ldots, K$ ) UEs selecting  $\xi_j$ , and UE l is ranked at (v = k - i + 1)-th ( $i = 1, 2, \ldots, k$ ). In this case, there are (k - i) UEs successfully access, and the UE l and i UEs with worese channel gains fails to access, and the AFP for UE l is:

$$\sum_{k=3}^{K} \Pr\left(|\mathbf{Z}_{j}|=k\right) \sum_{i=1}^{k} \Pr\left(i \text{ UEs failed to decode}\right), \quad (18)$$

where the probability of k UEs choosing the same pilot  $\xi_j$  is:

$$\Pr(|\mathbf{Z}_j| = k) = \binom{K}{k} \left(\frac{1}{L}\right)^k \left(1 - \frac{1}{L}\right)^{K-k}.$$
 (19)

When k UEs choose  $\xi_j$ , the decoding failure probability of  $i(i \neq k)$  UEs is

$$\Pr\left(\frac{P_{T}|h_{k-i+1}|^{2}}{\sum_{j=1}^{k-i}\delta P_{T}|h_{j}|^{2} + \sum_{j=k-i+2}^{k}P_{T}|h_{j}|^{2} + \sigma^{2}} < \gamma\right)$$
$$= \Pr\left(-\delta\gamma|h_{1}|^{2} - \dots - \delta\gamma|h_{k-i}|^{2} + \gamma\right)$$

$$|h_{k-i+1}|^2 + \dots + |h_k|^2 < \epsilon \gamma \Big), \tag{20}$$

where 
$$X_t = |h_t|^2 (t = k - i + 1, ..., k) \sim \exp(\frac{1}{w})$$
 and  $Y_u = -\delta\gamma |h_u|^2 (t = 1, ..., k - i) \sim \exp(\frac{\delta\gamma}{w})$ . Therefore, we can derive  $H_i = \sum_{i=k-i+1}^k X_i \sim Erlang(i, w), \ G_{k-i} = \sum_{i=1}^{k-i} Y_i \sim Erlang(k - i, \frac{w}{\delta\gamma})$ .

Let  $Z = H_i + G_{k-i}$ , which can be derived by taking the Laplace transform of the PDF of  $H_i$  and  $G_{k-i}$  due to they are independent of each other. Then, we can obtain f(z)via the Laplace inverse transform [40]. Thus, we can derive the closed-form of decoding failure probability in Eq.(20) as follows,

 $\Pr(i \text{ UEs failed to decode}) =$ 

$$\sum_{j=1}^{k-i} \frac{\binom{k-j-i}{k-j-1} (\delta\gamma)^{i}}{(1+\delta\gamma)^{k-j}} + \sum_{j=1}^{i} \frac{\binom{k-j-i}{i-j} (\delta\gamma)^{i-j}}{(1+\delta\gamma)^{k-j}} \cdot \left[1 - \exp(-\frac{w\gamma}{\epsilon}) \sum_{m=0}^{j-1} \frac{(\frac{w\gamma}{\epsilon})^{m}}{\Gamma(m)}\right], \quad (21)$$

where  $\Gamma(\cdot)$  is the incomplete Gamma function. Similarly, we can derive the decoding failure probability when i = k as:

$$\Pr\left(\frac{P_T|h_1|^2}{\sum\limits_{j=2}^k P_T|h_j|^2 + \sigma^2} < \gamma, \frac{\sum\limits_{j=1}^k P_T|h_j|^2}{\sigma^2} < \gamma\right)$$
$$= 1 - \exp\left(-\frac{w\gamma}{\epsilon}\right) \sum\limits_{m=0}^{k-1} \frac{\left(\frac{w\gamma}{\epsilon}\right)^m}{\Gamma(m)}.$$
 (22)

Thus, the AFP of Case III is:

$$AFP_{l,|\mathbf{Z}_{j}|>2} = \sum_{i=3}^{K} \frac{\binom{K}{k}(L-1)^{K-k}}{L^{K}} \cdot \left\{ \left\{ \sum_{i=1}^{k-1} \left\{ \sum_{j=1}^{k-i} \frac{\binom{k-j-i}{k-j-1}(\delta\gamma)^{i}}{(1+\delta\gamma)^{k-j}} + \right. \\ \left. \sum_{j=1}^{i} \frac{\binom{(k-j-i)}{i-j}(\delta\gamma)^{i-j}}{(1+\delta\gamma)^{k-j}} \right. \\ \left. \cdot \left[ 1 - \exp\left(-\frac{w\gamma}{\epsilon}\right) \sum_{m=0}^{j-1} \frac{\left(\frac{w\gamma}{\epsilon}\right)^{m}}{\Gamma(m)} \right] \right\} \right\} \\ \left. + \left[ 1 - \exp\left(-\frac{w\gamma}{\epsilon}\right) \sum_{m=0}^{k-1} \frac{\left(\frac{w\gamma}{\epsilon}\right)^{m}}{\Gamma(m)} \right] \right\}.$$
(23)

Further, by combining Eq. (14), Eq. (17) and Eq. (23), we can derive the closed-form expression of AFP for UE lin one time slot as Eq. (24), shown at the bottom of the next page. Then, as shown in Fig. 2, by substituting the number of activated UEs and available pilots in different access stages into Eq. (24), the AFP of UE l for each group in three UTMA schemes can be derived as Eq. (25), Eq. (26) and Eq. (27), shown at the bottom of the next page., respectively, where  $L^{(q)}$  denotes the number of available pilots for group q in their access stages.

#### C. Derivation of AAoI in UTMA Scheme

Assuming F is the number of access frames and  $H_q$  is the number of UEs in group q, thus the AAoI of group q can be expressed as:

$$\Delta_q = \frac{\sum_{j=1}^{H_q} \sum_{f=1}^F \Lambda_l^q(f)}{H_q F}.$$
(28)

Utilizing the theoretical results of AFP in each group p for three UTMA schemes, we can derive the corresponding AAoI. Let  $P_{s,l}^q$  denote the successful access probability of UE l, and  $P_{us,l}^q$  is the probability of inactivated or failure to access of UE l. Then, we have  $P_{s,l}^q$  for UE l of group q for each UTMA scheme as:

$$P_{s,l}^{q} = 1 - P_{us,l}^{q} = \lambda_{q} (1 - AFP_{l}^{q}),$$
(29)

where  $\lambda_q = \frac{K_q}{H_q}$  is the active probability of group q. Therefore, the AoI of TSU and TCU in the f-th frame can be expressed as follows:

$$\Lambda_{l}^{\text{TSUs}}(f) = \sum_{x=1}^{f} (3x-2) P_{s,l}^{\text{TSUs}} \left( P_{us,l}^{\text{TSUs}} \right)^{x-1}, \qquad (30a)$$

and

$$\Lambda_{l}^{\text{TCUs}}(f) = \sum_{x=1}^{f} (3x-1) P_{s,l}^{\text{TCUs}} \left( P_{us,l}^{\text{TCUs}} \right)^{x-1}.$$
 (30b)

Then, consider the AoI of TTU L, let  $P_{ss2,l}^{\text{TTUs}} = \lambda_{\text{TTUs}}\beta(1 - AFP_{l,2}^{\text{TTUs}})$  denote the probability of TTU l successfully

accessing in  $N_2$ ,  $P_{ss3,l}^{\text{TTUs}} = \lambda_{\text{TTUs}} \beta AF P_{l,2}^{\text{TTUs}} (1 - AF P_{l,3}^{\text{TTUs}})$  is the probability of TTU l failed to access in  $N_2$  but successfully accessing in  $N_3$ , and  $P_{us3,l}^{\text{TTUs}} = \lambda_{\text{TTUs}} (1 - \beta) (1 - AF P_{l,3}^{\text{TTUs}})$  is the probability of TTU l unscheduled in  $N_2$  but successfully accessing in  $N_3$ . In addition, we assume that  $P_{s3,l}^{\text{TTUs}} = P_{ss3,l}^{\text{TTUs}} + P_{us3,j}^{\text{TTUs}}$  is the probability of TTU l successfully access in  $N_3$ . Thus, the AoI of TTU l in three UTMA schemes are as follows:

1) IS-UTMA:

$$\Lambda_l^{\text{TTUs}}(f) = \sum_{x=1}^f 3x P_{s,l}^{\text{TTUs}} \left( P_{us,l}^{\text{TTUs}} \right)^{x-1}, \qquad (30c)$$

# 2) ECO- and ICO-UTMA:

$$\begin{split} \Lambda_{l}^{\text{ITUS}}(f) &= \\ \begin{cases} 2P_{ss2,l}^{\text{TTUS}} + 3(1 - P_{ss2,l}^{\text{TTUS}}), & f = 1, \\ 2P_{ss2,l}^{\text{TTUS}} + 3P_{s3,l}^{\text{TTUS}} + 6(P_{us,l}^{\text{TTUS}})^{2}, & f = 2, \\ 2P_{ss2,l}^{\text{TTUS}} + 3P_{s3,l}^{\text{TTUS}} + 3f(P_{us,l}^{\text{TTUS}})^{f-1} & \\ f^{-1} &+ [\sum_{x=2}^{f} 3x(P_{ss2,l} + P_{s3,l}^{\text{TTUS}})(P_{us,l}^{\text{TTUS}})^{x-1}], & f \ge 3. \end{split}$$
(30d)

By substituting Eq. (30) into Eq. (28), we have the closed-form expressions of AAoI for each group in three UTMA schemes as shown in Eq. (31), Eq. (32) and Eq. (33), at the bottom of the next page.

#### IV. OPTIMIZATION OF UTMA SCHEME

In this section, we first construct the joint parameter optimization problems of AAoI for ECO- and ICO-UTMA

$$AFP_{l} = \frac{K(L-1)^{K-1} \left[1 - \exp\left(-\frac{w\gamma}{\epsilon}\right)\right] + {K \choose 2} (L-1)^{K-2} \cdot \left[2 - \left(1 + \frac{w\gamma}{\epsilon} + \frac{1}{1+\delta\gamma}\right) \exp\left(-\frac{w\gamma}{\epsilon}\right)\right]}{L^{K}} + \sum_{i=3}^{K} \frac{{K \choose k} (L-1)^{K-k}}{L^{K}} \cdot \left\{\left\{\sum_{i=1}^{k-1} \left\{\sum_{j=1}^{k-i} \frac{{k-j-i \choose k-j-1} (\delta\gamma)^{i}}{(1+\delta\gamma)^{k-j}} + \sum_{j=1}^{i} \frac{{k-j-i \choose i-j} (\delta\gamma)^{i-j}}{(1+\delta\gamma)^{k-j}} \right. + \left. \left. \left\{1 - \exp\left(-\frac{w\gamma}{\epsilon}\right) \sum_{m=0}^{j-1} \frac{{w\gamma \choose \epsilon}^{m}}{\Gamma(m)}\right]\right\}\right\} + \left[1 - \exp\left(-\frac{w\gamma}{\epsilon}\right) \sum_{m=0}^{k-1} \frac{{(w\gamma)^{m}}}{\Gamma(m)}\right]\right\}.$$

$$(24)$$

1) **IS-UTMA:** 

$$AFP_l^q = AFP_l|_{K=K_q, L=L^{(q)}} \left( q \in \{ \text{TSUs, TCUs, TTUs} \} \right).$$
(25)

# 2) ECO-UTMA:

$$AFP_{l}^{\text{TSUs}} = AFP_{l}|_{K=K_{\text{TSUs}}},$$

$$AFP_{l}^{\text{TCUs}} = AFP_{l}|_{K=K_{\text{TCUs}}+\beta K_{\text{TTUs}}},$$

$$AFP_{l}^{\text{TTUs}} = (1 + \beta AFP_{l}|_{K=K_{\text{TCUs}}+\beta K_{\text{TTUs}}} - \beta) \cdot AFP_{l}|_{K=\beta K_{\text{TTUs}} \cdot AFP_{l}|_{K=K_{\text{TCUs}}+\beta K_{\text{TTUs}}} + (1-\beta)K_{\text{TTUs}}}.$$
(26)

# 3) **ICO-UTMA:**

$$AFP_l^q = AFP_l|_{K=K_q, L=L^{(q)}} \left( q \in \{ \text{TSUs, TCUs} \} \right),$$

$$AFP_l^{\text{TTUs}} = \left( 1 + \beta AFP_l|_{K=\beta K_{\text{TTUs}}, L=(1-\alpha)L} - \beta \right) \cdot AFP_l|_{K=\beta K_{\text{TTUs}} \cdot AFP_l|_{K=\beta K_{\text{TTUs}}, L=(1-\alpha)L} + (1-\beta)K_{\text{TTUs}}.$$
(27)

schemes under diverse AFP constraints, number of pilots and MCC UEs. Then, we decompose each optimization problem into two simplified sub-problems to obtain the optimal parameters for the ECO- and ICO-UTMA schemes. In practical, the related data is collected by the HTS and the optimization of UTMA scheme can be performed in the ground data center, and the HTS broadcasts the optimized parameters to the covered MCC UEs.

## A. Optimization of ECO-UTMA Scheme

Fig. 5(a) validates the derivation accuracy of Eq. (26) and Eq. (32) for  $AFP^{\text{TCUs}}$  and  $\Delta_{\text{TCUs}}$ , respectively, and we can observe that  $AFP^{\text{TCUs}}$  and  $\Delta_{\text{TCUs}}$  are monotonically non-decreasing functions of  $\beta'$ . Further, Fig. 5(b) shows that the simulated  $AFP^{\text{TTUs}}$  and  $\Delta_{\text{TTUs}}$  agree well with the theoretical performance of Eq. (26) and Eq. (33b), respectively, and  $AFP^{\text{TTUs}}$  and  $\Delta_{\text{TTUs}}$  are also monotonically non-increasing functions of  $\beta'$  under different  $K_{\text{TTUs}}$ .

In the ECO-UTMA scheme,  $K_{\text{TCUs}}$  TCUs and  $\beta' K_{\text{TTUs}}$ TTUs share L pilots in **D** at  $N_2$ , and the optimization for ECO-UTMA scheme is to find the optimal  $\beta'$ , i.e.,  $\beta'^*$ , to minimize  $\Delta_{\text{TCUs}}$  and  $\Delta_{\text{TTUs}}$  under their desired AFP. Therefore, the optimization problem for ECO-UTMA scheme can be constructed as follows:

$$\min_{\alpha'} \quad \Delta_q \left( q \in \{ \text{TCUs}, \text{TTUs} \} \right),$$

s.t. 
$$\begin{cases} AFP^q \le AFP^{q*}, \\ 0 \le \beta' \le 1, \end{cases}$$
(34)

where the two constraints are the desired AFP and the value range of offloading ratio, respectively.

Thus, according to Fig. 5(a), we can achieve the lowest  $\Delta_{\text{TCUs}}$  by set  $\beta' = 0$ , and the ECO-UTMA scheme degenerates to IS-UTMA scheme. To improve  $\Delta_{\text{TTUs}}$ , we can find the upper bound of  $\beta'$  as  $\beta_1'^*$  to meet the desired  $AFP^{\text{TCU*}}$ , and decompose the optimization problem Eq.(34) into two sub-problems as follows.

Sub-Problem 1: The upper bound  $\beta_1^{\prime*}$  of  $\beta^{\prime}$  must satisfy the desired  $AFP^{\text{TCUs}*}$ , then, for  $\beta^{\prime} = \beta_1^{\prime*}$ , we can achieve the lowest  $\Delta_{\text{TTUs}}$ , and we have:

$$\min_{\beta'} \quad \Delta_{\text{TTUs}}, s.t. \quad \begin{cases} AFP^{\text{TCUs}}(\beta') \le AFP^{\text{TCUs}*}, \\ 0 \le \beta' \le 1. \end{cases}$$
(35)

Hence, from Fig. 5(a),  $\beta_1^{\prime*}$  can be express as follows:

$$\beta_1^{\prime *} = \left\{ \beta_1^{\prime *} | AFP^{\text{TCUs}}(\beta_1^{\prime *}) = AFP^{\text{TCUs}*} \right\}.$$
(36)

Sub-Problem 2: Sub-problem 1 has found a upper bound for  $\beta'$  to satisfy the desired  $AFP^{\text{TCUs}*}$  and achieve the lowest  $\Delta_{\text{TTUs}}$ . Further, we can also find a lower bound for  $\beta'$  as  $\beta'_0 = \{\beta'_0 | AFP^{\text{TTUs}}(\beta'_0) = AFP^{\text{TTUs}*}\}$  to satisfy the desired  $AFP^{\text{TTUs}*}$ , and we have:

$$\min_{\beta'} \quad \Delta_{\text{TTUs}}$$

$$\Delta_{\text{TSUs}} = \frac{\sum_{l=1}^{H_{\text{TSUs}}} \sum_{f=1}^{F} \sum_{x=1}^{f} (3x-2) \frac{K_{\text{TSUs}} (1-AFP_l^{\text{TSUs}})}{H_{\text{TSUs}}} \left[ 1 - \frac{K_{\text{TSUs}} (1-AFP_l^{\text{TSUs}})}{H_{\text{TSUs}}} \right]^{x-1}}{H_{\text{TSUs}}F},$$
(31)

2) TCUs:

1) **TSUs:** 

$$\Delta_{\rm TCUs} = \frac{\sum_{l=1}^{H_{\rm TCUs}} \sum_{f=1}^{F} \sum_{x=1}^{f} (3x-1) \frac{K_{\rm TCUs} \left(1 - AFP_l^{\rm TCUs}\right)}{H_{\rm TCUs}} \left[1 - \frac{K_{\rm TCUs} \left(1 - AFP_l^{\rm TCUs}\right)}{H_{\rm TCUs}}\right]^{x-1}}{H_{\rm TCUs}F},$$
(32)

3) TTUs:

3.1) IS-UTMA:

$$\Delta_{\rm TTUs} = \frac{\sum_{l=1}^{H_{\rm TTUs}} \sum_{f=1}^{F} \sum_{x=1}^{f} 3x \frac{K_{\rm TTUs} (1 - AFP_l^{\rm TTUs})}{H_{\rm TTUs}} \left[ 1 - \frac{K_{\rm TTUs} (1 - AFP_l^{\rm TTUs})}{H_{\rm TTUs}} \right]^{x-1}}{H_{\rm TTUs} F},$$
(33a)

3.2) ECO- and ICO-UTMA:

$$\Delta_{\text{TTUs}} = \frac{1}{H_{\text{TTUs}}F} \cdot \sum_{l=1}^{H_{\text{TTUs}}} \left\{ \left\{ 4P_{ss2,l}^{\text{TTUs}} + 3\left(1 - P_{ss2,l}^{\text{TTUs}}\right) + 3P_{s3,l}^{\text{TTUs}} + 6P_{us,l}^{\text{TTUs}} \right\} + \sum_{f=3}^{F} \left\{ 2P_{ss2,l}^{\text{TTUs}} + 3P_{s3,l}^{\text{TTUs}} + \left\{ \sum_{x=2}^{f-1} 3x\left(P_{ss2,l}^{\text{TTUs}} + P_{s3,l}^{\text{TTUs}}\right)\left(P_{us,l}^{\text{TTUs}}\right)^{x-1} \right\} + 3f\left(P_{us,l}^{\text{TTUs}}\right)^{f-1} \right\} \right\}.$$
(33b)



(a)  $\Delta_{\text{TCUs}}$  and  $AFP^{\text{TCUs}}$  versus  $\beta$ , where  $K_{\text{TCUs}} = 2$  and  $H_{\text{TCUs}} = (b) \Delta_{\text{TTUs}}$  and  $AFP^{\text{TTUs}}$  versus  $\beta$ , where  $K_{\text{TCUs}} = 2$  and  $H_{\text{TTUs}} = 8$ .

Fig. 5. The AAoI and AFP of TCUs and TTUs versus  $\beta$ , where  $AFP^{\text{TCUs}*} = 10^{-5}$ ,  $AFP^{\text{TTUs}*} = 10^{-6}$  and L = 169.

s.t. 
$$\begin{cases} AFP^{\text{TTUs}}(\beta') \le AFP^{\text{TTUs}*},\\ \beta_0'^* \le \beta' \le \beta_1'^*. \end{cases}$$
 (37)

Note that if  $\beta_0^{\prime *} \leq \beta_1^{\prime *}$ , we can choose  $\beta^{\prime *}$  as  $\beta_1^{\prime *}$  to achieve the lowest  $\Delta_{\text{TTUs}}$  under the desired  $AFP^{\text{TCUs}*}$  and  $AFP^{\text{TTUs}*}$ . Otherwise,  $AFP^{\text{TCUs}*}$  and  $AFP^{\text{TTUs}*}$  can not be simultaneously satisfied, and we select  $\beta^{\prime *} = \beta_1^{\prime *}$  to satisfy the desired AFP requirement for the higher priority group, and then consider minimizing the AAoI of the lower priority group. Recall that  $AFP^{\text{TCUs}}$  is a monotonically non-decreasing function of  $\beta^{\prime}$  for ECO-UTMA scheme, then  $\beta^{\prime *}$  can be easily obtained in practical as  $\beta^{\prime *}K_{\text{TTUs}}$  should be an integer.

#### B. Optimization of ICO-UTMA Scheme

Fig. 6(a) validates the accuracy of Eq. (27) and Eq. (32) for  $AFP^{TCUs}$  and  $\Delta_{TCUs}$ , respectively, where both  $AFP^{TCUs}$  and  $\Delta_{TCUs}$  are monotonically non-increasing functions of  $\alpha$ . In addition, the simulated  $AFP^{TTUs}$  and  $\Delta_{TTUs}$  agree well with the theoretical performance of Eq. (27) and Eq. (33b) as shown in Fig. 6(b), respectively, and we can observe that  $AFP^{TTUs}$  is a monotonically non-increasing functions of  $\beta$  when  $g_{TTUs}$  is low.

The optimization goal of ICO-UTMA scheme is to find the optimal  $\alpha$  and  $\beta$  to minimize  $\Delta_{TCUs}$  and  $\Delta_{TTUs}$  under their desired AFP, where  $\alpha L$  and  $(1 - \alpha)L$  pilots are pre-allocated for  $K_{TCUs}$  TCUs and  $\beta K_{TTUs}$  TTUs in ICO-UTMA scheme, respectively. Thus, the optimization problem for ICO-UTMA scheme can be expressed as follows:

$$\min_{\alpha,\beta} \quad \Delta_q \left( q \in \{ \text{TCUs, TTUs} \} \right)$$
s.t.
$$\begin{cases}
AFP^q \leq AFP^{q*}, \\
0 \leq \alpha \leq 1, \\
0 \leq \beta \leq 1,
\end{cases}$$
(38)

where the three constraints are the desired AFPs, the value ranges of pilot allocation ratio and offloading ratio, respectively.

The objective function Eq. (38) is not jointly convex versus all variables, thus simplification is considered. In ICO-UTMA scheme, only  $\alpha$  affects  $\Delta_{TCUs}$ , while both  $\alpha$  and  $\beta$  affect

 $\Delta_{\text{TTUs}}$ . Thus, since the ICO-UTMA scheme avoids UE collisions between different groups, we can adopt a two-step optimization strategy to optimize (38). Combining the curve trend in Fig. 6(a), we can achieve the lowest  $\Delta_{\text{TCUs}}$  by set  $\alpha = 1$  and  $\beta \neq 0$ , and the ICO-UTMA scheme degenerates to ECO-UTMA scheme. To avoid collisions from TTUs and improve  $\Delta_{\text{TTUs}}$ , we can find the minimum  $\alpha$  as  $\alpha_{\min}$  to meet the desired  $AFP^{\text{TCUs}}$ , and use it to analyze the optimal  $\beta$  as  $\beta^*$  to minimize  $\Delta_{\text{TTUs}}$  under the desired  $AFP^{\text{TTUs}*}$ . Consequently, we decompose Eq. (38) into two simplified sub-problems as follows.

Sub-Problem 1: For desired  $AFP^{TCUs^*}$ ,  $\alpha_{min}$  can be obtained as follows:

$$\begin{array}{ll}
\min_{\alpha} & \alpha, \\
s.t. & \begin{cases} AFP^{\text{TCUs}}(\alpha) \le AFP^{\text{TCUs}*}, \\
0 \le \alpha \le 1, \end{cases}$$
(39)

and we have:

$$\alpha_{\min} = \left\{ \alpha_{\min} | AFP^{\text{TCUs}}(\alpha_{\min}) = AFP^{\text{TCUs*}} \right\}.$$
(40)

Note that for the ICO-UTMA scheme in practical scenarios,  $AFP^{TCUs}$  is a monotonically non-increasing function of  $\alpha$ . Thus,  $\alpha_{\min}$  can be also easily found due to  $\alpha_{\min}L$  is an integer.

Sub-Problem 2: After  $\alpha_{\min}$  is determined, we can find  $\beta^*$  to meet the desired  $AFP^{\text{TTUs}*}$  and minimize  $\Delta_{\text{TTUs}}$  under  $H_q$  and the system load  $g_q = \frac{K_q}{L}$ , and we have:

$$\min_{\beta} \quad \Delta_{\text{TTUs}}, \\
s.t. \quad \begin{cases} AFP^{\text{TTUs}}(\alpha_{\min}, \beta) \le AFP^{\text{TTUs}*}, \\ 0 \le \beta \le 1. \end{cases} \tag{41}$$

Therefore, according to Fig. 6(b), we can find a lower bound of  $\beta$  as  $\beta_{\min}$  to meet the desired  $AFP^{\text{TTUs}*}$ . In addition, Fig. 6(b) shows that  $\Delta_{\text{TTUs}}$  is a convex function of  $\beta$ , and there is an extreme point denoted as  $\beta_e$  to achieve a minimum  $\Delta_{\text{TTUs}}$ . Thus, the minimum  $\Delta_{\text{TTUs}}$  can be achieved if and only if  $\beta = \beta_{\min}$  or  $\beta = \beta_e$  under the desired  $AFP^{\text{TTUs}*}$ , and the selection rule for  $\beta^*$  is as follows:

$$\beta^* = \begin{cases} \beta_{\min}, & \text{if } \beta_{\min} > \beta_e, \\ \beta_e, & \text{if } \beta_{\min} \le \beta_e. \end{cases}$$
(42)



(a)  $\Delta_{\text{TCUs}}$  and  $AFP^{\text{TCUs}}$  versus  $\alpha$ , where  $H_{\text{TCUs}} = 8$ .



(b)  $\Delta_{\text{TTUs}}$  and  $AFP^{\text{TTUs}}$  versus  $\beta$ , where  $H_{\text{TTUs}} = 20$  and  $\alpha_{\min} = 0.85$ .

Fig. 6. The AAoI and AFP of TCUs and TTUs versus  $\alpha$  and  $\beta$ , where  $AFP^{\text{TCUs}*} = 10^{-5}$ ,  $AFP^{\text{TTUs}*} = 10^{-6}$  and L = 169.

Considering that  $AFP_{\text{TTUs}}$  is a monotonically non-increasing function of  $\beta$ , and  $\Delta_{\text{TTUs}}$  is a convex function of  $\beta$ , we can easily obtain  $\beta^*$  according to Eq. (42) for the ICO-UTMA scheme because  $\beta^*K_{\text{TTUs}}$  is an integer.

In addition, our scheme can be verified to provide an AFP as low as  $10^{-6}$  within one time slot from Fig. 5 and Fig. 6. Therefore, setting each access stage equals to one time slot in our system model is sufficient to meet the AFP requirements of MCC UEs. In practical scenarios, we can set the length of one time slot according to the worst two-way propagation delay corresponding to the altitude of HTS. Moreover, we can set the number of time slots for each type of MCC UEs according to their AFP requirements, allowing multiple access opportunities to ensure the AFP requirements under the specified PDB requirements.

# V. SIMULATION RESULTS AND DISCUSSIONS

Fig. 5 and Fig. 6 in Section IV validate that the UTMA scheme can provide UT protection for three types of MCC UEs under the desired AFP. In this section, we deploy the UTMA scheme to massive access scenario, where we still divide UEs into three groups with different access priorities, i.e.,  $L_1$ ,  $L_2$  and  $L_3$ , and the UEs in  $L_1$  and  $L_3$  have the highest and lowest access priority, respectively. First, we provide extensive Monte Carlo simulations to validate the accuracy of our theoretical analysis for AFP and AAoI with different values of  $\alpha$  and  $\beta$ . Then, we discuss the AAoI performance versus  $g_i$  and T for ICO-UTMA scheme under different parameters,



Fig. 7. The variation of AAoI and AFP derived in Section III versus  $g_i$  in UTMA scheme, where SNR = 20dB.

TABLE I Simulation Parameters

Description	Values
Number of access frames $F$	1000000
Number of UEs in group $i$	$ \{ H_1 = 8, H_2 \in [94, 338], \\ H_3 \in [338, 507] \} $
Number of orthogonal pilots $L$	169
Maximum collision resolution order $T$	2
SNR(dB)	[-5, 20]
Pilot allocation ratio $\alpha$	$\{0.5, 0.7\}$
Offloading ratio $\beta$	0.4

and analyze the value range of  $g_2$  and  $g_3$  to find the optimal AAoI. Further, we compare the UTMA scheme with existing schemes [14].

Table I summarizes the Monte Carlo simulation parameters, where we set F = 1000000 to obtain the more precise AAoI. Then,  $H_i$  is set to be 8, [94, 338], and [338, 507], respectively,



(b)  $L_2$  and  $L_3$ 

Fig. 8. The variation of AAoI and AFP derived in Section III versus  $g_i$  in UTMA scheme, where SNR = 5dB.

where 8 is the density requirement for MCC UEs in future NTN [8], and we simulate large  $H_2$  and  $H_3$  to validate the AFP performance of our UTMA schemes under a generic crowded random access scenario [41]. To obtain the largest number of orthogonal pilot sequences, we set L = 169. In addition, considering a tradeoff between the performance of AFP and the complexity, we set T = 2 [26]. Further, we set the Signal-to-Noise Ratio (SNR)  $\in [-5, 20]$  dB, and  $\alpha$  and  $\beta$  are the optimized parameters via the optimization in Section IV.

Fig. 7 illustrates the AAoI performance of each group versus  $g_i (i \in \{1, 2, 3\})$  for our three UTMA schemes under SNR = 20 dB, and the theoretical derivations agree well with the simulation results under different parameters. Fig. 7(a) compares the AAoI and AFP performance of  $L_1$  under the UTMA and GFAO schemes [14]. Since the UTMA scheme introduces a multi-dimensional codebook to resolve UE collisions, which can achieve a lower AFP in one time slot, thus the UTMA scheme has good timeliness performance. On contrast, the



Fig. 9. The variation of AAoI and AFP derived in Section III versus  $g_i$  in UTMA scheme, where SNR = 10dB.

UEs attempt to access in multiply slots in GFAO scheme, sacrificing timeliness for reliability and the AFP of GFAO outperforms that of the UTMA scheme. Fig. 7(b) shows that as  $q_i$  increases, all AAoI curves for each group are monotonically non-increasing functions under different  $\alpha$  and  $\beta$ , where the AAoI is higher in the low load region and then decreases significantly. Because when  $g_i$  increases from 0, the number of activated UEs increases and the large AAoI caused by inactivated UEs will decrease rapidly, and the AAoI may decrease when  $g_i \leq T$ . Moreover, the IS-UTMA outperforms ECO- and ICO-UTMA in  $L_2$  due to it does not provide offloading, and the ICO-UTMA scheme outperforms the ECO-UTMA scheme in terms of AAoI because it avoids UE collisions between different groups. As shown in Fig. 7(b), the ECO-UTMA scheme can provide AFP  $10^{-2} \sim 10^{-1}$  for all  $g_2$ , while the ICO-UTMA scheme can provide AFP  $\leq 10^{-4}$ if  $g_i \leq 0.025$ , and  $10^{-2} \sim 10^{-1}$  if  $g_i$  is large. Moreover, due



Fig. 10. The variation of AAoI and AFP performance of each group versus SNR in three UTMA schemes, where  $g_1 = 0.01$ ,  $g_2 = 0.02$ ,  $g_3 = 0.1$ , L = 169, T = 2,  $\alpha = 0.7$  and  $\beta = 0.4$ .

to offloading, where the UE collisions in  $N_3$  is resolved, the ECO- and ICO-UTMA schemes are beneficial to  $L_3$ , providing AFP as low as  $10^{-4}$ , while the IS-UTMA scheme can only provide AFP  $10^{-2} \sim 10^{-1}$ .

We utilize SNR=20 dB to validate that our UTMA scheme can achieve the  $10^{-6} \sim 10^{-5}$  AFP requirements of MCC as shown in Fig. 7, and also simulate the performance of 5 and 10 dB in Fig. 8 and Fig. 9, respectively. It can be observed that the lowest achievable AFP can reach  $10^{-3}$  at SNR=5 dB and  $10^{-4}$  at SNR=10 dB in Fig. 8 and Fig. 9, respectively, and the theoretical derivations agree well with the simulation results. Further, Fig. 10 shows the AAoI and AFP performance of each group versus SNR  $\in [-5, 5]$  dB for three UTMA schemes, and as the SNR increases, all AAoI and AFP curves for each group are monotonically decreasing. We can observed that the proposed UTMA schemes can achieve AFP  $10^{-2}$  in SNR  $\in [-5, 0]$  dB and  $10^{-3}$  in SNR  $\in [0, 5]$  dB, respectively. Thus, our UTMA schemes can guarantee the timely and reliable status updates in S-IoT.



(c)  $L_3$ , where  $\alpha = 0.6$ ,  $H_3 = \{507, 676\}$  and  $T = \{2, 3\}$ .

Fig. 11. The AAoI of  $L_2$  and  $L_3$  versus  $\alpha$  and  $\beta$  under different  $g_i$ ,  $H_i$  and T in ICO-UTMA.

Fig. 11 shows the AAoI performance of  $L_2$  and  $L_3$  versus  $\alpha$  and  $\beta$  under different  $g_i$ ,  $H_i$  and T in ICO-UTMA scheme, which can resolve up to LT UE collisions in a time slot. Ideally, the ICO-UTMA scheme allows  $\alpha LT$  UEs in  $L_2$  and  $(1-\alpha)LT$  UEs in  $L_3$  to access successfully in  $N_2$ . Therefore, the AAoI performance of  $L_2$  deteriorates if  $K_2 > \alpha LT$ , i.e.,  $g_2T > \alpha LT$ . Two black boxes are illustrated in Fig. 11(a), where the AAoI begins to increase when  $g_2 > \alpha T$  with  $\alpha = 0.5$  and T = 2 or  $\alpha = 0.4$  and T = 3. Thus, we can derive that  $g_2$  should satisfy  $g_2 \leq \alpha T$  to guarantee the AAoI performance



Fig. 12. The AAoI of  $L_2$  and  $L_3$  versus load for proposed IS-, ECO-, ICO-UTMA scheme and GFAO scheme, where  $H_2 = 338$ ,  $H_3 = 507$ ,  $T = \{2, 3\}$  and  $\Delta N = \{2, 3\}$ .

TABLE II The Comparison of the Minimum Achievable AAOI for IS-, ECO-, ICO-UTMA Schemes and GFAO Scheme under Different T and  $\Delta N$ 

Order T	Number of Time Slots $\Delta N$	Load g <sub>i</sub>	Comparison of AAoI $\Delta_i$
2	2	$0 \le g_1 \le 0.05$	UTMA <gfao< td=""></gfao<>
2	2	$\begin{array}{c} 0 \leq g_2 \leq 1.5 \\ 1.5 < g_2 \leq 1.7 \\ 1.7 < g_2 \leq 2 \\ 0 \leq g_2 \leq 2 \end{array}$	IS-UTMA <ico-utma<eco-utma<gfao< td=""></ico-utma<eco-utma<gfao<>
2	2		IS-UTMA <eco-utma<gfao<ico-utma< td=""></eco-utma<gfao<ico-utma<>
2	2		IS-UTMA <gfao<eco-utma<ico-utma< td=""></gfao<eco-utma<ico-utma<>
3	3		IS-UTMA <ico-utma<eco-utma<gfao< td=""></ico-utma<eco-utma<gfao<>
2	2	$\begin{array}{c} 0 \leq g_3 \leq 1.9 \\ 1.9 < g_3 \leq 2.1 \\ 2.1 < g_3 \leq 2.5 \\ 2.5 < g_3 \leq 3 \\ 0 \leq g_3 \leq 3 \end{array}$	ICO-UTMA <eco-utma<is-utma<gfao< td=""></eco-utma<is-utma<gfao<>
2	2		ICO-UTMA <eco-utma<gfao<is-utma< td=""></eco-utma<gfao<is-utma<>
2	2		ICO-UTMA <gfao<eco-utma<is-utma< td=""></gfao<eco-utma<is-utma<>
2	2		GFAO <ico-utma<eco-utma<is-utma< td=""></ico-utma<eco-utma<is-utma<>
3	3		ICO-UTMA <eco-utma<is-utma<gfao< td=""></eco-utma<is-utma<gfao<>

of  $L_2$ . Similarly, according to the relationship between  $K_i$  and  $L^{(i)}$ ,  $g_3$  should satisfy  $\beta g_3 L \leq (1 - \alpha)LT$  in  $N_2$  and  $(1 - \beta)g_3 L \leq LT$  in  $N_3$  to guarantee the AAoI performance of  $L_3$ . Hence,  $g_3 \leq \min\left\{\frac{(1-\alpha)T}{\beta}, \frac{T}{1-\beta}\right\}$ . Similarly, four black boxes are illustrated in Fig. 11(b) and Fig. 11(c), where the AAoI begins to increase when  $g_3 > \frac{(1-\alpha)T}{\beta}$  with  $\beta = 0.4$  and  $T = \{2,3\}$  or  $\alpha = 0.6$  and  $T = \{2,3\}$ .

Fig. 11 shows the AAoI performance of  $L_2$  and  $L_3$  versus load  $g_2$  and  $g_3$  for the proposed IS-, ECO-, ICO-UTMA schemes and the GFAO scheme under different T and  $\Delta N$ , where  $\Delta N$  is denoted as the number of time slots in an access stage for the GFAO scheme. In one time slot, our UTMA scheme can resolve T UE collisions over one pilot through the T-order codebook. Therefore, to be fairly comparison, we assume that  $\Delta N$  is equal to T, i.e.,  $\Delta N = T \in \{2,3\}$ . In addition, Table II summarizes the comparison of the minimum achievable AAoI for the IS-, ECO-, ICO-UTMA and the GFAO schemes under T and  $\Delta N$  in Fig. 11.

Fig. 11 and Table II show that the IS-UTMA scheme can significantly decrease the  $\Delta_2$  than that of the GFAO scheme. The numerical results confirm that the IS-UTMA scheme can achieve a minimum  $\Delta_2$  approximately  $\frac{1}{2}$  and  $\frac{1}{6}$ of the GFAO under T = 2 and T = 3. For example, when  $1.5 < g_2 \le 1.7$  under T = 2, the IS-UTMA scheme can achieve  $\Delta_2 = 5.0$ , but the GFAO scheme can only achieve  $\Delta_2 = 10.5$ . In addition, when  $0 \le g_2 \le 2$  under T = 3, the IS-UTMA scheme can achieve  $\Delta_2 = 2.3$ , where the GFAO scheme has  $\Delta_2 = 13.0$ . In general, larger T allows to resolve more UE collisions in one time slot, and thus T = 3 has a lower  $\Delta$  than T = 2. However, when  $g_2 \leq 1.5$ , in the ECO-UTMA scheme,  $\Delta$  of T = 3 only slightly decreases than that of T = 2 for  $L_2$ , because only  $g_2L + \beta K_3$  UEs in  $N_2$  to perform access, which leads to the resolvable UE collisions LT is redundant. In addition, in ICO-UTMA scheme, the resolvable UE collisions  $\alpha LT$  for UEs in  $L_2$  is redundant, and thus the ICO-UTMA scheme outperforms the ECO-UTMA scheme when  $q_2 \leq 1.5$ . On the other hand, considering that the UE collisions become serious when  $g_2 > 1.5$ , the ECO-UTMA scheme outperforms the ICO-UTMA scheme as the ECO-UTMA scheme offer  $L_2$  a degree of freedom in selecting pilots.

Further, to avoid collisions from  $L_3$  and improve  $\Delta_3$ , the ECO- and ICO-UTMA schemes allow  $L_3$  to offload in  $L_2$  access stage. From Fig. 11 and Table II, we can observe that the ECO- and ICO-UTMA schemes can provide UT protection for  $L_3$  than the IS-UTMA scheme, and significantly decrease  $\Delta_3$  than that of the IS-UTMA and GFAO schemes when  $g_3 \leq T$ . For example, when  $0 \leq g_3 \leq 3$  under T = 3, the ICO- and ECO-UTMA schemes can achieve  $\Delta_3 = 4.4$  and  $\Delta_3 = 5.3$ , respectively, but the IS-UTMA and GFAO schemes can only achieve  $\Delta_3 = 6.1$  and  $\Delta_3 = 8.1$ , respectively. Moreover, due to the pre-allocated **D** for  $L_2$  and  $L_3$ , the ICO-UTMA scheme can relieve the UE collisions between  $L_2$  and  $L_3$ . As shown in Table II, the ICO-UTMA scheme outperforms the ECO-UTMA scheme in  $\Delta_3$  for providing UT protection under different T.

# VI. CONCLUSION

In this paper, we proposed three UTMA schemes to guarantee the various timeliness requirements for three type MCC UEs in S-IoT, and a multi-dimensional codebook was introduced to resolve UE collisions. Specially, the IS-UTMA scheme allowed each group to perform random access in successive time slot according to its priority, while the ECO- and ICO-UTMA scheme allowed timeliness tolerant group to offload in timeliness critical group access stage to improve the timeliness. To capture the timeliness evaluation of each MCC UE group, we derived the closed-form expression of the AAoI of each UE group for three UTMA schemes by tracing AFP and instantaneous AoI. Moreover, we constructed the joint parameter optimization problems for the ECO- and ICO-UTMA schemes to minimize AAoI under desired AFP requirements. Extensive simulations validated the accuracy of the theoretical derivations, and showed that the proposed UTMA scheme can exhibit significantly lower AAoI than state-of-the-art schemes by resolving UE collisions in code domain.

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