A DGTD Scheme for Modeling the Radiated Emission From DUTs in Shielding Enclosures Using Near Electric Field Only

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Abstract—To meet the electromagnetic interference regulation, the radiated emission from device under test such as electronic devices must be carefully manipulated and accurately characterized. Instead of resorting to the direct far-field measurement, in this paper, a novel approach is proposed to model the radiated emission from electronic devices placed in shielding enclosures by using the near electric field only. Based on the Schelkkunoff's equivalence principle and Raleigh-Carson reciprocity theorem, only the tangential components of the electric field over the ventilation slots and apertures of the shielding enclosure are sufficient to obtain the radiated emissions outside the shielding box if the inside of the shielding enclosure was filled with perfectly electric conductor (PEC). In order to efficiently model wideband emission, the time-domain sampling scheme is employed. Due to the lack of analytical Green's function for arbitrary PEC boxes, the radiated emission must be obtained via the full-wave numerical methods by considering the total radiated emission as the superposition between the direct radiation from the equivalent magnetic currents in free space and the scattered field generated by the PEC shielding box. In this study, the state-of-the-art discontinuous Galerkin time-domain (DGTD) method is utilized, which has the flexibility to model irregular geometries, keep high-order accuracy, and more importantly involves only local operations. For open-region problems, a hybridized DGTD and time-domain boundary integration method applied to rigorously truncate the computational domain. To validate the proposed approach, several representative examples are presented and compared with both analytical and numerical results.

Index Terms—Boundary integration (BI) method, discontinuous Galerkin time-domain (DGTD) method, electronic systems in shielding enclosure, equivalence principle, radiated emission, Raleigh–Carson reciprocity theorem.

I. INTRODUCTION

T ODAY'S electronic systems consisting of highly populated RF modules, digital dies, and printed circuit boards (PCB) become an efficient radiator as frequencies increase [1]–[3]. To meet the electromagnetic interference regulation, the

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radiated emissions from noise sources such as victim traces due to crosstalk, discontinuities of return currents happening at conducting trace-vias transitions, and propagating of the switching noise along the power/ground plate guide [4] must be controlled below the required level. Admittedly, the conventional full-wave numerical approaches such as finite-difference timedomain method [5]–[7], finite-element method (FEM) [8], and method of moments [9] are accurate by directly solving the Maxwell's equations. However, the computational cost is too expensive since the multiscale geometries result in poorly conditioned matrix equations with millions of unknowns.

As an alternative, the straightforward far-field (FF) measurement conducted in the open area test site (OATS) or semianechoic chambers is also a widely referred technique in electromagnetic compatibility society [10]. Usually, the maximum radiation at 3 or 10 m away from the electronic system is of interest [10], [11]. Unfortunately, this method is time consuming, prohibitively expensive, and requires electromagnetic (EM) cleaning environments for OATS. Therefore, other remedies must be developed.

Rigorously, the aforeproposed approaches can be categorized into two groups. For the first group, the mode-expansion-based technique is involved. In [12], the electric field is first measured over a spherical surface enclosing the antenna, and then, spherical wave modes are used to expand the measured fields. Based on the orthogonal property of the spherical wave modes, the expansion coefficients can be conveniently calculated. Similarly, the electric field is sampled over a cylindrical surface, and then, expanded by cylindrical wave modes [13]. Later, the planarly scanned near-electric field are approximated by a number of plane-waves in the spectral domain [14]. Via Fourier transform, the FF over a certain rectangular plane in front of the antenna can be predicted. Instead of direct expanding the field via mode functions, in [15], the Dyadic Green's function in the presence of perfectly electrical conducting sphere is expanded by spherical wave modes. With this Green's function, the field outside the measurement spherical surface can be straightforwardly obtained based on the Huygens' principle. The main advantage of this approach is that the Green's function is valid at any frequency but only requires a single calculation. Thus, it is more time efficient.

As for the second approach, the original radiators are replaced by a set of equivalent current sources that are able to reproduce the original emission. The equivalent source can be either electric, magnetic currents, or Hertzian dipoles. In [16], the

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radiated near electric field of the antenna is sampled over a rectangular plane in front of the antenna. To generate the same radiation, the antenna is substituted by a surface magnetic current over an infinitely large PEC plane. Via point matching technique, the unknown magnetic current is inversely determined based on conjugate gradient method. In [17], this approach is directly extended to the equivalent electric current source situation. The main deficiency of these two methods is that only the radiation in the forward half-space can be predicted. To overcome this problem, [18]-[22] proposed to construct the equivalent current source over the surface of the radiator and simultaneously the near-field is sampled over a surface enclosing the radiator. To guarantee the continuous property of the equivalent current, the Rao-Wilton-Glisson [23] basis function is used to expand the unknown current. By point-matching method, the expansion coefficient can be calculated through iterative methods. Other alternative sources such as Hertzian dipoles are also deployed to reproduce the radiated emissions from PCBs and ICs in [25]. In [24], the parameters of the equivalent dipole sources are optimized by genetic algorithm. For the equivalent source approach, the inverse process is involved which could be prohibitive cost due to the ill-conditioned matrix equations. Furthermore, the established current source could be nonunique due to the existence of nonradiating sources.

In this paper, a novel approach based on the near electric field only is proposed to characterize the radiated emission from electronic systems placed in shielding enclosures. Usually, the surface of the shielding enclosure can be assumed as PEC, thus, only the tangential components of electric field over the ventilation slots and apertures plus the tangential components of the magnetic field over the whole surface of the enclosure are needed according to the Huygens' principle. By further referring to the Love's equivalence principle [26], the inside of the Huygens' surface can be filled with arbitrary material without affecting the outgoing radiation. Thus, we fill the inside of the shielding enclosure with PEC. As a result, only the contribution from the equivalent magnetic current (derived from the near electric field: $\mathbf{M}_s = -\mathbf{\hat{n}} \times \mathbf{E}$) over the ventilation slots and apertures are needed since the electric current (derived from the near magnetic field: $\mathbf{J}_s = \hat{\mathbf{n}} \times \mathbf{H}$) over a PEC surface is nonradiative in line with the Raleigh–Carson reciprocity theorem. In this way, the number of NF sampling is drastically reduced. On the other hand, a powerful approach should be capable of efficiently predicting the radiated emission over a very broad frequency band. Thus, time-domain strategy is more preferable compared with frequency-domain method since only single NF-FF transformation is sufficient. To reach this aim, the near electric field is recorded in the time domain. In order to obtain the radiation from the equivalent magnetic current source over the PEC-filled shielding enclosure, the original problem is equivalently transformed to a scattering problem by considering the total radiation as the superposition between the direct radiation from the magnetic current source in free face and the scattered field by the PEC shielding box. In this study, the discontinuous Galerkin time-domain (DGTD) method [27]-[29] is utilized to solve this scattering issue. Compared with the approach in [30], the near electric field is only required over the slots and apertures over



Fig. 1. Left: The electronic system placed into a shielding enclosure, and the tangential components of the electric field are temporally sampled over the ventilation slots and apertures by an electric dipole. Right: The equivalence of the original problem by filling the inside of the shielding enclosure with PEC. The equivalent magnetic current \mathbf{M}_s is able to reproduce the original radiated emission by the superposition of the direct radiation from $\mathbf{M}_s = -\hat{\mathbf{n}} \times \mathbf{E}_{\text{meas}}$ in free space and the scattered field from the PEC filled shielding box.

the shielding enclosure while it requires the magnetic field over the whole surface of the shielding enclosure in [30] since the tangential components of the magnetic field is nonzero over the PEC surface.

As the combination of finite volume method [31] and FEM [32], all spatial operations of DGTD are local due to the use of numerical flux for information exchange between neighboring elements. Thus, the resultant mass-matrices are blockdiagonal and can be inverted before starting time-marching scheme. Consequently, a compact and efficient solver when combined with an explicit time marching scheme is reached. Due to the existence of the equivalent magnetic surface current, the discontinuity of the tangential electric field must be considered when deriving the numerical flux expressions based on the Rankine–Hugoniot Jump Relations along the characteristics of hyperbolic systems. For this open-region scattering problem, the DGTD is integrated with the time-domain boundary integral (TDBI) algorithm to truncate the computational domain by evaluating the field values required for the incoming numerical flux calculation over the truncation boundary [33]. It is mathematically exact, and the truncation boundary can be conformal to the surface of the shielding enclosure, thus making the computational region as small as possible.

The remainder of this paper organized as follows. In Section II, the basic EM theories and DGTD formulations are detailed, including the clarification of equivalence principle-based method, the derivation of the numerical flux and the formulation of matrix equations. Section III will benchmark various canonical examples to verify the accuracy and robustness of the algorithm. Finally, conclusions and discussions are presented at the end of the paper.

II. THEORY AND MATHEMATICAL FORMULATION

For electronic systems in shielding enclosures as shown in Fig. 1, both the electric and magnetic fields over the surface of the shielding enclosure are needed according to the Huygens' principle, which is time consuming and also very difficult. Therefore, it is more preferable if only electric or magnetic field was required. According to Love's equivalence principle and Raleigh–Carson reciprocity theorem [26], [34], the equivalent electric currents $\mathbf{J}_s(\mathbf{r}', t) = \hat{\mathbf{n}} \times \mathbf{H}(\mathbf{r}', t)$ is nonradiative if the

inside of the shielding enclosure is filled up with PEC. Consequently, only the tangential components of the electric field (or the equivalent magnetic currents $\mathbf{M}_s(\mathbf{r}', t) = \mathbf{E}(\mathbf{r}', t) \times \hat{\mathbf{n}}$) over the ventilation slots and apertures are required to predict the radiated emission outside the shielding enclosure based on the Schelkkunoff's equivalence principle.

However, the radiated fields cannot be analytically calculated since the DGF in the presence of arbitrary PEC box is not available [37]. However, the calculation of the numerical DGF is prohibitively expensive. In this study, the DGTD method is employed by considering the problem as a scattering issue with incident field generated from $\mathbf{M}_{s}(\mathbf{r}', t)$.

Due to the existence of the surface magnetic current M_s , the following boundary condition over the ventilation slots and apertures must be satisfied

$$\hat{\mathbf{n}} \times \left(\mathbf{E}^+ - \mathbf{E}^- \right) = -\mathbf{M}_s \tag{1}$$

with superscripts + and - denoting the two sides of the impedance surface and $\hat{\mathbf{n}}$ representing the unit normal vector pointing from - to +.

A. Numerical Flux Derivation

To incorporate the boundary condition in 1) into DGTD, the mathematical expression of the numerical flux should be reformulated. For an arbitrary mesh element i (tetrahedrons are used in this study), the *Rankine–Hugoniot Jump Relations* along the three different *characteristics* [31] for the *f*th face of element i are defined as

1) Jump across the characteristic $x_n = -c^i t$

$$\frac{1}{\mu^i}\hat{\mathbf{n}}_{i,f} \times (\mathbf{E}_f^* - \mathbf{E}^i) = -c^i(\mathbf{H}_f^* - \mathbf{H}^i) \qquad (2)$$

$$\frac{1}{\epsilon^i}\hat{\mathbf{n}}_{i,f} \times (\mathbf{H}^i - \mathbf{H}_f^*) = -c^i (\mathbf{E}_f^* - \mathbf{E}^i).$$
(3)

2) Jump across the characteristic $x_n = 0$

$$\hat{\mathbf{n}}_{i,f} \times \left(\mathbf{E}_f^{**} - \mathbf{E}_f^* \right) = -\mathbf{M}_s \tag{4}$$

$$\hat{\mathbf{n}}_{i,f} \times (\mathbf{H}_f^{**} - \mathbf{H}_f^*) = 0.$$
(5)

3) Jump across the characteristic $x_n = c_f^j t$

$$\frac{1}{\mu_f^j} \hat{\mathbf{n}}_{i,f} \times (\mathbf{E}_f^j - \mathbf{E}_f^{**}) = c_f^j (\mathbf{H}_f^j - \mathbf{H}_f^{**}) \qquad (6)$$

$$\frac{1}{\epsilon_f^j} \hat{\mathbf{n}}_{i,f} \times (\mathbf{H}_f^{**} - \mathbf{H}_f^j) = c_f^j (\mathbf{E}_f^j - \mathbf{E}_f^{**})$$
(7)

where $1 \leq f \leq 4$ for tetrahedrons, j denotes the neighboring element sharing the fth face of element i, $\hat{\mathbf{n}}_{i,f}$ is the outward unit normal vector of face f. c^i and c^j_f represent the characteristic speed in element i and its neighboring j, respectively. $\epsilon^{i/j}$ and $\mu^{i/j}$ are the permittivity and permeability, respectively. $(\mathbf{E}_f^*, \mathbf{H}_f^*)$ and $(\mathbf{E}_f^{**}, \mathbf{H}_f^{**})$ are the intermediate states in element i and j, respectively. By combining (2), (4), (5), and (6), the upwind flux for the Ampere's law equation is formulated by

$$\hat{\mathbf{n}}_{i,f} \times \mathbf{H}_{f}^{*} = \hat{\mathbf{n}}_{i,f} \times \frac{\left(Z^{i}\mathbf{H}^{i} + Z_{f}^{j}\mathbf{H}_{f}^{j}\right) + \hat{\mathbf{n}}_{i,f} \times \left(\mathbf{E}^{i} - \mathbf{E}_{f}^{j}\right)}{Z^{i} + Z_{f}^{j}} - \frac{\hat{\mathbf{n}}_{i,f} \times \mathbf{M}_{s}}{\left(Z^{i} + Z_{f}^{j}\right)}.$$
(8)

Similarly, with (3), (4), (5), and (7), the upwind flux for the Maxwell–Faraday's law equation is given by

$$\hat{\mathbf{n}}_{i,f} \times \mathbf{E}_{f}^{*} = \hat{\mathbf{n}}_{i,f} \times \frac{\left(Y^{i}\mathbf{E}^{i} + Y_{f}^{j}\mathbf{E}_{f}^{j}\right) + \hat{\mathbf{n}}_{i,f} \times \left(\mathbf{H}_{f}^{j} - \mathbf{H}^{i}\right)}{Y^{i} + Y_{f}^{j}} + \frac{Y_{f}^{j}\mathbf{M}_{s}}{2\left(Y^{i} + Y_{f}^{j}\right)}$$
(9)

where $Z^i = \sqrt{\mu^i/\epsilon^i}$ and $Z_f^j = \sqrt{\mu_f^j/\epsilon_f^j}$ represent the characteristic impedance of element *i* and the neighboring at the *f*th face.

Since the surface magnetic current \mathbf{M}_s is over the PEC, therefore the parameters of the neighboring element j are: $Z_f^j = 0$ and $Y_f^j = \infty$. For programming convenience, this can be equivalently achieved by letting $\mathbf{E}_f^j = -\mathbf{E}^i$, $\mathbf{H}_f^j = \mathbf{H}^i$, $Z_f^j = Z^i$ and $Y_f^j = Y^i$ [35].

B. DGTD Formulation

Let Ω denote the computation domain of interest, which is bound by surface $\partial\Omega$. With DGTD, the domain Ω is first split into N nonoverlapping tetrahedrons Ω_i with boundary $\partial\Omega_i$. In element *i*, the electric field **E** and magnetic field **H** are approximated by vector basis functions $\Phi^i(\mathbf{r})$ and $\Psi^i(\mathbf{r})$ [29], [33]: $\mathbf{E}^i = \sum_{k=1}^{n_e^i} e_k^i(t) \Phi_k^i(\mathbf{r})$ and $\mathbf{H}^i = \sum_{l=1}^{n_h^i} h_k^i(t) \Psi_l^i(\mathbf{r})$, where n_e^i and n_h^i are the number of vector basis function [32] for **E** and **H** in *i*th element, respectively; e_k^i and h_k^i are the unknown time-dependent coefficients.

By applying the DG testing over the two first-order timederivative Maxwell's curl equation, we can obtain

$$\int_{\Omega_{i}} \mathbf{\Phi}_{k}^{i} \cdot \left[\epsilon_{i} \frac{\partial \mathbf{E}^{i}}{\partial t} - \nabla \times \mathbf{H}^{i} \right] d\mathbf{r} =$$

$$\sum_{f=1}^{4} \int_{\partial\Omega_{i,f}} \mathbf{\Phi}_{k}^{i} \cdot \left[\hat{\mathbf{n}}_{i,f} \times (\mathbf{H}_{f}^{*} - \mathbf{H}^{i}) \right] d\mathbf{r} \qquad (10)$$

$$\int_{\Omega_{i}} \mathbf{\Psi}_{l}^{i} \cdot \left[\mu_{i} \frac{\partial \mathbf{H}^{i}}{\partial t} + \nabla \times \mathbf{E}^{i} \right] d\mathbf{r} =$$

$$\sum_{f=1}^{4} \int_{\partial\Omega_{i,f}} \mathbf{\Psi}_{l}^{i} \cdot \left[\hat{\mathbf{n}}_{i,f} \times (\mathbf{E}^{i} - \mathbf{E}_{f}^{*}) \right] d\mathbf{r}. \qquad (11)$$

After a tedious mathematical operation, we can achieve the semidiscrete matrix equations as

$$\bar{\mathbf{M}}_{e}^{i} \frac{\partial \mathbf{e}^{i}}{\partial t} = \bar{\mathbf{S}}_{e}^{i} \mathbf{h}^{i} + \sum_{f=1}^{4} \left(\bar{\mathbf{F}}_{ee}^{ii,f} \mathbf{e}_{f}^{i} + \bar{\mathbf{F}}_{ee}^{ij,f} \mathbf{e}_{f}^{j} + \bar{\mathbf{F}}_{eh}^{ii,f} \mathbf{h}_{f}^{j} + \bar{\mathbf{F}}_{eh}^{ij,f} \mathbf{h}_{f}^{j} \right) + \bar{\mathbf{F}}_{e}^{i,M_{s}}$$
(12)

$$\bar{\mathbf{M}}_{h}^{i} \frac{\partial \mathbf{h}^{i}}{\partial t} = -\bar{\mathbf{S}}_{h}^{i} \mathbf{e}^{i} + \sum_{f=1}^{4} \left(\bar{\mathbf{F}}_{hh}^{\text{ii},f} \mathbf{h}_{f}^{i} + \bar{\mathbf{F}}_{hh}^{\text{ij},f} \mathbf{h}_{f}^{j} + \bar{\mathbf{F}}_{he}^{\text{ii},f} \mathbf{e}_{f}^{j} + \bar{\mathbf{F}}_{he}^{\text{ij},f} \mathbf{e}_{f}^{j} \right) + \bar{\mathbf{F}}_{h}^{i,M_{s}}$$
(13)

where

$$\begin{split} \left[\mathbf{\bar{M}}_{e}^{i} \right]_{\mathrm{kl}} &= \int_{\Omega_{i}} \mathbf{\Phi}_{k}^{i} \cdot \epsilon^{i} \mathbf{\Phi}_{l}^{i} d\mathbf{r} \\ \left[\mathbf{\bar{M}}_{h}^{i} \right]_{\mathrm{kl}} &= \int_{\Omega_{i}} \mathbf{\Psi}_{k}^{i} \cdot \mu^{i} \mathbf{\Psi}_{l}^{i} d\mathbf{r} \\ \left[\mathbf{\bar{S}}_{e}^{i} \right]_{\mathrm{kl}} &= \int_{\Omega_{i}} \mathbf{\Phi}_{k}^{i} \cdot \nabla \times \mathbf{\Psi}_{l}^{i} d\mathbf{r} \\ \left[\mathbf{\bar{S}}_{e}^{i} \right]_{\mathrm{kl}} &= \int_{\Omega_{i}} \mathbf{\Psi}_{k}^{i} \cdot \nabla \times \mathbf{\Phi}_{l}^{i} d\mathbf{r} \\ \left[\mathbf{\bar{F}}_{\mathrm{ee}}^{\mathrm{ii},f} \right]_{\mathrm{kl}} &= \frac{-1}{Z^{i} + Z_{f}^{j}} \int_{\partial\Omega_{i,f}} \mathbf{\Phi}_{k}^{i} \cdot \hat{\mathbf{n}}_{i,f} \times (\hat{\mathbf{n}}_{i,f} \times \mathbf{\Phi}_{l}^{i}) d\mathbf{r} \\ \left[\mathbf{\bar{F}}_{\mathrm{ee}}^{\mathrm{ii},f} \right]_{\mathrm{kl}} &= \frac{-1}{Z^{i} + Z_{f}^{j}} \int_{\partial\Omega_{i,f}} \mathbf{\Phi}_{k}^{i} \cdot \hat{\mathbf{n}}_{i,f} \times (\mathbf{\hat{n}}_{i,f} \times \mathbf{\Phi}_{l}^{j,f}) d\mathbf{r} \\ \left[\mathbf{\bar{F}}_{\mathrm{eh}}^{\mathrm{ii},f} \right]_{\mathrm{kl}} &= -\frac{Z_{f}^{j}}{Z^{i} + Z_{f}^{j}} \int_{\partial\Omega_{i,f}} \mathbf{\Phi}_{k}^{i} \cdot \hat{\mathbf{n}}_{i,f} \times \mathbf{\Psi}_{l}^{i} d\mathbf{r} \\ \left[\mathbf{\bar{F}}_{\mathrm{eh}}^{\mathrm{ii},f} \right]_{\mathrm{kl}} &= \frac{-1}{Z^{i} + Z_{f}^{j}} \int_{\partial\Omega_{i,f}} \mathbf{\Phi}_{k}^{i} \cdot \hat{\mathbf{n}}_{i,f} \times \mathbf{M}_{s} d\mathbf{r} \\ \left[\mathbf{\bar{F}}_{\mathrm{eh}}^{\mathrm{ii},f} \right]_{\mathrm{kl}} &= \frac{-1}{Z^{i} + Z_{f}^{j}} \int_{\partial\Omega_{i,f}} \mathbf{\Phi}_{k}^{i} \cdot \hat{\mathbf{n}}_{i,f} \times (\hat{\mathbf{n}}_{i,f} \times \mathbf{\Psi}_{l}^{i}) d\mathbf{r} \\ \left[\mathbf{\bar{F}}_{\mathrm{eh}}^{\mathrm{ii},f} \right]_{\mathrm{kl}} &= \frac{-1}{Z^{i} + Z_{f}^{j}} \int_{\partial\Omega_{i,f}} \mathbf{\Psi}_{k}^{i} \cdot \hat{\mathbf{n}}_{i,f} \times (\hat{\mathbf{n}}_{i,f} \times \mathbf{\Psi}_{l}^{i}) d\mathbf{r} \\ \left[\mathbf{\bar{F}}_{\mathrm{hh}}^{\mathrm{ii},f} \right]_{\mathrm{kl}} &= \frac{-1}{Z^{i} + Z_{f}^{j}} \int_{\partial\Omega_{i,f}} \mathbf{\Psi}_{k}^{i} \cdot \hat{\mathbf{n}}_{i,f} \times (\hat{\mathbf{n}}_{i,f} \times \mathbf{\Psi}_{l}^{i}) d\mathbf{r} \\ \left[\mathbf{\bar{F}}_{\mathrm{hh}}^{\mathrm{ii},f} \right]_{\mathrm{kl}} &= \frac{-1}{Y^{i} + Y_{f}^{j}} \int_{\partial\Omega_{i,f}} \mathbf{\Psi}_{k}^{i} \cdot \hat{\mathbf{n}}_{i,f} \times (\hat{\mathbf{n}}_{i,f} \times \mathbf{\Psi}_{l}^{i}) d\mathbf{r} \\ \left[\mathbf{\bar{F}}_{\mathrm{hh}}^{\mathrm{ii},f} \right]_{\mathrm{kl}} &= \frac{1}{Y^{i} + Y_{f}^{j}} \int_{\partial\Omega_{i,f}} \mathbf{\Psi}_{k}^{i} \cdot \hat{\mathbf{n}}_{i,f} \times \mathbf{\Phi}_{l}^{i} d\mathbf{r} \\ \left[\mathbf{\bar{F}}_{\mathrm{he}}^{\mathrm{ii},f} \right]_{\mathrm{kl}} &= \frac{Y_{f}^{j}}{Y^{i} + Y_{f}^{j}} \int_{\partial\Omega_{i,f}} \mathbf{\Psi}_{k}^{i} \cdot \hat{\mathbf{n}}_{i,f} \times \mathbf{\Phi}_{l}^{j,f} d\mathbf{r} \\ \left[\mathbf{\bar{F}}_{\mathrm{he}}^{\mathrm{ii},f} \right]_{\mathrm{kl}} &= \frac{-Y_{f}^{j}}{Y^{i} + Y_{f}^{j}} \int_{\partial\Omega_{i,f}} \mathbf{\Psi}_{k}^{i} \cdot \mathbf{M}_{s} d\mathbf{r}. \\ \end{array}$$

It should be noted that $\overline{\mathbf{F}}_{e}^{i,M_s}$ and $\overline{\mathbf{F}}_{h}^{i,M_s}$ are two column vectors and nonzero only over the ventilation slots and apertures of the shielding enclosure.

In this work, 12 edge vector basis functions (six constant tangential/linear normal (CT/LN) and six linear tangential/linear normal (LT/LN) basis functions, respectively) are used for both **E** and **H** in each mesh element, i.e., $n_e^i = 12$ and $n_h^i = 12$ for $i = 1, \ldots, N$. Thus, the dimension of the matrix equations to be solved is 12 by 12. In this study, the inversion of the mass matrices are precalculated and stored before starting the time-marching scheme.

To solve the semidiscrete matrix equations from (12) to (13), the fourth-order Runge–Kutta method is employed. For explicit time-marching scheme, the Courant–Friedrichs–Lewy-like condition must be satisfied to ensure stability. In general, the time-step size δt is determined in terms of the following condition [33], [36]:

$$c_0 \delta t \le \min\{l_{\min}\sqrt{\epsilon_r \mu_r}/4(p+1)^2\}$$
(14)

where c_0 is the free-space light speed, p is the order of basis function. In this study, first-order basis functions are used, thus p = 1.

C. TDBI Equation

As a partial differential equation solver, DGTD method has to be truncated by artificial boundary conditions for open-space problems. At the truncation boundary $\partial\Omega$, the field values \mathbf{E}^{j} and \mathbf{H}^{j} in (8) and (9) used for incoming flux evaluation are not available. In this study, our previously developed hybrid DGTD and TDBI is employed by evaluating \mathbf{E}^{j} and \mathbf{H}^{j} using the equivalent electric current $\mathbf{J}_{i',f'}^{h}$ and magnetic current $\mathbf{J}_{i',f'}^{e}$ over a Huygens' surface enclosing the scatterer [33]. Namely,

$$\mathbf{E}_{f}^{j,\partial\Omega}(\mathbf{r},t) = \sum_{i'} \sum_{f'} [\mu_0 \mathcal{L}_{i',f'}(\mathbf{J}_{i',f'}^{\mathrm{h}}) - \mathcal{K}_{i',f'}(\mathbf{J}_{i',f'}^{\mathrm{e}})]$$
$$\mathbf{H}_{f}^{j,\partial\Omega}(\mathbf{r},t) = \sum_{i'} \sum_{f'} [\epsilon_0 \mathcal{L}_{i',f'}(\mathbf{J}_{i',f'}^{\mathrm{e}}) + \mathcal{K}_{i',f'}(\mathbf{J}_{i',f'}^{\mathrm{h}})] \quad (15)$$

where the operators $\mathcal{L}_{i',f'}$ and $\mathcal{K}_{i',f'}$ are defined as

$$\mathcal{L}_{i',f'}(\mathbf{J}) = -\frac{1}{4\pi} \int_{\partial\Omega_{i',f'}} \frac{\partial_t \mathbf{J}(\mathbf{r}', t - R/c)}{R} d\mathbf{r}' + \frac{c^2}{4\pi} \nabla \int_{\partial\Omega_{i',f'}} \int_0^{t - R/c} \frac{\nabla' \cdot \mathbf{J}(\mathbf{r}', t')}{R} dt' d\mathbf{r}' \mathcal{K}_{i',f'}(\mathbf{J}) = \frac{1}{4\pi} \nabla \times \int_{\partial\Omega_{i',f'}} \frac{\mathbf{J}(\mathbf{r}', t - R/c)}{R} d\mathbf{r}'.$$
(16)

Since the equivalent Huygens' current sources are calculated by DGTD, all time-marching schemes are conducted explicitly, and no matrix inversion is involved. Thus, compared with traditional FEM-BI, the DGTD-BI scheme is more efficient.

D. Comments and Discussions

Due to the unavailability of the NF measurement equipment, only the simulated NF electric field data is used instead. In fact, we first use our DGTD solver to straightforwardly get the tangential components of the electric field over the slots and apertures. Then, the DGTD scheme introduced above is further applied to calculated the radiated emission outside the shielding enclosure. For practical situations, the time-step resolution $\delta t_{\rm meas}$ used for NF sampling is usually different with



Fig. 2. Schematic illustration of the linear interpolation method. The function value f_1 is interpolated based on f_0 and f_2 and express as $f_1 = P_1 f_0 + P_0 f_2$, $P_0 = (t_1 - t_0)/(t_2 - t_0)$ and $P_1 = (t_2 - t_1)/(t_2 - t_0)$.

the time-step size $\delta t_{\rm DG}$ for the DGTD based solvers (see 14). Thus, the equivalent magnetic current \mathbf{M}_s at $t = n \delta t_{\rm DG}$ on the right-hand side of (12) and (13) must be interpolated from the sampled NF electric field. To facilitate the interpolation scheme, the shifted polynomials T(t) are deployed as the temporal basis functions [33]. That is,

$$T(t) = \begin{cases} 1 - t/|\Delta t_{\text{meas}}| & -\Delta t_{\text{meas}} \le t \le \Delta t_{\text{meas}} \\ 0 & \text{otherwise.} \end{cases}$$
(17)

An schematic illustration is shown in Fig. 2.

To include the influence of the practical measurement errors on the accuracy of the proposed method, the artificial noise is added to the simulated NF data. The amount of the noise is gauged by the signal-to-noise ratio (SNR). The results obtained from both the noise-free and noise-contaminated NF data are presented and compared to verify the robustness of the developed approach.

III. NUMERICAL RESULTS

In this part, representative examples are provided to validate the proposed method, including a Hertzian dipole in the free space and two PCBs in shielding enclosures.

A. Hertzian Dipole in Free Space

With the purpose to demonstrate the accuracy of our approach, we consider a z-directed electric Hertzian dipole in free space as the first example. The tangential components of the electric field over a spherical surface ($r_{\rm meas} = 0.1$ m) enclosing the dipole are computed analytically by

$$E_{\theta} = \frac{\eta_0 \sin(\theta)}{4\pi R} \left[\frac{1}{c_0} \partial_t g(t - R/c_0) + \frac{g(t - R/c_0)}{R} + \frac{c_0}{R^2} \int_0^{t - R/c_0} g(\tau) d\tau \right]$$
(18)

where $g(t) = \frac{2}{15}(t-t_0)\exp(-(t-t_0)^2/t_m^2)$, $t_m = 1.27$ ns and $t_0 = 5t_m$.

For this example, the time-step sizes for the NF sampling and DGTD are $\delta t_{meas} = 10$ ps and $\delta t_{DG} = 1.2$ ps, respectively. And, the time-marching step-size for TDBI is $\delta t_{BI} = 21.1$ ps. The computed electric fields by the proposed approach at



Fig. 3. Calculated electric field component E_z at $\mathbf{r}_0 = 0.12 \ \hat{\mathbf{y}}$ m (a) and $\mathbf{r}_0 = 10 \ \hat{\mathbf{y}}$ m (b). For comparison, the analytical results by (18).



Fig. 4. Two-layer PCB with microstrip traces and vertical vias placed into a shielding enclosure with top-opened (denoted by the green surface, where the NF sampling is conducted). The parameters of the shielding box are defined as: $a = 6 \text{ cm}, b = 10 \text{ cm}, c = 18 \text{ cm}, h_1 = 2 \text{ cm}, \text{ and } h_2 = 1 \text{ cm}.$

 $\mathbf{r} = (0, 0.12, 0)$ m and (0, 10, 0) m are plotted in Fig. 3. For comparison, the analytical solutions are also provided. It is noted that excellent agreements are observed both in the NF and FF region.

B. PCB Board in a Top-Opened Shielding Enclosure

To further validate our approach, in the second example, the radiation from a PCB placed in a shielding box without top covers is investigated, as shown in Fig. 4. The PCB has two



Fig. 5. Calculated FF radiation patterns by the proposed method at $f_1 = 0.5$ GHz (a), $f_2 = 0.75$ GHz (b), and $f_3 = 1.0$ GHz (c).



Fig. 6. FF patterns in *xoy* and *yoz* planes corresponding to the 3-D patterns in Fig. 5.

dielectric layers with thickness denoted as h_1 and h_2 . The relative electric permittivities are 3.0 and 2.0, respectively. Three signal lines with six ports defined at the left and right side of the package are distributed over the two-layered PCB. In our simulation, the left three ports are stimulated by three lumped voltage sources with $R_s = 50 \ \Omega$.



Fig. 7. Calculated FF pattern at f = 1.0 GHz by the proposed approach.

First, we assume that the right three ports are shorted to the ground (a PEC boundary condition), and the NF electric fields over the top cover are obtained by time-domain simulation, and the corresponding sampling time-step size is around 4.62 ns. Next, the above proposed scheme is facilitated to calculate the radiated emission outside the shielding box. For this step, the time-step sizes for DGTD and TDBI are $\delta t_{\rm DG} = 0.59$ ns and $\delta t_{\rm BI} = 13.61$ ns, respectively. In Fig. 5, the FF radiation patterns at frequency f = 0.5, 0.75, and 1.0 GHz are presented. For comparison, the simulated counterparts by direct full-wave simulation are also shown in Fig. 6. Obviously, very good agreements are achieved. It is noted that the forward radiation becomes stronger and the beam is more narrow with the frequency increasing.

Second, the situation when the right three ports are floating in the space are considered. Similarly, the simulated NF fields over the top cover are used as the equivalent magnetic current $M_s(\mathbf{r}', t)$. For this example, only the 3-D FF radiation pattern at f = 1.0 GHz are calculated and shown in Fig. 7, while the 2-D FF patterns in xoz and yoz planes at f = 0.5, 0.75, and 1.0 GHz are plotted in Fig. 8. The simulated references are also given for accuracy comparison. Clearly, good agreements are noted.

C. PCB in a Shielding Enclosure With Slots

In the last example, a PCB placed in a shielding enclosure with two ventilation slots is demonstrated, as shown in Fig. 9. The thickness and the relative electric permittivity of the substrate



Fig. 8. FF patterns in xoy and yoz planes corresponding to the 3-D patterns in Fig. 7.

are 0.02 and 2.2 m, respectively. The left port is driven by a lumped voltage source [38] defined as

$$V_{s}(t) = e^{-\alpha_{1}^{2}(f_{2}-f_{1})^{2}\left(t-\frac{\alpha_{2}}{f_{2}-f_{1}}\right)^{2}} \times \cos\left[2\pi \frac{f_{1}+f_{2}}{2}\left(t-\frac{\alpha_{2}}{f_{2}-f_{1}}\right)\right]$$

with $f_1 = 0.4$ GHz, $f_2 = 1.6$ GHz, $\alpha_1 = 1.035$ and $\alpha_2 = 2.539$, and the right port is loaded with a resistor $R_0 = 50 \Omega$. To facilitate the proposed algorithm, the temporal tangential electric fields over the slots are obtained via simulation with sampling time resolution $\delta t_{\text{meas}} = 5.64$ ps. Due to the strong cavity resonance, the sampling is conducted over a long time duration around 176 ns. Then, the proposed strategy is applied to characterize the radiation outside the shielding box. The time-step sizes for DGTD and TDBI are $\delta t_{\text{DG}} = 0.58$ ps and $\delta t_{\text{BI}} = 19.72$ ps, respectively. In Fig. 10, the recorded electric field at (0, 0, 0.12) m is plotted. The reference solution is also provided. It can be seen that the fields take much time to degrade because of the cavity resonance. In Fig. 11, the computed 3-D FF patterns at



Fig. 9. PCB in a shielding enclosure with parameters defined as a = 0.14 m, b = 0.22 m, and c = 0.3 m. The width and length of the two slots are 0.02 and 0.2 m, respectively.



Fig. 10. x, y, and z-components of the electric field at $\mathbf{r}' = 0.12 \ \hat{\mathbf{z}}$ as the function of time t.



Fig. 11. Obtained FF 3-D patterns at frequencies $f_1 = 0.5$ GHz (left) and $f_2 = 1.25$ GHz (right).



Fig. 12. 2-D FF patterns in *xoz* and *yoz* planes corresponding to the 3-D patterns in Fig. 11.

f = 0.5 and 1.25 GHz are shown. To compare with the reference results, the 2-D patterns in xoz and yoz planes are plotted in Fig. 12. Again, very good agreements between the proposed results and the reference solution are reached.

To characterize the cavity resonance enhanced radiation, the radiated energy normalized to the source power is calculated by

$$\mathbf{P}_{r}(\omega) = \mathbf{R}_{s} \times \frac{\oint_{S} \mathbf{E}(\omega) \times \mathbf{H}^{*}(\omega) dS}{||\mathbf{V}_{s}(\omega) \times \mathbf{V}_{s}^{*}(\omega)||}$$

where $R_s = 50 \Omega$ denotes the source impedance, and the integration is conducted over a surface S enclosing the shielding box. The calculated result from 0.5 to 1.2 GHz is presented in Fig. 13, which agrees to the solution obtained by direct simulation very well. Based on the result, it is interesting to found that the cavity resonance has significant influence on the radiation intensity.



Fig. 13. Radiated power versus frequency by the proposed algorithm and the reference result obtained by straightforward simulation.



Fig. 14. Calculated NF electric field using noise-contaminated data with different SNRs by the proposed method. The x (a) and y (b) components of near electric-field.



Fig. 15. FF pattern calculated by noise data with $SNR = 3 \ dB$ (a) and $SNR = 10 \ dB$ (b).

D. Investigation of Noise Influence

For practical NF scanning situation, the reliability of the measurement data is highly affected by uncertainty faults including probe-positioning error, the dynamics of the probe, background noise, and the influence of cables, etc. Thus, it is necessary to investigate the robustness of the proposed approach if the noisepolluted NF data was employed. To achieve this objective, we artificially add noise with different SNR to the simulated NF data. The benchmark in Section III-B is revisited again, but only the open-circuit case is considered. First, the NF data at $\mathbf{r}' = 0.1 \hat{\mathbf{z}}$ is calculated corresponding to different SNRs, as shown in Fig. 14. Significant influence on the NF data is observed. To study the influence on the FF patterns, in Fig. 15, the FF radiation pattern at 1.0 GHz using noise data is presented. Compared with the noise-free obtained FF pattern in Fig. 7, it is interestingly found that the noise has trivial effects on the FF patterns compared with the NF data.

IV. CONCLUSION

In this paper, a time-domain NF-FF transformation approach is proposed to model the radiated emissions from the electronic systems placed in shielding box using only near electric field over the ventilation slots and apertures. Because of unavailability of the analytical DGF in the presence of an arbitrary-shaped PEC box, the DGTD-based full-wave numerical algorithm is employed by considering the original radiation problem as a scattering issue from the PEC-filled shielding enclosure with incident wave generated by the equivalent magnetic currents $M_s = -\hat{n} \times E$ over the slots and apertures of the enclosure. Both analytical and numerical benchmarks are given to verify the developed method. The robustness of the approach is further verified by using noise-polluted NF data.

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