

## Forced Collision: Detecting Wormhole Attacks with Physical Layer Network Coding\*

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**Abstract:** Previous research on security of network coding focused on the protection of data dissemination procedures and the detection of malicious activities such as pollution attacks. The capabilities of network coding to detect other attacks have not been fully explored. In this paper, we propose a new mechanism based on physical layer network coding to detect wormhole attacks. When two signal sequences collide at the receiver, the starting point of the collision is determined by the distances between the receiver and the senders. Therefore, by comparing the starting points of the collisions at two receivers, we can estimate the distance between them and detect fake neighbor connections via wormholes. While the basic idea is clear, we have proposed several schemes at both physical and network layers to transform the idea into a practical approach. Simulations using BPSK modulation at the physical layer show that the wireless nodes can effectively detect fake neighbor connections without the adoption of special hardware or time synchronization.

**Key words:** physical layer network coding; wormhole attacks; cross-layer design

### Introduction

Investigators have proposed the physical layer network coding technique<sup>[1,2]</sup> to fully explore the advantages such as improved throughput, reduced congestion, and strengthened robustness. The technique is especially valuable in wireless networks when we consider the limited bandwidth and power resources of the nodes. Since network coding may allow data errors and/or corrupted packets to propagate widely and ruin the data recovery procedure at the final destination, previous research into network coding security focused on the protection of data dissemination procedures and the detection of malicious activities such as pollution

attacks<sup>[3,4]</sup>.

However, the security capabilities of physical layer network coding to detect malicious attacks have not been fully explored. For instance, it is possible that when signals collide at the receiver, we can potentially extract information about the network structure. This information can then be used to detect attacks on network topology. In this paper, we conduct an investigation of this problem. Specifically, we propose a new mechanism to detect wormhole attacks.

Several reasons lead us to choose wormhole attacks as the primary research topic for this investigation. First, wormhole attacks impose severe threats to the correct detection of network topology, which is the foundation of various operations within wireless networks such as routing and data transmission. Second, a wormhole attack is a representation of stealth attacks on wireless networks, where traditional methods such

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Received: 2011-06-21; revised: 2011-08-29

\* Supported in part by the NSF CNS Award (No. 1143602)

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as encryption and authentication cannot defend against such attacks. Therefore, a detection method based on physical layer network coding will allow us to better understand this problem. Finally, previous approaches for detecting wormhole attacks are usually implemented at the network layer. Our proposed approach uses physical layer properties. At the same time, our approach does not require time synchronization among wireless nodes or depend on any special hardware.

The basic idea of our proposed approach is as follows: when the long sequences from two senders collide at the receiver, the starting point of the collision between the sequences is jointly determined by the sending time and the physical distances across all the receiver and senders. For two receivers, their starting points of collision will be different, and this difference is restricted by the physical distance between them. Therefore, through measuring and comparing the overlapping parts of the received sequences, we can estimate the physical distance between two wireless nodes and detect the fake connection between them. Since the proposed approach only measures the starting point of the collision in the sequences, we do not need time synchronization among the wireless nodes. Our analysis will also show that the physical distances among the senders and receivers will not impact the detection results. Therefore, we can choose the senders from a large area within the network.

Although the basic idea of the proposed approach is clear, we need to design schemes at both physical layer and network layer to make the approach practical. At the network layer, we need to determine the senders and their data sequences. Mechanisms must be designed to prevent the man-in-the-middle attack. At the same time, the receivers need a scheme to verify the authenticity of the recovered sequences from collisions. At the physical layer, we need to carefully select data transmission parameters such as modulation and carrier frequency. Consequently, algorithms are designed to recover the received sequences. We will also investigate the impacts of different factors, such as phase shift and carrier frequency jitter, on the proposed approach using both analysis and simulation.

Our investigation has the following contributions:

- We make an attempt to explore the security capabilities of the physical layer network coding technique. The research will demonstrate that in addition to

improving the bandwidth efficiency and data robustness in wireless networks, physical layer network coding can also be used to detect malicious attacks. This research provides a new incentive for further development of this technique.

- The proposed wormhole detection mechanism does not require any special hardware or time synchronization in the wireless network. Therefore, existing systems can easily adopt the proposed approach without going through drastic structural and functional changes.

- We carefully design schemes in both network layer and physical layer to make the approach practical. Impacts of different factors in the communication channel are studied through theoretic analysis and simulation.

The remainder of the paper is organized as follows: in Section 1, we introduce the basic idea of the detection mechanism and the role of physical layer network coding in wormhole detection. Section 2 reviews the related work. Sections 3 and 4 design mechanisms in the network layer and in the physical layer to make the approach secure and practical. We perform both an analysis and simulations to investigate the impacts of different factors in the physical layer. In Section 5 we study the security and detection accuracy of the proposed approach. Finally, Section 6 concludes the paper.

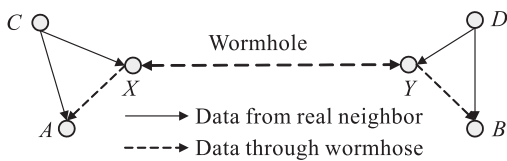
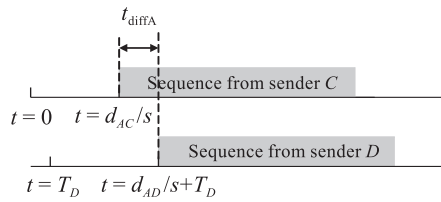
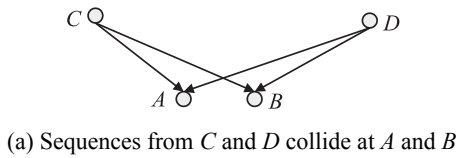
## 1 The Basic Idea

In this part, we introduce the basic idea of using physical layer network coding to detect wormhole attacks. We assume that two wireless nodes are neighbors if and only if the distance between them is shorter than  $r$ . However, this assumption does not restrict wireless nodes from transmitting signals at a higher power level in order to reach a longer distance. We assume the attackers are not capable of compromising any wireless nodes within the network. However, they can deploy their own nodes to eavesdrop on the traffic, tunnel the packets, and retransmit the data. In the following analysis, we use  $d_{MN}$  to represent the physical distance between two nodes  $M$  and  $N$ . We use  $T$  to represent a specific moment and  $t$  to represent a time duration. If the radio signal propagates at the speed of light  $s$ , the transmission delay between two nodes  $M$  and  $N$  will be  $\frac{d_{MN}}{s}$ . In the following

analysis, we describe the time difference between the received sequences. We are not using the system clocks to directly measure the actual time. On the contrary, we can pinpoint the starting bit in the sequence that the collision starts. Then we can translate this information into a time difference. This topic is discussed further in Section 5.1.

Figure 1a illustrates an example of using physical layer network coding to verify the neighbor relationship. We assume that nodes  $A$  and  $B$  in the network can hear each other and they want to verify the neighbor relationship. They jointly choose two other nodes,  $C$  and  $D$ , in the network that can both hear from.  $C$  and  $D$  will then generate and send out long random sequences that will collide at  $A$  and  $B$ . Without losing generality, we assume that node  $C$  will send out its sequence first. We assume that  $C$  starts sending at  $T_C = 0$  and  $D$  starts sending at  $T_D \geq 0$ .

Based on these assumptions, we can derive that  $A$  will receive the signals from  $C$  at the time  $\frac{d_{AC}}{s}$ , and the signals from  $D$  at  $\left(T_D + \frac{d_{AD}}{s}\right)$ . Therefore, the difference between the arriving time of the two sequences at node  $A$  is  $t_{\text{diff}A} = \left(T_D + \frac{d_{AD} - d_{AC}}{s}\right)$ , as



**Fig. 1** Two colliding sequences and the impacts of the wormhole

illustrated in Fig. 1b. In other words,  $A$  will first receive the sequence from  $C$  for  $t_{\text{diff}A}$  seconds, then the two sequences will collide at the node. If  $t_{\text{diff}A} < 0$ , the sequence from  $D$  will arrive first at  $A$ . Similarly, we can derive the difference between the arriving time at node  $B$  as  $t_{\text{diff}B} = \left(T_D + \frac{d_{BD} - d_{BC}}{s}\right)$ .

Now let us look at the difference between  $t_{\text{diff}A}$  and  $t_{\text{diff}B}$ :

$$t_{\text{diff}B} - t_{\text{diff}A} = \left(T_D + \frac{d_{BD} - d_{BC}}{s}\right) - \left(T_D + \frac{d_{AD} - d_{AC}}{s}\right) = \frac{(d_{BD} - d_{AD}) + (d_{AC} - d_{BC})}{s} \quad (1)$$

For the three nodes  $A$ ,  $B$ , and  $D$ , they either form a triangle or stay on the same line. Either way, we must have  $\|(d_{BD} - d_{AD})\| \leq \|d_{AB}\|$ . Similarly, we have  $\|(d_{AC} - d_{BC})\| \leq \|d_{AB}\|$ . Therefore, we must have:

$$\begin{aligned} \|(t_{\text{diff}B} - t_{\text{diff}A})\| &= \frac{\|(d_{BD} - d_{AD}) + (d_{AC} - d_{BC})\|}{s} \leq \\ &\frac{\|d_{BD} - d_{AD}\| + \|d_{AC} - d_{BC}\|}{s} \leq \frac{\|d_{AB}\|}{s} + \frac{\|d_{AB}\|}{s} = \\ &\frac{2 \times d_{AB}}{s} \leq \frac{2r}{s} \end{aligned} \quad (2)$$

The last part of the equation holds since when  $A$  and  $B$  are real neighbors, the distance between them is smaller than or equal to  $r$ . From Eq. (2), we can see that the difference between  $t_{\text{diff}A}$  and  $t_{\text{diff}B}$  is restricted by the physical distance between nodes  $A$  and  $B$ . In this way, the two nodes can compare the time differences between the received colliding sequences to verify their neighbor relationship.

Below we will study the case when  $A$  and  $B$  are not real neighbors and they have to communicate through a wormhole. Here we adopt a simplified model of attackers and assume that the two attackers  $X$  and  $Y$  can send and receive radio signals at the same time. More realistic scenarios will be discussed in Section 4. Since the malicious nodes possess total control over the tunneling procedure, in the following analysis we assume that  $X$  and  $Y$  will introduce extra delay  $t_{\overline{XY}}$  and  $t_{\overline{YX}}$  for the traffic transmitted in different directions. This scenario is illustrated in Fig. 1c.

Following the previous assumptions, we can derive that  $A$  will receive the sequence from  $C$  at time  $\frac{d_{AC}}{s}$ ,

and the sequence from  $D$  at time  $\left(T_D + \frac{d_{DY} + d_{XY} + d_{AX}}{s} + t_{\overline{YX}}\right)$ . Similarly,  $B$  will receive the sequence from  $C$  at time  $\left(t_{\overline{XY}} + \frac{d_{CX} + d_{XY} + d_{BY}}{s}\right)$ , and the sequence from  $D$  at time  $\left(T_D + \frac{d_{BD}}{s}\right)$ . Therefore, we have

$$t_{\text{diffA}} - t_{\text{diffB}} = t_{\overline{XY}} + t_{\overline{YX}} + \frac{(d_{DY} + d_{BY} - d_{BD})}{s} + \frac{(d_{AX} + d_{CX} - d_{AC})}{s} + 2 \times \frac{d_{XY}}{s} \quad (3)$$

Since the three nodes  $A$ ,  $C$ , and  $X$  either form a triangle or are on the same line, we must have  $(d_{AX} + d_{CX} - d_{AC}) \geq 0$ . Similarly, we have  $(d_{DY} + d_{BY} - d_{BD}) \geq 0$ . The extra transmission delay  $t_{\overline{XY}}$  and  $t_{\overline{YX}}$  introduced by the malicious nodes cannot be smaller than 0. Therefore, we have

$$\|t_{\text{diffA}} - t_{\text{diffB}}\| \geq \left(2 \times \frac{d_{XY}}{s}\right) \quad (4)$$

When the length of the wormhole  $d_{XY}$  is longer than the radio transmission range  $r$ , we have  $\|t_{\text{diffA}} - t_{\text{diffB}}\| > \frac{2r}{s}$ . Combining the results in Eqs. (2) and (4), we find that two nodes in the wireless network can verify their neighbor relationship by comparing the differences between the starting points of collision in the received sequences.

The proposed approach has several highly desirable properties. First, since the mechanism uses only the starting points of the collision between the sequences to detect wormholes, we do not need the senders or receivers to synchronize their clocks. As illustrated in Eqs. (2) and (4), the parameter  $T_D$  has been canceled out. Second, in Eq. (2) the physical distances between the senders and the receivers have also been canceled out. The difference is determined only by the physical distance between the nodes that want to verify their neighbor relationship. This implies that we can choose the senders from a large area in the network, and they do not need to be direct neighbors of  $A$  and  $B$ . Third, the proposed mechanism does not require the wireless nodes to be equipped with any special hardware which will result in a lower node cost. The capabilities of the nodes to recover colliding sequences will be discussed in Section 4. Finally, the proposed

approach works in a distributed manner and does not require a centralized controller. Nodes  $A$  and  $B$  can determine their senders and exchange  $t_{\text{diffA}}$  and  $t_{\text{diffB}}$  to detect wormholes. With these desirable properties, the approach can be easily adopted by existing networks.

## 2 Related Work

### 2.1 Wormhole detection

**Location and Time Based Solutions** This group of solutions try to restrict the transmission range of a packet by measuring the time and/or positions of the wireless nodes. For example, packet leash is proposed by Hu et al.<sup>[5]</sup> for wormhole prevention. The geographic leashes and temporal leashes use location information and signal propagation delay respectively to verify a neighbor relation. In SECTOR<sup>[6]</sup>, the wireless nodes use a special hardware to respond to a one-bit challenge. The challenger measures the round trip time to estimate the distance between the nodes. Using directional antenna<sup>[7]</sup>, the neighbor relation between two nodes can be verified based on the directions of the received signals. In LiteWorp<sup>[8]</sup>, the wireless nodes use the short safe period after deployment to detect the real 1-hop and 2-hop neighbors. They will then monitor the packet forwarding actions to detect wormholes. The improved approach<sup>[9]</sup> for wormhole detection in mobile wireless networks requires the nodes to have GPS and loosely synchronized clocks. The EDWA<sup>[10]</sup> method also requires the wireless nodes to be equipped with GPS. In TrueLink<sup>[11]</sup>, the wireless nodes strictly follow the 802.11 standard of the time interval between packets to restrict their transmission distances. It requires the wireless nodes to have very accurate clocks.

**Graph Based Approaches** Investigators have tried to detect wormholes based on their impacts on the network topology. MDS-VoW<sup>[12]</sup> is a centralized mechanism for wormhole detection in sensor networks. It reconstructs the layout of sensors using multi-dimensional scaling and detects wormholes by visualizing the anomalies introduced by the attacks. A decentralized approach for dynamic networks is proposed in Ref. [13]. In Ref. [14], the researchers analyze the geometric random graphs induced by the communication range constraint of the nodes. They present a defense mechanism based on local broadcast keys.

Maheshwari et al.<sup>[15]</sup> model the wormhole detection problem as a disk graph embedding task. They design a localized algorithm to locate the forbidden substructures in the connectivity graph.

**Statistical Analysis Methods** In Ref. [16], the investigators study the impacts of wormholes on multi-path routing protocols. They try to locate the hot links that are contained in a majority of the obtained routes. In NNT and ADT<sup>[17]</sup>, the researchers try to detect increases in the node degrees and decreases in the shortest paths caused by the wormholes.

## 2.2 Physical layer network coding

Physical layer Network Coding (PNC) tries to turn the broadcast property of wireless networks to a capacity boosting advantage. It uses the additive nature of the electromagnetic waves to serve as the coding procedure. The PNC technique under QPSK modulation is studied in Ref. [2]. The researchers investigate the general modulation-demodulation principles and analyze the performance penalty of different factors. In Ref. [1], the authors try to decode the interfered signals under MSK modulation. The mechanism can recover the colliding sequences under phase shift and the lack of synchronization. After these pioneering papers, research on PNC focuses on improving the decoding accuracy. In Ref. [18], the authors compare the amplify-and-forward and decode-and-forward techniques. Zhang et al. investigate the decoding techniques of PNC over finite and infinite fields in Ref. [19]. In Ref. [20], the authors propose to dynamically adjust the coefficients to increase the ‘distances’ among different codes. Investigators also proposed to adopt Tomlinson-Harashima precoding to improve the data recovery accuracy<sup>[21]</sup>. The determination of threshold values for decoding in two-way relay channels is studied in Ref. [22].

## 3 Building a Practical Approach: Network Layer Issues

In Section 1, we introduce the basic idea of using physical layer network coding to detect wormhole attacks. However, several issues need to be solved before the idea can be turned into a viable solution. In this section we focus on the issues in the network layer. The physical layer issues will be handled in the next

section.

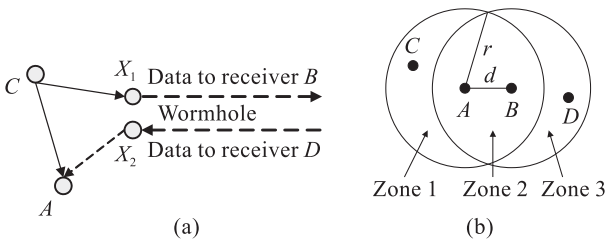
### 3.1 Assumptions and model of attackers

We assume that the links among wireless nodes are bidirectional and the two neighboring nodes can always send packets to each other. We adopt the unit disk graph model in this work and assume that two wireless nodes are neighbors when the distance between them is shorter than  $r$ , where  $r$  is defined as the communication range. We assume that the wireless nodes can adjust the transmission power such that the signal range can be increased, e.s.  $2r$ . We assume that each node is equipped with an omni-directional antenna. We also assume that the communication channel is half duplex and a node cannot transmit and receive signals at the same time. The wireless nodes will periodically broadcast neighbor discovery beacons such that changes in neighbor lists can be detected.

We assume that the wireless nodes share a secure, light-weight Pseudo Random Bit Generator (PRBG)<sup>[23]</sup>. The senders will use this generator to determine the sequences. By exchanging only the seeds for the PRBG, the receivers can regenerate the sequences and determine whether or not they have successfully recovered the sequences. Since we assume that the malicious nodes are all external attackers, the wireless nodes will employ encryption to protect the data communication amongst them. They can use either group keys or pair wise keys. Note that the generation and maintenance of the keys is beyond the scope of this paper.

For the attackers, we assume that they cannot compromise the legitimate nodes in the wireless networks. At the same time, they cannot break the secret keys amongst the legitimate nodes by passively listening to the communication channel. The attackers can deploy their own nodes in the network to form wormholes. We assume that the attackers can communicate with each other through a real-time, long-range, out-of-band channel.

The assumption of the half-duplex channel has some impacts on the analysis of data collision through the wormhole. As illustrated in Fig. 1c, the malicious node  $X$  cannot simultaneously listen to the sequence from  $C$  and forward data to  $A$ . It has to be decoupled into two nodes,  $X_1$  and  $X_2$ , in order to accomplish these tasks. As illustrated in Fig. 2a,  $X_1$  can get a copy of



**Fig. 2 Practical issues in the network layer: (a) a more realistic node model of the attackers for the half-duplex channel; (b) the zones that the senders can be chosen from**

the data that  $X_2$  is transmitting through the out-of-band channel. Therefore,  $X_1$  will be able to decode the sequence from  $C$  in the presence of interference. Decoupling the node  $X$  into two nodes will introduce some changes to Eq. (4). However, these changes can be hidden in the transmission delay of the wormhole and will not subvert our approach.

### 3.2 Selection of senders

In this part we study two problems: first, how to choose the senders in a real network environment; second, the relationship between the wormhole detection probability and the number of rounds of verification. Answers to these questions will allow us to better understand the advantages and limitations of the proposed approach.

#### 3.2.1 Selection of senders

The analysis in Section 1 showed that the detection of wormholes will not be impacted by the distances among the senders and receivers. However, in a real wireless network, several reasons restrict us from choosing a sender that is multiple hops away from the receiver. First, if the sender is far away from the receivers, it has to transmit the signal at a high power level. This will not only consume the limited battery power of the sender but it will also cause interference in a large area. Second, if we choose a sender that is multiple hops away, this path has a higher probability to contain a wormhole. The malicious nodes can then manipulate the arriving time of the sequences and compromise the detection mechanism. Therefore, we propose to choose the senders from the union of the neighbor lists of the receivers.

Figure 2b shows the areas that the senders can be chosen from. As an example, nodes  $A$  and  $B$  want to verify their neighbor relationship. They jointly

choose the senders  $C$  and  $D$  such that  $C$  is a direct neighbor of  $A$  and  $D$  is a direct neighbor of  $B$ . Since  $A$  and  $B$  are neighbors, the senders must be within the distance  $2r$  to both of the receivers. In this way, the senders can adjust their sending power to make sure that the signals can be received by both of the receivers.

This scheme will greatly increase the pool of senders that we can choose from. As shown in Fig. 2b, if we require the senders to be direct neighbors of both receivers, we can choose senders only from zone 2. Now we can choose from zones 1 and 3 as well. If the distance between  $A$  and  $B$  is  $d$  where ( $d \leq r$ ), the size of zone 2 is

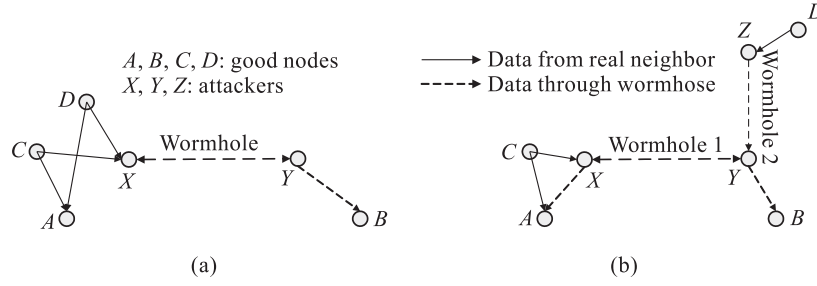
$$\text{Area}_{\text{zone2}} = 2r^2 \arccos\left(\frac{d}{2r}\right) - d\sqrt{r^2 - \left(\frac{d}{2}\right)^2}$$

and the size of zone 1 is  $\pi r^2 - \text{Area}_{\text{zone2}}$ . Therefore, if the distance between  $A$  and  $B$  has a uniform distribution on the interval  $[0, r]$ , we can calculate the average size of zone 2. We find that on average the ratio between the total size of zones 1, 2, and 3 and the size of zone 2 is about 1.9. This implies that our approach has a much larger pool of senders to conduct wormhole detection.

#### 3.2.2 Determining number of verification rounds

In Fig. 1c, we show one possible scenario of sender selections in which  $C$  and  $D$  are at different sides of the wormhole. Since the wireless nodes cannot distinguish a real neighbor from a fake neighbor through the wormhole, there is a chance that both senders are located at the same side of the wormhole. At the same time, the existence of multiple wormholes in the network can also create more complicated scenarios. In Fig. 3, we illustrate two such cases. In both scenarios, the sequences from  $C$  and  $D$  will go through a wormhole to reach  $B$ . Therefore, the malicious nodes can manipulate the difference between the arriving time of the two sequences to compromise the proposed approach. To mitigate such attacks, we propose to conduct multiple rounds of verification with different senders to improve the odds of countering the malicious nodes.

We assume that nodes  $A$  and  $B$  are connected through a wormhole and they want to verify their neighbor relationship. We assume that the number of real neighbors of  $A$  and  $B$  are  $RN_A$  and  $RN_B$ ,



**Fig. 3 Neighbor selection scenarios that can avoid detection**

respectively. Similarly, the number of fake neighbors of the two nodes through the wormhole are  $FN_A$  and  $FN_B$ . Therefore, the probability that we choose one real neighbor for each receiver in order to form the senders within  $p$  rounds is

$$1 - \left( 1 - \frac{RN_A}{RN_A + FN_A} \cdot \frac{RN_B}{RN_B + FN_B} \right)^p \quad (5)$$

Based on this equation, we can see that the malicious nodes can reduce the probability of being detected by introducing a large number of fake neighbors via wormholes. However, in real wireless networks there are several reasons that will restrict the attackers from doing this. First, when the attackers deploy a large number of malicious nodes to create numerous wormholes, it will become fairly difficult for them to maintain a web of real-time, out-of-band communication channels across all of these nodes. Second, the legitimate nodes possess a good estimate of the node density and the average number of neighbors in the network. Previous research efforts<sup>[24,25]</sup> have shown that the node degrees in MANETs follow some distributions. Therefore, if the wormholes make the node degrees abnormally large, the legitimate nodes will become suspicious and adopt other mechanisms to detect the wormholes. If the node degrees follow some distributions such as binomial<sup>[25]</sup>, the wireless nodes can easily figure out the corresponding parameters to achieve a certain detection probability.

### 3.3 Generation of sending sequences

The sequences that the senders transmit should satisfy two requirements: First, the receivers should be able to verify the authenticity of the sequences to make sure that they are generated by the senders. Second, the sequences should be kept as a secret from the attackers before they are sent out. The first requirement will guarantee that the attackers cannot generate some

random sequence to deceive the receiver. As illustrated in Fig. 1c, if the receivers cannot verify the authenticity of the sequences, the malicious nodes  $X$  and  $Y$  can generate some random sequences to send to  $A$  and  $B$ . In this way, they can easily control the difference between the arriving time of the two sequences and compromise the proposed approach. The second requirement can prevent the man-in-the-middle attack. If the attackers know the sequences before they are sent by  $C$  and  $D$ , they can impersonate the senders and control the starting point of the collision of the sequences at the receivers.

To satisfy these requirements, the wireless nodes can use the following procedure to generate the sequences. We assume that every node is equipped with the same PRBG. They also have a secure channel to exchange information and the attackers cannot gain access to the data. Therefore, the two senders and two receivers can jointly determine two random numbers. These numbers will be used by the two senders as the seeds for the PRBG. Since the receivers also know the seeds, they can easily verify the received sequences. At the same time, the seeds will be kept as a secret from the attackers.

### 3.4 Neighbor verification procedure

Given the building blocks at the network layer, the following neighbor relation verification algorithm is employed.

(1) When two nodes  $A$  and  $B$  want to verify their neighbor relationship, each of them will choose one neighbor from their neighbor lists, namely  $C$  and  $D$ , to be the senders.  $C$  and  $D$  should be within  $2r$  to both  $A$  and  $B$ .

(2) The four nodes will jointly choose two seeds  $r_C$  and  $r_D$  for the PRBG at  $C$  and  $D$  to generate the sequences.  $A$  and  $B$  will also have a copy of the seeds.

(3)  $A$  uses  $(r_C \text{ xor } r_D)$  as the seed for the PRBG to

generate a series of pilot bits.  $A$  will broadcast the pilot bits at the power level such that  $B$ ,  $C$ , and  $D$  will all receive the data to learn that the verification procedure starts.

(4)  $C$  and  $D$  will verify the pilot bits from  $A$ . Each of them will then choose a random delay to make sure that  $A$  and  $B$  are ready to receive. Then, the two nodes will send out the sequences generated by the PRBG based on the seeds  $r_C$  and  $r_D$ . They will send the sequences with a sufficiently high power level such that both  $A$  and  $B$  can receive them. The two sequences will be long enough such that a large part of the sequences will collide at the receivers.

(5)  $A$  and  $B$  will use the algorithm in Section 4 to separate the sequences and verify them. The two nodes will exchange the starting points of the collisions and use the method described in Section 1 to verify their neighbor relationship.

(6) Steps 1 to 5 will repeat until  $A$  and  $B$  find that they are connected through a wormhole or they are convinced that they are real neighbors after  $p$  rounds.

## 4 Building a Practical Approach: Physical Layer Issues

To turn the proposed approach into a practical solution, the physical layer needs to accomplish the following tasks. First, the physical layer needs to successfully separate the two interfered sequences. It also needs to locate the starting point of the collision so that the information can be used to detect wormholes. Second, we need to assess the impacts of different factors in the physical layer on the proposed approach. In the following subsections, we will determine the parameters for signal transmission, design the receiver algorithm to separate the colliding sequences, and evaluate the approach under different parameters through theoretical analysis and simulation.

### 4.1 Modulation of signals

When the two senders generate their sequences using the PRBG, the data bits need to be modulated and demodulated in order to achieve over-the-air transmission. Thus, we need to decide on a proper modulation/demodulation scheme on both ends.

#### 4.1.1 Binary Phase Shift Keying (BPSK)

Phase-Shift Keying (PSK) is a digital modulation

scheme that conveys data by modulating the phase of the carrier wave. Since any digital modulation scheme uses a finite number of distinct signals to represent digital data, PSK uses a finite number of phases that are each assigned with a unique pattern of binary bits. The demodulator, which is designed specifically for the symbol set used by the modulator, determines the phase of the received signal and maps it back to the symbol it represents, thus recovering the original binary data. This requires the receiver to be able to compare the phase of the received signal to a reference signal.

BPSK is the simplest form of PSK. It uses two phases which are often separated by  $\pi$ . Using BPSK, a symbol can be expressed by the following formula:

$$s_i(t) = \cos(2\pi\omega_c t + \theta_i), \quad i = 1, 2,$$

where  $\theta_i$  is the phase of the symbol and  $|\theta_1 - \theta_2| = \pi$ .

It does not particularly matter exactly where the constellation points are positioned so long as their phase difference is sufficiently large, e.g.,  $\pi$ .

When we consider that there are two senders in the proposed mechanism, the  $j$ -th output symbol of sender  $i$  can be expressed as

$$s_{ij}(t) = \cos(2\pi\omega_c t + \theta_{ij}), \quad i = 1, 2, j = 1, 2,$$

where  $\theta_{ij}$  is the phase, and  $\theta_{11} = \theta_1$ ,  $\theta_{12} = \theta_1 + \pi$ ,  $\theta_{21} = \theta_2$ ,  $\theta_{22} = \theta_2 + \pi$ .

#### 4.1.2 Why BPSK

Several reasons lead us to choose BPSK as the modulation scheme for the proposed mechanism. First, BPSK is a very robust modulation scheme. Compared to the other PSK schemes, the constellation points of BPSK are the farthest away from each other, which means it takes a substantial amount of noise or distortion to make the demodulator reach an incorrect decision. This property is especially important when we consider that the receiver must verify the authenticity of the received sequences to avoid attacks on the proposed approach.

This modulation scheme will also help the receiver separate the two sequences. Using BPSK, the largest phase difference among the four modulated symbols is  $\pi/2$ . When the two input sequences are orthogonal to each other, it is straightforward for the receiver to distinguish between those two sequences from their collision. Furthermore, the structure of the receiver is much simpler compared to the other modulation schemes, resulting in lower implementation costs of the



proposed approach.

## 4.2 Data recovery algorithms

Data recovery is the most important task that the receiver needs to implement. Below we will describe in detail the sequence detection and separation algorithms. For simplicity, we do not consider frequency jitter and power amplitude in this subsection, although they will be discussed later in this section.

### 4.2.1 Packet reception

When we are designing the physical layer mechanisms, the first question we need to answer is how the receiver can detect the arrival of a data packet. This is a standard problem in digital communication. Since the received signal demonstrates a much higher energy level than that of the white noise, the receiver can look at the incoming energy level to detect the reception of data packets.

Next, since our approach does not require the wireless nodes to maintain synchronized clocks, there is a good chance that the sequence from one sender will arrive at the receiver first. Therefore, the receiver must be able to locate the starting point of the collision. Before this point, the receiver runs standard BPSK decoding. After this point, the receiver will treat the data as a packet corrupted by interference. It will then execute the interference decoding algorithm described below. To answer this question, the receiver will measure the variance in the energy level of the incoming signals. Since BPSK encodes the bits in the phase, the energy of a non-interfered BPSK signal is nearly constant. When two signals collide at the receiver, the variance will become much larger. Therefore, we can set up a threshold, and when the variance is larger than the pre-determined value, the sequence separation algorithm will be executed.

### 4.2.2 Data recovery

As described in Section 4.1.2, one of the key advantages of using two BPSK signals is to simplify the structure of the receiver. Given the modulation scheme in Section 4.1.2, the receiver only needs a low pass filter and an oscillator, which generates the cosine wave of the same phase offset as one of the sequences. Without loss of generality, we assume its phase offset to be the same as Sequence 1. Therefore, the receiver can be expressed as

$$r(t) = \cos(2\pi\omega_c t + \theta_1),$$

where  $\omega_c$  is the carrier frequency of the receiver and  $\theta_1$  is the phase of Sequence 1.

If the received signal is from Sequence 1, for example  $s_{11}$ , using trigonometric identities, the output of the oscillator will be

$$r_1(t) = s_{11}(t) \cdot r(t) = \cos(2\pi\omega_c t + \theta_1) \cdot \cos(2\pi\omega_c t + \theta_1) = \frac{1}{2}[1 + \cos(4\pi\omega_c t + 2\theta_1)] \quad (6)$$

Similarly, if the received signal is from Sequence 2, for example  $s_{21}$ , the output of the oscillator will be

$$r_2(t) = s_{21}(t) \cdot r(t) = \cos(2\pi\omega_c t + \theta_2) \cdot \cos(2\pi\omega_c t + \theta_1) = \frac{1}{2}[\cos(\theta_1 - \theta_2) + \cos(4\pi\omega_c t + \theta_1 + \theta_2)] \quad (7)$$

Since we attach a low pass filter after the oscillator at the receiver, the  $4\pi\omega_c t$  term in Eqs. (6) and (7) will be eliminated. Since the two sequences collide at the receiver, the final output of the filter will be

$$\tilde{r}(t) = \tilde{r}_1(t) + \tilde{r}_2(t) = \frac{1}{2} + \frac{1}{2}\cos(\theta_1 - \theta_2) \quad (8)$$

Since  $\cos(\theta_1 - \theta_2) \leq 1$ ,  $\tilde{r}_1(t) \geq \tilde{r}_2(t)$ , the demodulation is actually determined by  $\tilde{r}_1(t)$  such that the final output of the receiver is the recovered Sequence 1. In particular, when  $\theta_1 - \theta_2 = \pi/2$ ,  $\cos(\theta_1 - \theta_2) = 0$  so that  $\tilde{r}(t) = \tilde{r}_1(t)$ , there is no interference from Sequence 2, resulting in the recovered Sequence 1 being the most accurate. This is the orthogonal case mentioned in Section 4.1.2. When the phase difference between the two signals is not  $\pi/2$ , we propose to adopt the phase equalization method to compensate for this error. The details of the method will be described in Section 4.2.3. When the recovered Sequence 1 is obtained, it can be subtracted from the combined signal to yield Sequence 2. The receiver will then execute the decoding algorithm to recover the second sequence.

**Sequence Verification** As we discussed in Section 3, the receiver must verify the authenticity of the recovered sequences to defend against attacks from malicious nodes. Since the receiver has a copy of the seeds of the PRBG, it can regenerate the sequences. It will then compare the calculated sequences to the recovered ones. To distinguish a correct sequence from a random one, the similarity between the calculated sequence and the recovered one should be non-negligibly larger than 0.5. This threshold value shows that the proposed mechanism is very robust against bit errors in recovered sequences.

### 4.2.3 Improvement on the algorithm

Based on the discussion above, it is obvious that in order to achieve the highest recovery accuracy, we need to ensure that the phase offset of the receiver is consistent with the phase offset of Sequence 1 and that the phase difference between the two senders ( $|\theta_1 - \theta_2|$ ) is around  $\pi/2$ . However, in reality, the phase is actually a time-varying variable that depends on many factors. Consequently, we introduce pre-equalization here to compensate for this error.

Pre-equalization is a function applied at the transmitter that counteracts the phase degradation caused by the transmission channel. Equalization is implemented in two steps, namely, channel training and data transmission. In the first step, each of the two senders will send out some pilot bits to train the channel. The receiver will figure out how the channel influences the phases by comparing the received signals. Then, before the second step starts, the senders will adjust their phases based on the feedback from the receiver. Since we assume this communication system is in a pseudo-stationary state within a period of time, the channel condition in Step 2 is almost the same as in Step 1. Thus, these adjustments will lead to orthogonality in Step 2.

### 4.3 Impacts of various factors on BER

As discussed in Section 3, the receiver must verify the authenticity of the recovered sequences. Otherwise, an attacker can send out some random sequence and the receiver cannot distinguish it from the real sequence. In this subsection, we plan to investigate the impacts of various factors in the physical layer on the bit error rate (BER), which is defined as

$$\text{BER} = \frac{\text{number of incorrectly recovered bits}}{\text{total number of transmitted bits}}$$

#### 4.3.1 Phase difference

In Section 4.2.2, the final output of the filter is

$$\tilde{r}(t) = \tilde{r}_1(t) + \tilde{r}_2(t) = \frac{1}{2} + \frac{1}{2} \cos(\theta_1 - \theta_2).$$

When  $\theta_1 - \theta_2 = \pi/2$  such that  $\cos(\theta_1 - \theta_2) = 0$ , the two signals are orthogonal to each other and they have the least interference. When  $\theta_1 - \theta_2 = 0$  such that  $\cos(\theta_1 - \theta_2) = 1$ , then  $\tilde{r}_1(t) = \tilde{r}_2(t)$ , which means the interference from Sequence 2 is as strong as Sequence 1 itself. Therefore, the recovered Sequence 1 will be the least accurate. Using probability theory, we can

calculate the BER value in this case. There are four possible combinations of Sequence 1 and Sequence 2, namely  $\{(0,0),(0,1),(1,0),(1,1)\}$ . When the transmitted bits are (0,0) or (1,1), there will be no problem, since the interference of Sequence 2 will not change the decision on Sequence 1. However, when the transmitted bits are (0,1) or (1,0), the resulting signal is around 0, which means there is a probability of 0.5 that the recovered bit is wrong. Therefore, the BER here can be expressed as a conditional probability:

$$\text{BER} = P[E | (0,1) \cup (1,0)] \times P[(0,1) \cup (1,0)] = \frac{1}{2} \times \frac{1}{2} = \frac{1}{4} \quad (9)$$

where  $E$  is the event that a bit is incorrectly recovered.

When  $\theta_1 - \theta_2 \in (0, \pi/2)$  such that  $\cos(\theta_1 - \theta_2) \in (0, 1)$ . Since the cosine function is monotonically decreasing in the range  $(0, \pi/2)$ , we can expect that the interference from Sequence 2 decreases as  $\theta_1 - \theta_2$  increases, which means the BER is a monotonically decreasing function within the range  $[0, \frac{1}{4}]$  concerning phase difference. Note that the receiver can still successfully verify the recovered sequences with the 25% BER rate.

#### 4.3.2 Frequency jitter

In our previous analysis, the carrier frequencies of Sequence 1, Sequence 2, and the oscillator are assumed to be the same. However, similar to the behavior of the phase, the carrier frequency is also a time-varying variable. In this subsection, we will explore how the frequency jitter affects the BER performance. When taking frequency jitter into account, the symbol can be expressed as

$$s_i(t) = A \cos(2\pi(\omega_c + \omega_{\Delta i})t + \theta_i),$$

where  $\omega_{\Delta i}$  is the frequency jitter of the  $i$ -th carrier frequency. The frequency jitter of the oscillator is assumed to be  $\omega_{\Delta 3}$ .

As for Sequence 1, whose frequency jitter is  $\omega_{\Delta 1}$ , its output of the oscillator will be

$$\begin{aligned} r_1(t) &= s_1(t) \cdot r(t) = \\ & \cos[2\pi(\omega_c + \omega_{\Delta 1})t + \theta_1] \cdot \cos[2\pi(\omega_c + \omega_{\Delta 3})t + \theta_1] = \\ & \frac{1}{2} \{ \cos[2\pi(\omega_{\Delta 1} - \omega_{\Delta 3})t] + \cos[4\pi\omega_c t + 2\pi(\omega_{\Delta 1} + \omega_{\Delta 3})t + 2\theta_1] \} \end{aligned} \quad (10)$$

Due to the low pass filter, the final output of the filter will be

$$\tilde{r}_1(t) = \frac{1}{2} \cos[2\pi(\omega_{\Delta 1} - \omega_{\Delta 3})t] \quad (11)$$

Similarly, as for Sequence 2, whose frequency jitter is  $\omega_{\Delta 2}$ , its output of the low pass filter will be

$$\tilde{r}_2(t) = \frac{1}{2} \cos[2\pi(\omega_{\Delta 2} - \omega_{\Delta 3})t + (\theta_2 - \theta_1)] \quad (12)$$

Considering the orthogonal case, where  $\theta_2 - \theta_1 = \pi/2$ , Eq. (12) becomes

$$\tilde{r}_2(t) = \frac{1}{2} \cos[2\pi(\omega_{\Delta 2} - \omega_{\Delta 3})t + \pi/2] = \frac{1}{2} \sin[2\pi(\omega_{\Delta 2} - \omega_{\Delta 3})t] \quad (13)$$

In order to get an accurate recovery of Sequence 1, the  $\tilde{r}_1(t)$  should be as large as possible, while  $\tilde{r}_2(t)$  should be as small as possible. Therefore, we would like  $\omega_{\Delta 1} - \omega_{\Delta 3} = 0$  and  $\omega_{\Delta 2} - \omega_{\Delta 3} = 0$ . In other words, if the carriers have the same frequency jitter, it will have no effect on BER. Otherwise, it will result in an increased number of bit errors.

#### 4.4 Simulation results

In this subsection, we use computer simulators implemented in Simulink to explore the impacts of various factors on BER and compare them with the theoretical analysis results derived in Section 4.3.

##### 4.4.1 Phase difference and SNR

In real wireless networks, all the signals will pass through a noisy channel prior to arriving at the receiver. In wireless communication, an Additive White Gaussian Noise (AWGN) channel is the most widely used model and the Signal-to-Noise power Ratio (SNR) is a key metric of the transmission performance across this channel. Intuitively, a high noise level will result in a high BER rate.

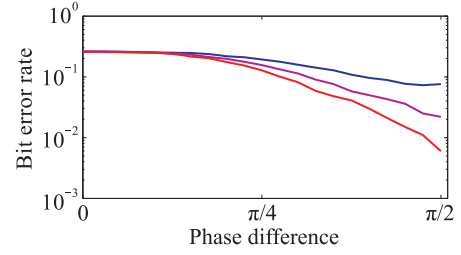
In this part, the relationship between the BER and phase difference, as well as BER and SNR, are studied. SNR values of 0 dB, 3 dB, and 5 dB are examined. The phase difference ranges from 0 to  $\pi/2$ . The resulting plot is shown in Fig. 4.

There are several important observations about the results shown in Fig. 4.

All the three curves are monotonically decreasing functions.

When the phase difference is equal to zero,  $\text{BER} \approx 0.25$  in all three cases.

Given the same phase difference, the BER is larger when there is a higher noise level.



**Fig. 4** The BER values with respect to phase difference and SNR. The blue curve is obtained when SNR=0 dB, the pink curve corresponds to SNR=3 dB, and the red curve is for SNR=5 dB.

All of these observations match the analysis results in Section 4.3.1.

##### 4.4.2 Power amplitude

In our previous discussions, we have not taken power amplitude into account. However, in an actual communication system, the power of a signal will gradually deteriorate on its way to the destination. Even when the two signals are transmitted using the same power, the received power will not be the same. Therefore, the resulting output of the filter should be rewritten as

$$\tilde{r}(t) = A_1 \tilde{r}_1(t) + A_2 \tilde{r}_2(t) = \frac{1}{2} A_1 + \frac{1}{2} A_2 \cos(\theta_1 - \theta_2) \quad (14)$$

where  $A_1$  and  $A_2$  are amplitude of the received Sequence 1 and received Sequence 2, which are different.

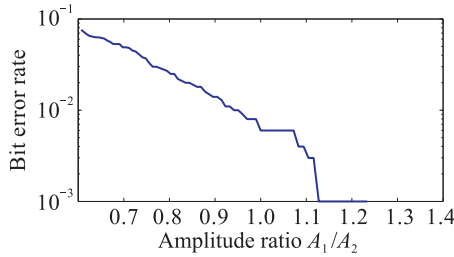
In order to recover Sequence 1 correctly, we want the interference from Sequence 2 to be as low as possible. This is a relative comparison between the two sequences, such that we can use a fraction to express their relationship:

$$\frac{P_1}{P_2} = \frac{A_1}{A_2 \cos(\theta_1 - \theta_2)}$$

Given  $\theta_1 - \theta_2$  is kept constant, if  $A_1$  becomes larger or  $A_2$  becomes smaller, the interference from Sequence 2 becomes weaker such that the recovered Sequence 1 is more accurate.

In the following simulation, we set phase difference between two signals to be  $\pi/2$  and the SNR to be 5 dB. We also assume that the receiver has the same phase offset as Sequence 1. The amplitude of Sequence 1 is increased from -5 dB to 5 dB, while the amplitude of Sequence 2 is decreased from 5 dB to -5 dB. Therefore, the ratio is monotonically increasing. The BER plot is shown in Fig. 5.

Based on Fig. 5, it is obvious that the power amplitude has an impact on BER. When  $A_2$  is much larger than  $A_1$ , the BER can be as high as 0.08. However,



**Fig. 5 The BER value with respect to amplitude. The x-axis is the ratio of amplitude between two sequences.**

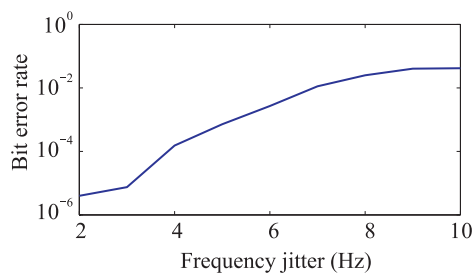
when  $A_1$  becomes larger than  $A_2$  ( $\frac{A_1}{A_2} > 1$ ), the BER value falls below 0.5%, which introduces a very low bit error rate.

The simulation results provide us some insight into the data recovery algorithm. When the senders send out the pilot bits to train the channel for phase equalization, the receiver can also provide feedback to them for their transmission power. Based on the signal deterioration model, we can control the power ratio between the received signals to achieve a balance between the recovery rates of the two sequences.

#### 4.4.3 Frequency jitter

In this subsection, the relationship between the BER and frequency jitter is studied. We set the phase difference of the two signals to be  $\pi/2$ , the amplitude of the two sequences to be the same, and the SNR value to be 5 dB. We change the carrier frequency of the receiver. Since the carrier frequency can be either smaller or larger than the normal one, we use frequency offset as the x-axis and the corresponding BER plot is shown in Fig. 6.

Based on Fig. 6, it is obvious that the frequency jitter also has an impact on the BER. As predicted in Section 4.3.2, when there is no frequency jitter, which means the two senders and the receiver have the same carrier frequency, the BER is the lowest. Consequently,



**Fig. 6 The BER value with respect to frequency jitter. The x-axis is the carrier frequency offset of the receiver.**

the more jitter presents in the system, the higher the BER will be. However, when the frequency jitter is within a range, we have a relatively low BER rate and the overall performance will not be severely hurt.

Having studied Figs. 4-6, we can conclude that phase difference has the largest impact on the BER rate. We can adopt different methods to compensate for the errors so that the detection capabilities of the proposed approach will not be severely impacted by these factors.

## 5 Discussion

### 5.1 Why depend on PNC to measure time difference

As shown in Section 1, the proposed approach measures the starting point of interference of two colliding sequences to estimate the distance between the receivers. Here we have to answer one question: why do not we directly use system clocks to measure the difference between the arriving time of two sequences? In that way, we can let the two senders send out their packets alternatively and still allow the receivers to estimate their distance.

Unfortunately, previous research<sup>[26,27]</sup> has shown that wireless nodes have a maximum clock drift rate at microsecond level ( $10^{-6}$  s). At the same time, the deviations of clock drift rates are also at the microsecond level. Equation (2) in Section 1 shows that when the two receivers are real neighbors, the difference between  $t_{diffA}$  and  $t_{diffB}$  is restricted by  $\frac{2r}{s}$ . If we assume that the radio range  $r$  is 250 meters and the signal propagates at the speed of light, the difference is roughly  $500 \text{ m} \div 300\,000 \text{ km/s} \approx 1.67 \times 10^{-6} \text{ s}$ . We can see that the measured duration and the clock drift are at the same level. Therefore, directly using the system clock to measure the time difference will introduce a large number of false alarms.

Physical layer network coding provides a solution to this problem. As the analysis in Ref. [1] shows, the wireless nodes can locate the bit from which the interference of two colliding sequences starts. If the wireless nodes are transmitting at the bit rate of 11 Mb/s,  $1.67 \mu\text{s}$  equals to the difference of 18 bits in the received sequences. With the continuous increase in the bit-rate of wireless networks, the difference will

become larger and larger. Therefore, physical layer network coding allows us to more accurately measure the difference and detect fake neighbor connections.

## 5.2 Security of the proposed approach

In Section 3 we discuss the authenticity of the received sequences and the prevention of man-in-the-middle attack. In this part, we study other security aspects of the approach.

When node  $A$  uses  $(r_c \text{ xor } r_d)$  as the seed to generate the pilot bits, it is very difficult for the attackers to counterfeit this information. If we assume that the seeds  $r_c$  and  $r_d$  have the length of  $k$  and the pilot bits have the length of  $h$ , the probability that an attacker can correctly regenerate the pilot bits without the information of  $r_c$  and  $r_d$  equals to  $\max(\frac{1}{2^h}, \frac{1}{2^k})$ . We can adjust the values of  $k$  and  $h$  to prevent the attackers from fabricating the starting signal and conducting man-in-the-middle attack on the mechanism.

Since the attackers have a total control over the tunneling procedure, they can block the verification procedure by discarding the packets going through the wormhole. This operation, however, will allow the legitimate nodes to derive more information about the wormholes. If node  $A$  fails to get a sequence from a sender and it is not because of the low quality of the communication channel, we conclude that there is a wormhole between  $A$  and the sender. This can be proven by contradiction. If there is no wormhole between  $A$  and the sender, we know that the distance between them is shorter than  $2r$ . Therefore, the sender will send out the sequence when it receives the pilot bits and  $A$  would have received the sequence. When node  $B$  fails to receive a sequence, it will exchange information with node  $A$ . If  $A$  gets that sequence,  $B$  concludes that there is a wormhole between the sender and  $B$ . It can draw this conclusion since node  $A$  confirms that the sender actually sends out the sequence. Therefore, if there is no wormhole between  $B$  and the sender, it would have received it. Based on the analysis, we can see that the attackers will expose more wormholes when they try to avoid detection by discarding packets.

Except for discarding packets, the attackers can also intentionally add noise to the packets when they tunnel

them through the wormhole. This operation may lead to one of the two results. If the introduced noises are not strong and the receivers can still verify the authenticity of the sequences, the neighbor verification procedure will not be impacted. On the contrary, if the bit error rate becomes very large and the receiver can no longer verify the authenticity of the sequence, it will treat the packet as a lost one. The receiver can then follow the description in the previous paragraph and treat the connection as a wormhole. This decision can be justified as follows: treating a very error-prone connection as a wormhole and avoiding it during the routing procedure will not significantly deteriorate the network performance.

## 5.3 False alarms of the proposed approach

False positive and false negative alarms are important parameters to evaluate a detection mechanism. In Section 3.2, we propose to adopt multiple rounds of verification to reduce false negative alarms. In this part, we focus on the investigation of false positive alarms.

When nodes  $A$  and  $B$  are real neighbors and the proposed approach identifies that they are connected through a wormhole, we have a false positive alarm. If both of the senders  $C$  and  $D$  are real neighbors to at least one of the receivers, we can derive that the two senders are within  $2r$  to the two receivers. In this way, both the pilot bits and the transmitted sequences will reach their targets and the verification procedure will complete successfully. Therefore, to cause a false positive alarm, we must have at least one sender connecting to both receivers through wormholes. Without losing generality, we assume that the sender is node  $C$ .

If the two receivers  $A$  and  $B$  get the sequence from  $C$  through the same sending operation of the wormhole, the attackers will not be able to manipulate the difference between  $t_{\text{diff}A}$  and  $t_{\text{diff}B}$  since this operation has the same effect as node  $C$  is at the position of the wormhole node. The attacker can keep the sequence in the wormhole for a period of time. This operation, however, has the same effect as node  $C$  adjusts its transmission time. Previous analysis has shown that this parameter will be removed from the final calculation result.

With this analysis, we find that the attackers need to deliver the sequence from  $C$  to the two receivers through two different sending operations so that they

can control the difference between their arriving time. This goal can be achieved through maintaining two separate wormholes to the receivers, or transmitting the sequences through different directional antennas. Both schemes will increase the deployment difficulty and the hardware costs of the attackers. At the same time, the following simulation will show that the false positive alarms have limited impacts on the average path length in the network.

In this simulation, we assume that the legitimate nodes are deployed randomly and uniformly in a  $2\text{ km} \times 2\text{ km}$  area. The transmission range  $r$  is 250 m. Two legitimate nodes  $A$  and  $B$  are real neighbors. When they want to verify the neighbor relationship, the attackers will transmit the sequences to them through two malicious nodes  $X$  and  $X'$  respectively. Here  $X$  is only a neighbor of  $A$  and  $X'$  is only a neighbor of  $B$ . Since  $A$  and  $B$  are real neighbors, the physical distance between  $X$  and  $X'$  is in the interval  $[0, 3r]$ . Under these assumptions, we study the relationship among the number of false positive alarms, the node density, and the number of wormholes in the network.

Figure 7 shows the simulation results. We can see that the node density does not have a large impact on the ratio between the number of false positive alarms and the total number of neighbor relations in the network. At the same time, when there are fewer than 3 pairs of wormholes, there are less than 1% of real neighbor relations that are wrongly labeled as wormholes. Previous research<sup>[12]</sup> shows that when the false positive alarm rate is smaller than 1%, its impacts on the average path length among legitimate nodes are very limited. Therefore, we conclude that when there are not many pairs of wormholes in the network, the false positive alarms will not significantly deteriorate

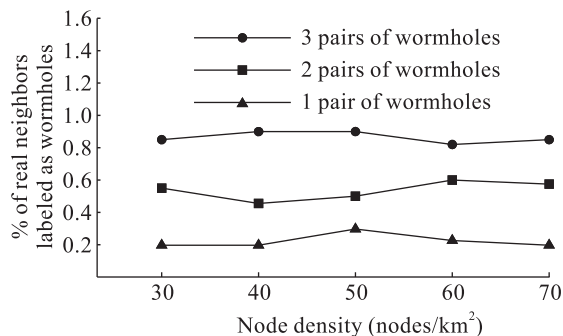


Fig. 7 Percent of real neighbors labeled as wormholes (false positive alarm)

the network performance.

## 6 Conclusions

In this paper we propose a wormhole detection mechanism for wireless networks based on physical layer network coding. When the sequences from two senders collide at the receiver, the starting point of collision is determined by the distances from the senders to the receiver. Two wireless nodes can then compare their starting points of collision to estimate the distance between them and verify the neighbor relationship. To turn this mechanism into a practical approach, we study various problems in the network layer and the physical layer. We also analyze the safety of the proposed approach and investigate the false alarm rate.

Immediate extensions to our approach consist of the following aspects. First, we will implement the proposed approach in software defined radio and test it in real network environments. Second, we will improve the efficiency of the detection mechanism by allowing multiple pairs of neighbors to share the same pair of senders. Finally, we will investigate using physical layer network coding to detect other stealth attacks on wireless network topology.

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