## Comments

## Corrections to "Unscented Filtering and Nonlinear Estimation"

SIMON J. JULIER AND JEFFREY K. UHLMANN

In the above paper [1], we surveyed the state of the art in unscented techniques for nonlinear estimation, and we provided a number of examples that illustrate its advantages over traditional linearized approaches such as the extended Kalman filter (EFK). Unfortunately, the description of the reentry example in Section VI-B of the paper was not completely and correctly explained and was not entirely consistent with the implementation used to generate Fig. 9(a)–(c). The force terms D(k) and G(k) acting upon the projectile are

$$\begin{split} D(k) &= \beta(k) \exp\left\{\frac{[R_0 - R(k)]}{H_0}\right\} V(k) \\ G(k) &= -\frac{Gm_0}{R^3(k)} \end{split}$$

and not the equations quoted in the paper. The process noise covariance matrix used on each filter is *not* be the same as the process noise used to drive the motion of the true projectile in the simulation. The process noise used to drive the simulation was specified in the paper; the process noise used to drive each filter is

	$2.4064 \times 10^{-5}$	0	0	
Q(k) =	0	$2.4064 \times 10^{-5}$	0	
	0	0	$10^{-6}$	

All the Jacobian matrices for the EKF were calculated numerically using a central difference scheme and a step size of  $10^{-3}$ .

The corrected graphs for Fig. 9(a)–(c) appear here. The conclusions that can be drawn from the results—that the EKF yields and inconsistent estimate, whereas the unscented Kalman filter yields a consistent estimate—remain the same as those presented in the original paper.

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S. J. Julier is with IDAK Industries, Jefferson City, MO 65109 USA (e-mail: sjulier@idak.com).

J. K. Uhlmann is with the Department of Computer Engineering and Computer Science, University of Missouri–Columbia, Columbia, MO 65211 USA (e-mail: uhlmannj@missouri.edu).

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**Fig. 9.** Mean squared errors and estimated covariances calculated by an EKF and an unscented filter. In all the graphs, the solid line is the mean squared error calculated by the EKF, and the dotted line is its estimated covariance. The dashed line is the unscented mean squared error and the dot–dashed line its estimated covariance. (a) Results for  $x_1$ . (b) Results for  $x_3$ . (c) Results for  $x_5$ .

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## REFERENCES

 S. J. Julier and J. K. Uhlmann, "Unscented filtering and nonlinear estimation," *Proc. IEEE*, vol. 92, pp. 401–422, Mar. 2004.

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